



NMR of Solids

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Interactions of nuclear spins in a solid

E_Z = Zeeman effect

E_{RF} = RF field

E_{CS} = Chemical shift

E_J = JJ coupling

E_D = Dipolar interactions

E_Q = Quadrupolar coupling

E_{ij} = Unpaired electrons

$E_Z \gg$ other interactions

Very often some effects are masked by the others

For example $E_D \gg E_J$

$E_X = K$ (spin factor) [space factor $f(\theta)$]

θ = angle between an axis of the system and B_0

Chemical Shift δ

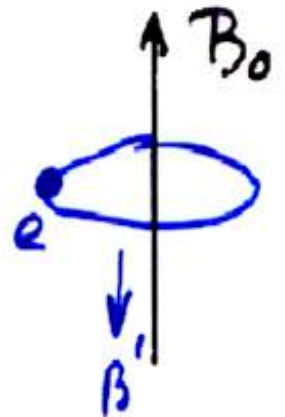
$$\omega = \gamma B$$

$$\text{Sample: } 2\pi\nu_s = \gamma B_0(1 - \sigma_s)$$

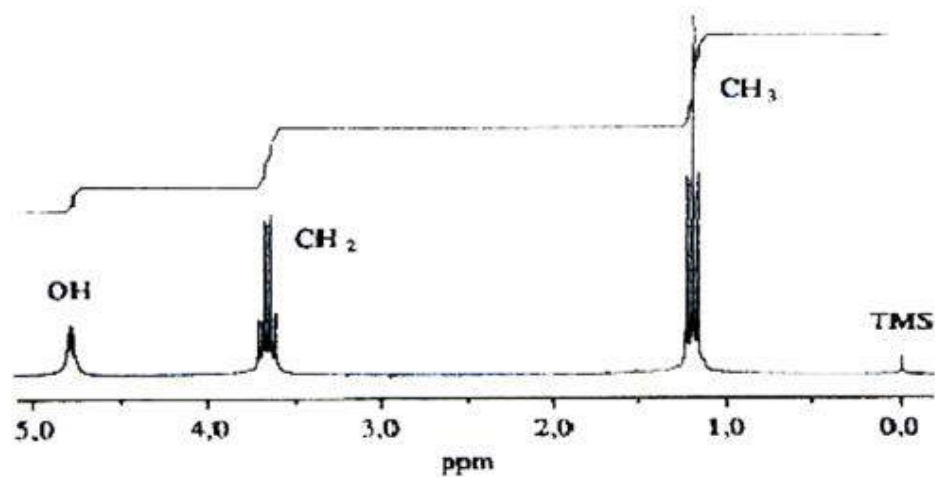
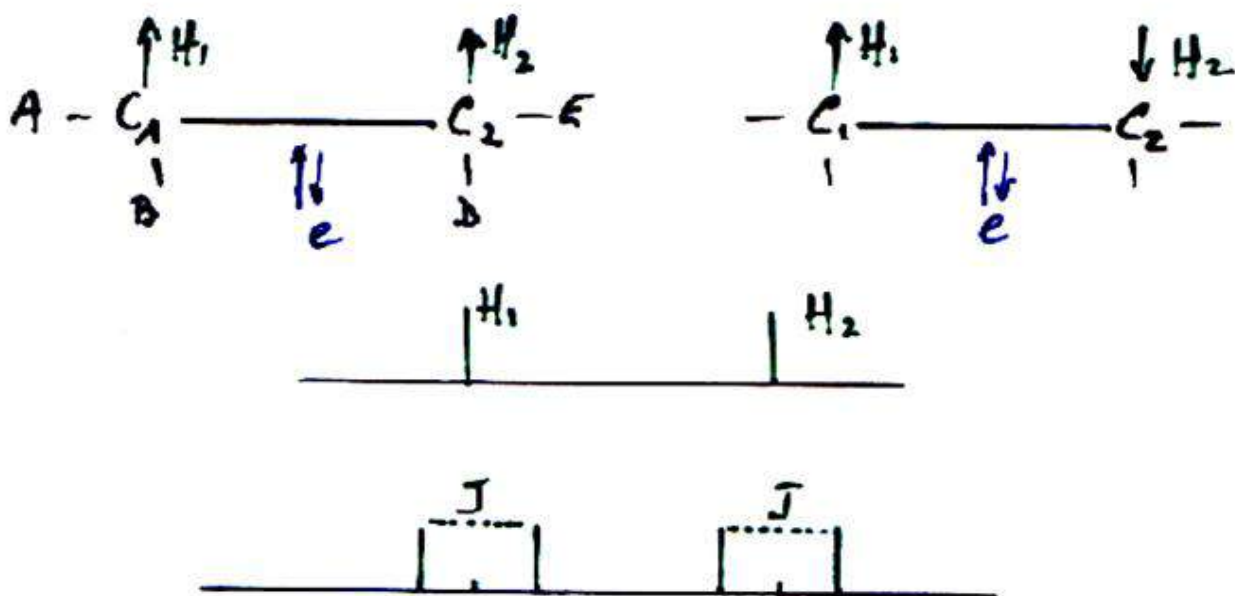
$$\text{Reference: } 2\pi\nu_r = \gamma B_0(1 - \sigma_r)$$

$$\Delta N = \nu_r - \nu_s = \frac{\gamma B_0}{2\pi} (\sigma_s - \sigma_r)$$

$$\delta = \frac{\gamma B_0 / 2\pi (\sigma_s - \sigma_r)}{\gamma B_0 / 2\pi (1 - \sigma_r)} \sim \sigma_s - \sigma_r \text{ ppm}$$

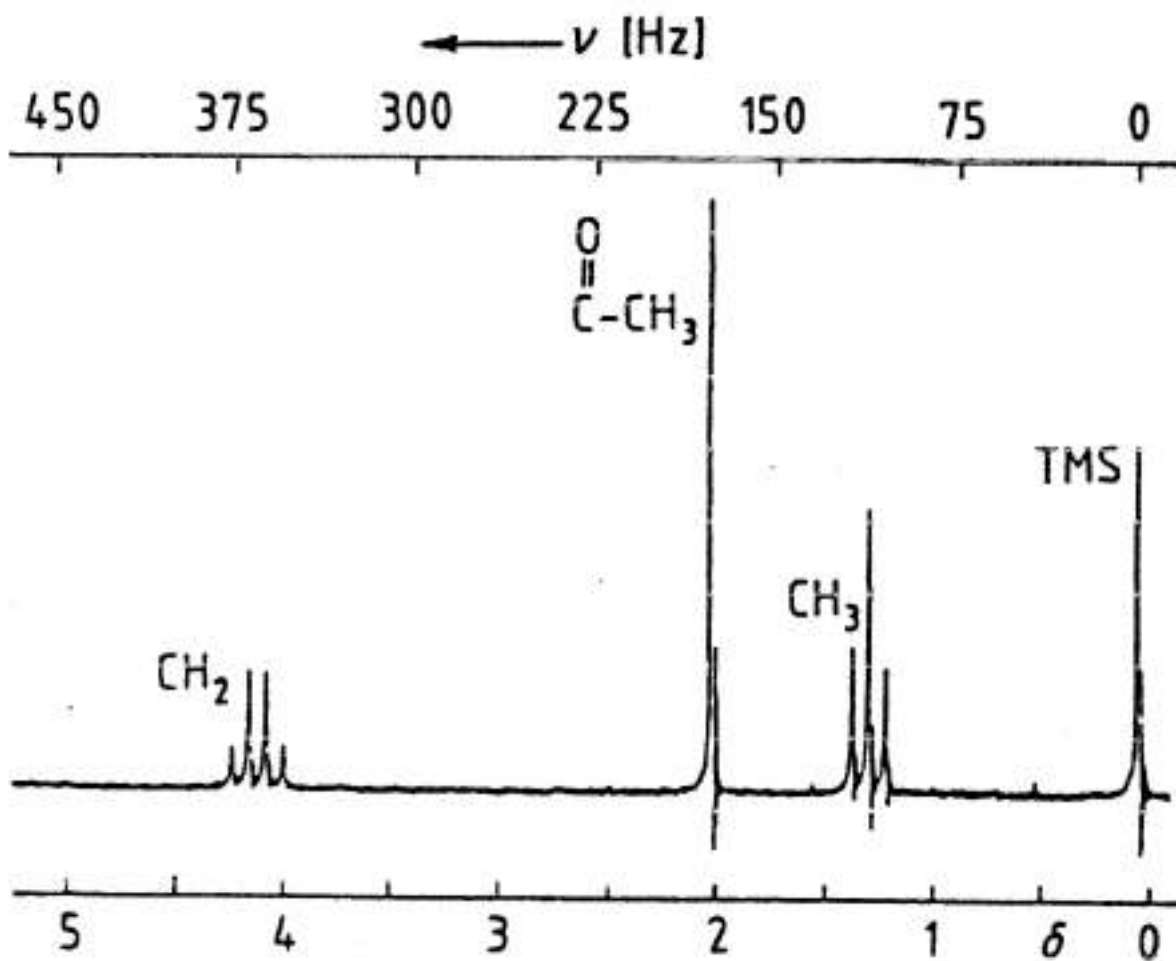
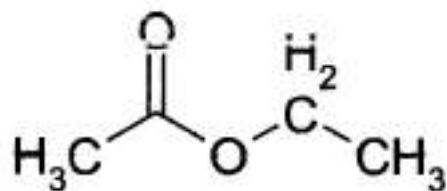


Spin-spin coupling J



$$2nI + 1$$

Ethyl acetate



Nuclear Electric Quadrupole Moment

non-spherical distribution of nuclear charge

A

B

C

D



$$I = 0$$

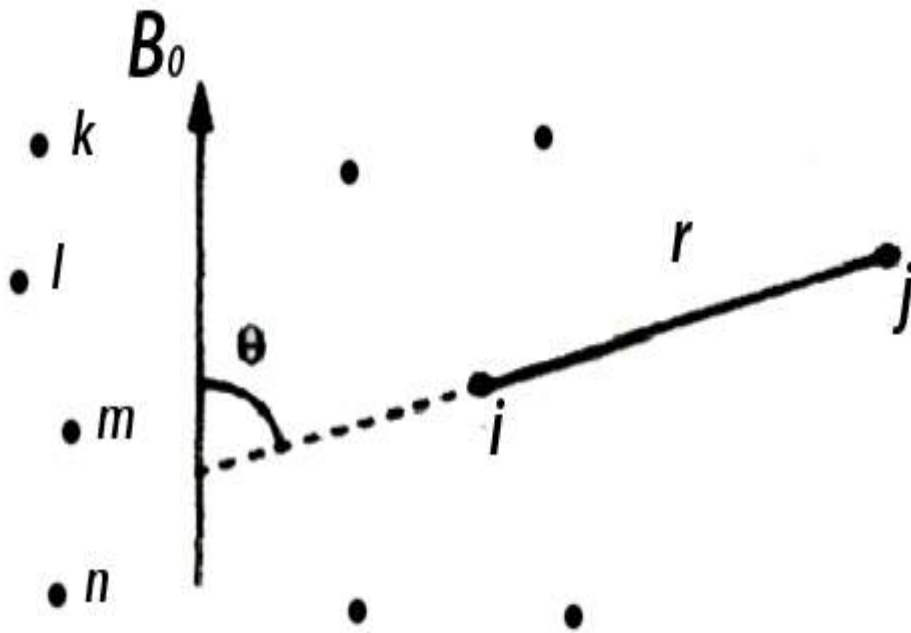
$$I = 1/2$$

$$I \geq 1 ; eQ > 0$$

$$I \geq 1 ; eQ < 0$$

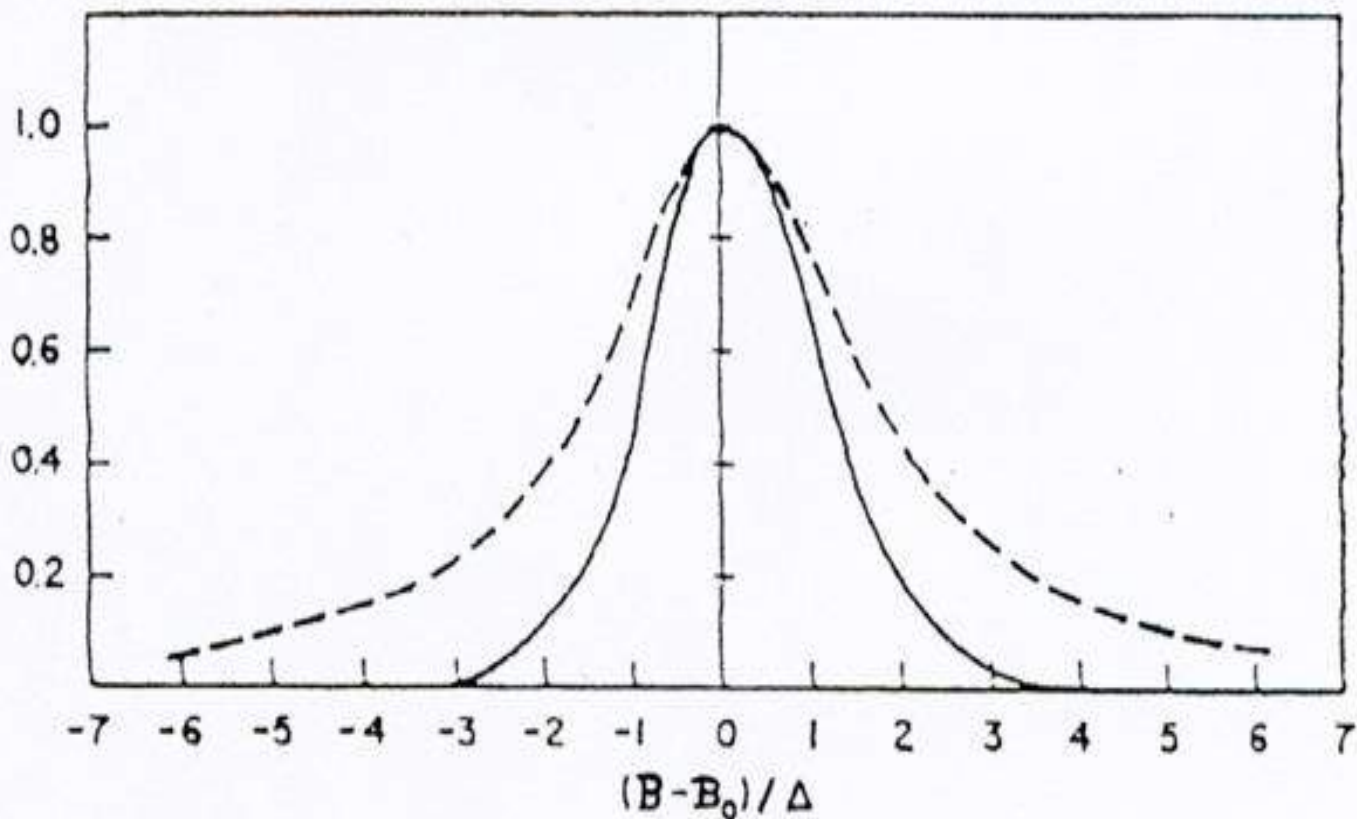
Dipolar Magnetic Interaction between nuclei

$$\text{DMI} = \text{CONSTANT} \cdot (1 - 3 \cos^2 \theta) \cdot r^{-3}$$



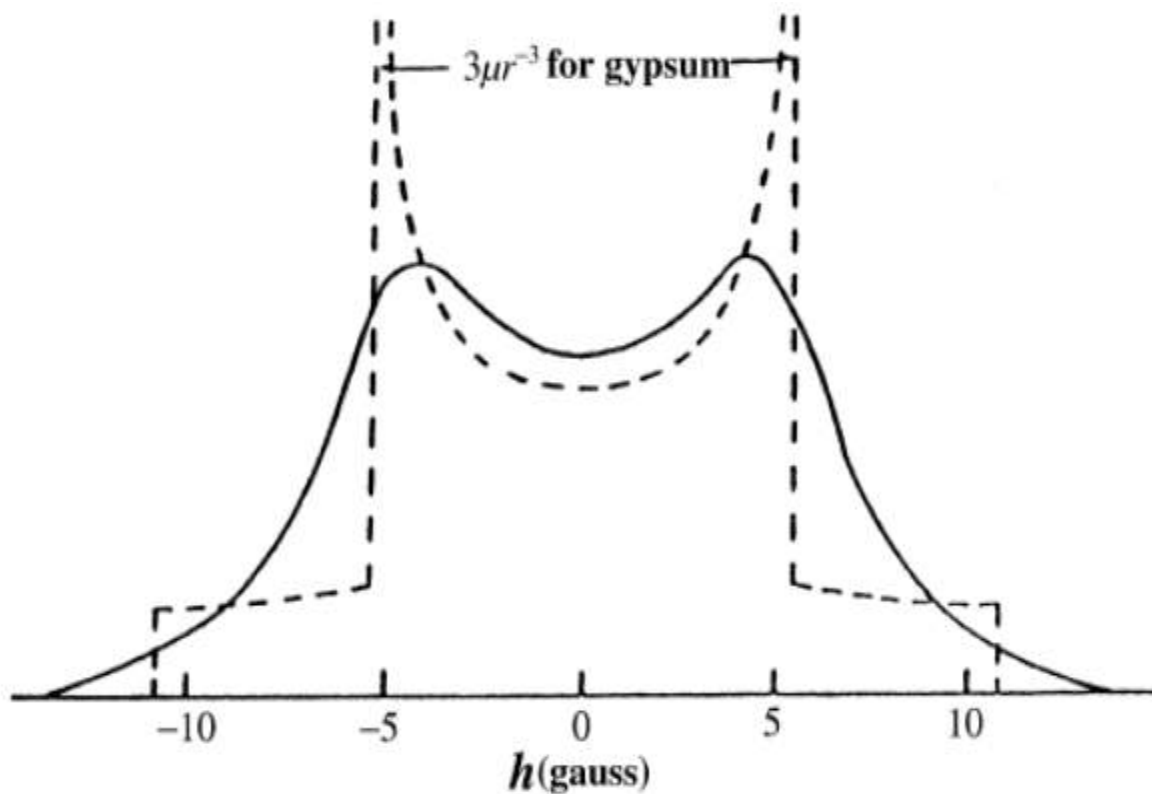
For powder samples the interactions must be summed up over all directions.

Gaussian (solid line) and Lorentzian (broken line) curves of solids



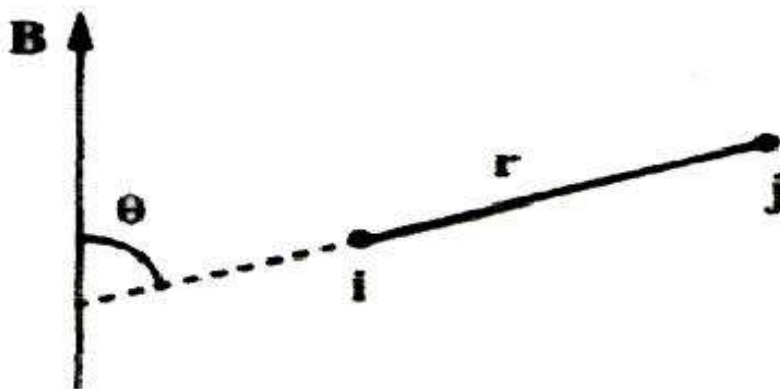
Spectrum for a two spins magnetic configurations

- - - - - theoretical; _____ real



Dipolar Magnetic Interaction between two ^1H nuclei

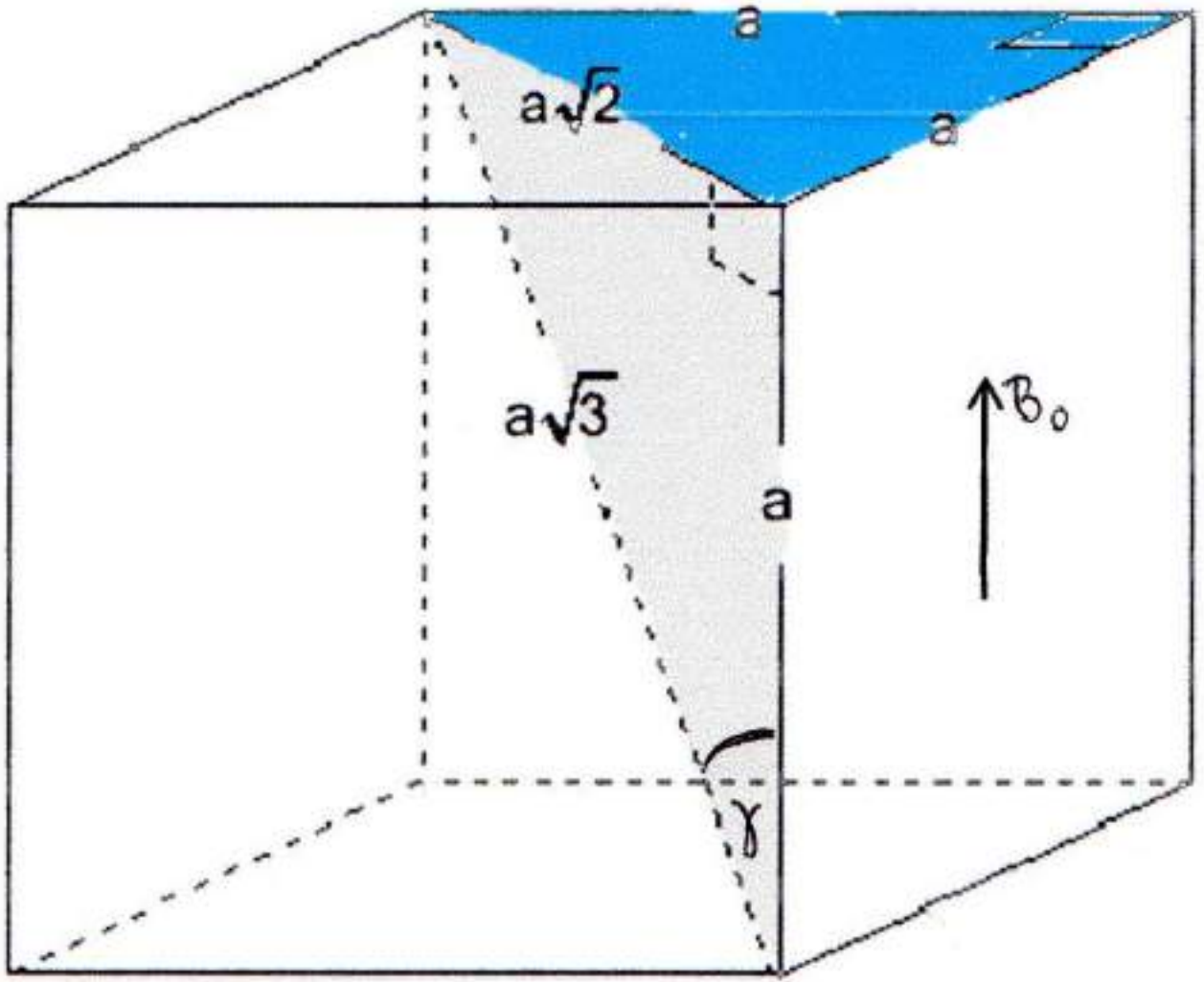
$$\text{DMI} = \text{CONSTANT} \cdot (1 - 3 \cos^2 \theta) \cdot r^{-3}$$



For powder samples the interactions must be summed up over all directions.

$$\text{DMI} = 0 \quad \text{if} \quad \cos \theta = 1/\sqrt{3}$$

$$\theta = 54^\circ 44'$$

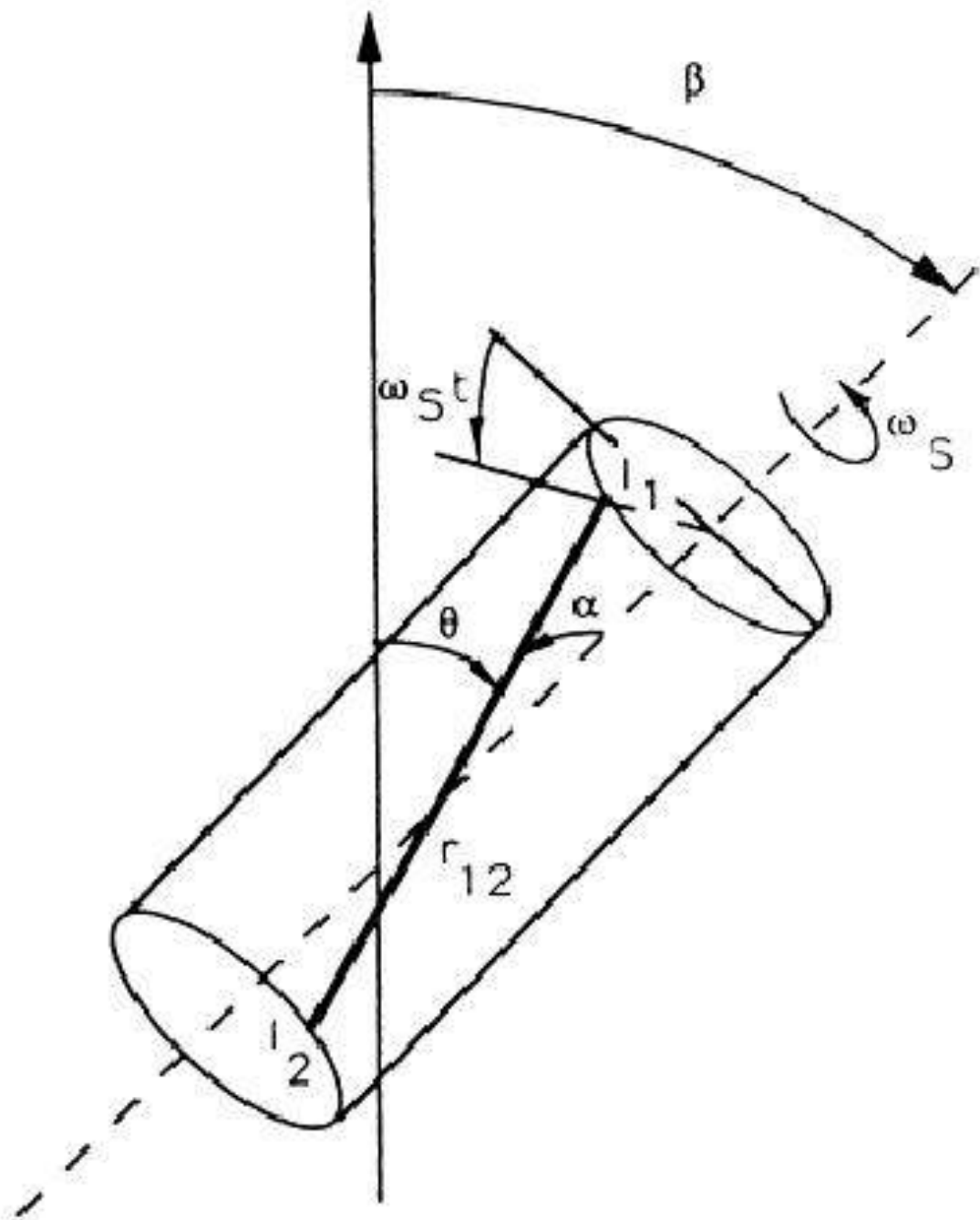


$$a^2 + (a\sqrt{3})^2 = (a\sqrt{2})^2 + 2a.(a\sqrt{3})\cos\gamma$$

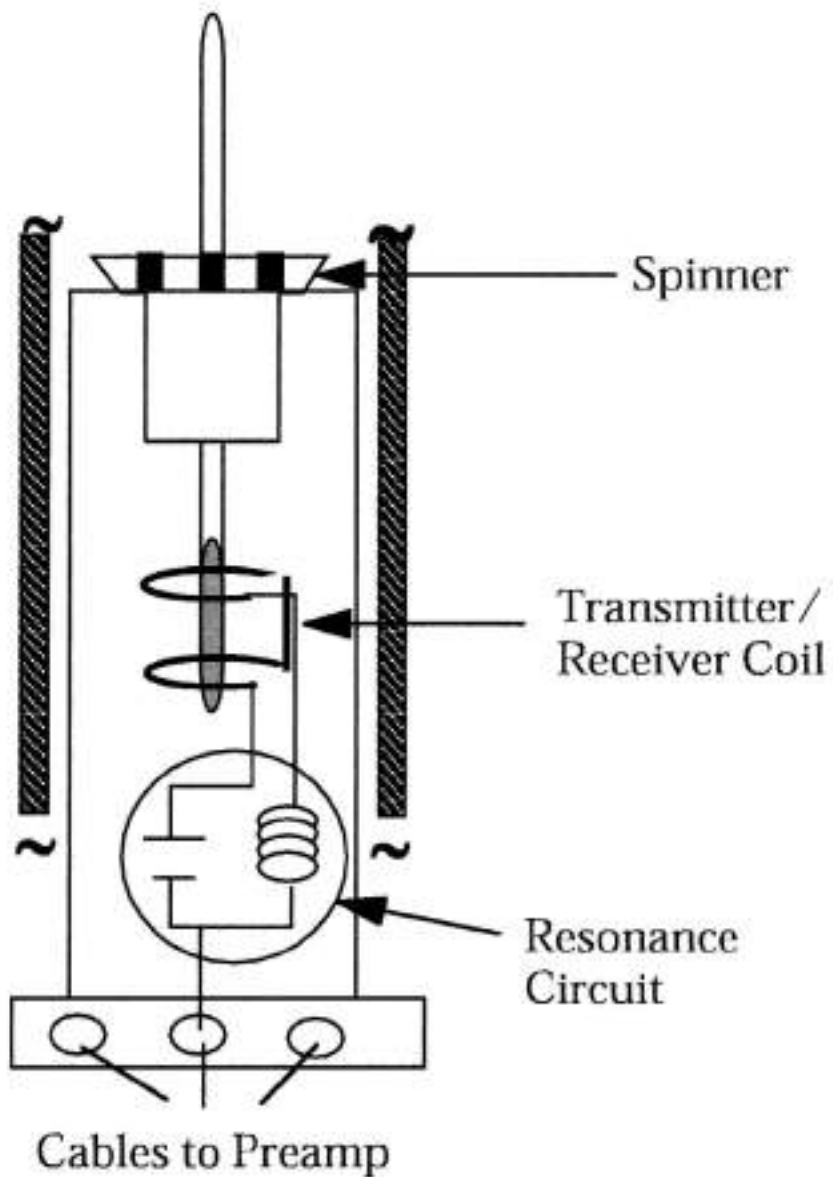
$$\cos\gamma = 1/\sqrt{3}$$

$$\gamma = 54^\circ 44'$$

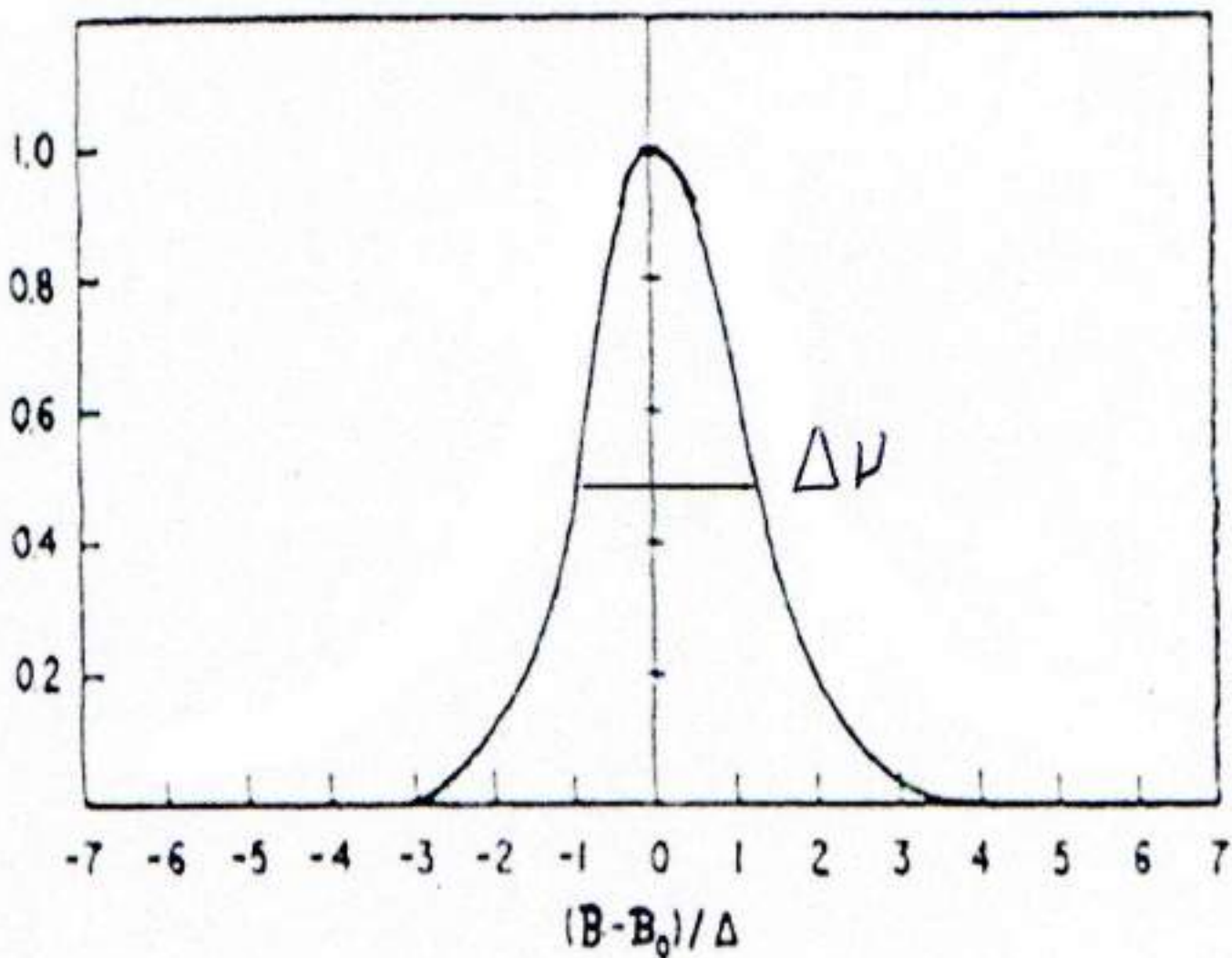
Magic angle spinning (MAS)



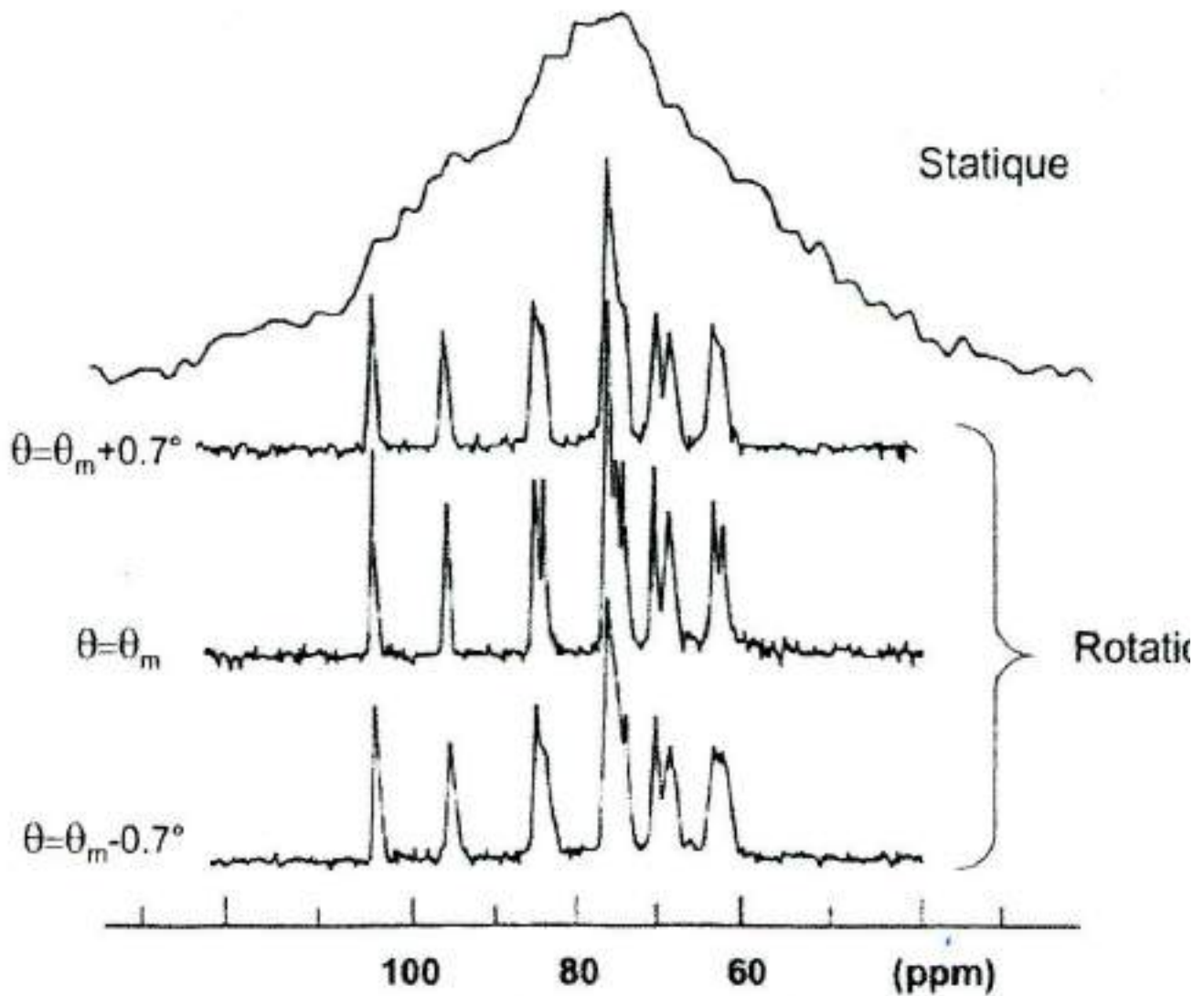
SPINNER



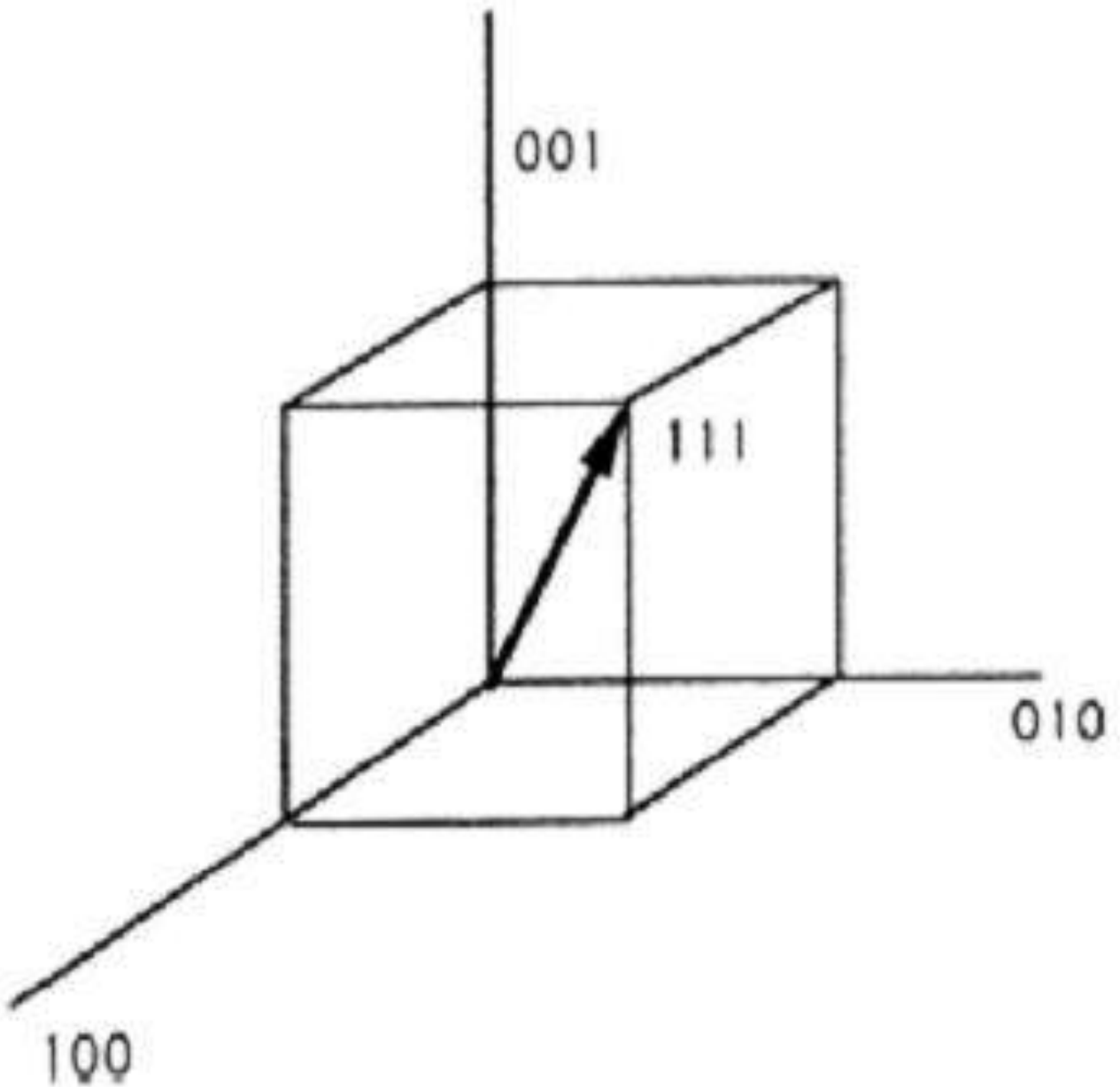
To obtain a HR spectrum, the rotation of the sample, ν_r , must be faster than the line width, $\Delta\nu$, without rotation.



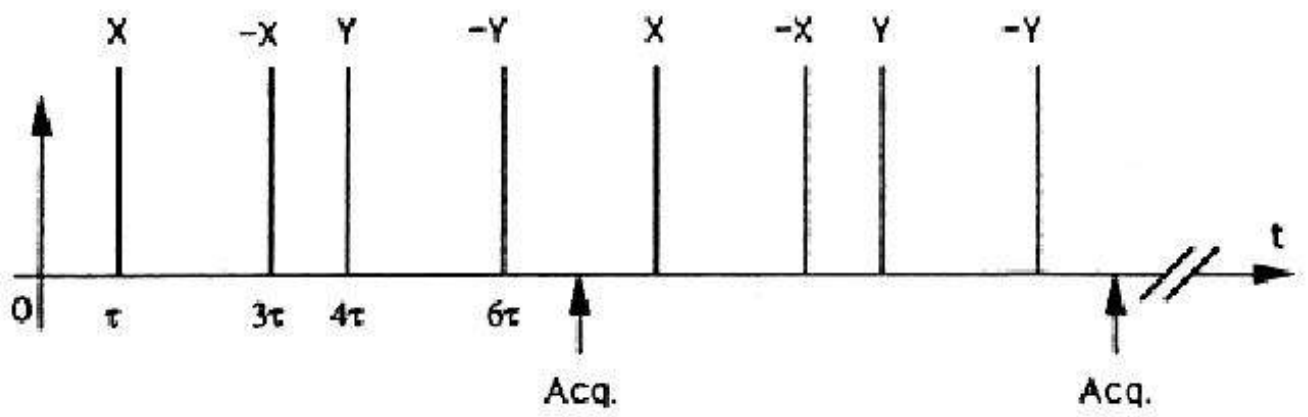
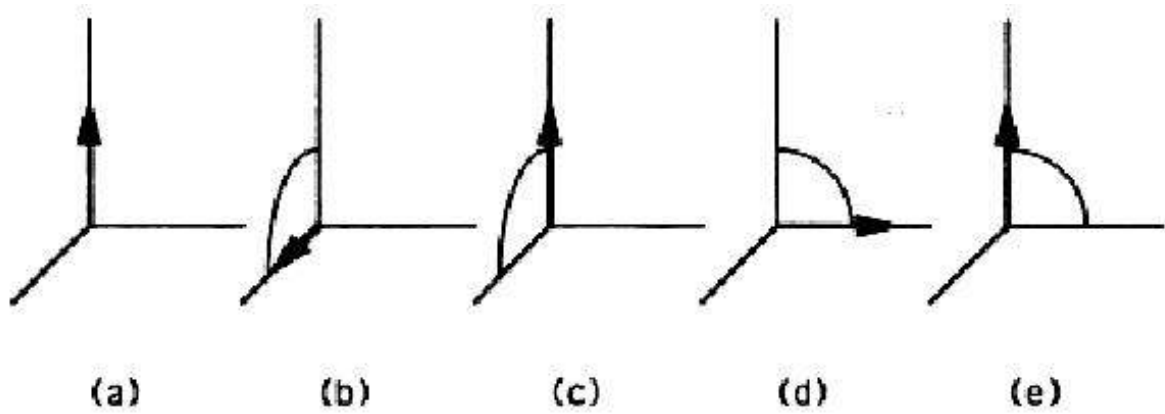
Accuracy of the angle



The angle between the diagonal of the cube and the side is = the magic angle

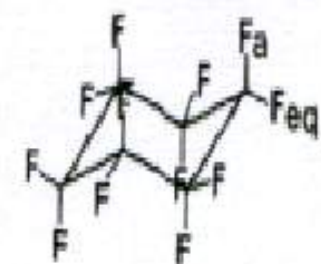


Pulse sequences



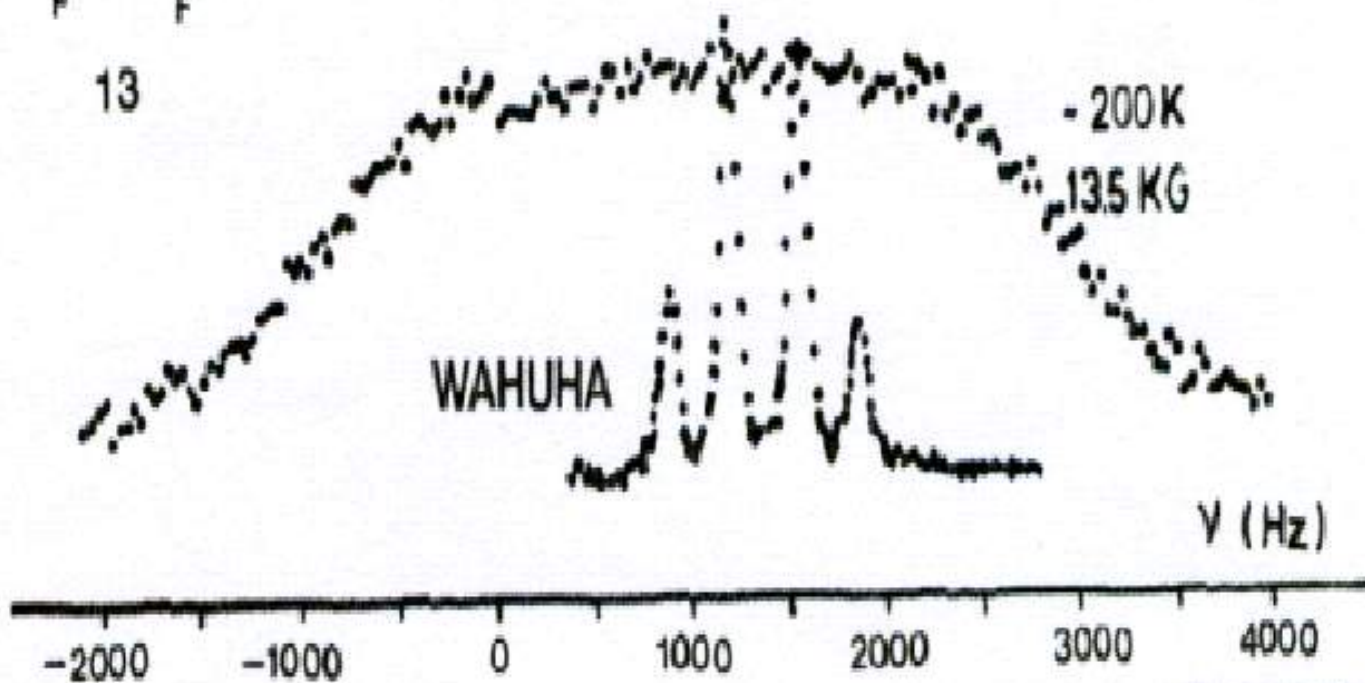
Examples

^{19}F NMR. Application of the Wahuha sequence to perfluorocyclohexane C_6F_{12} at 200 K



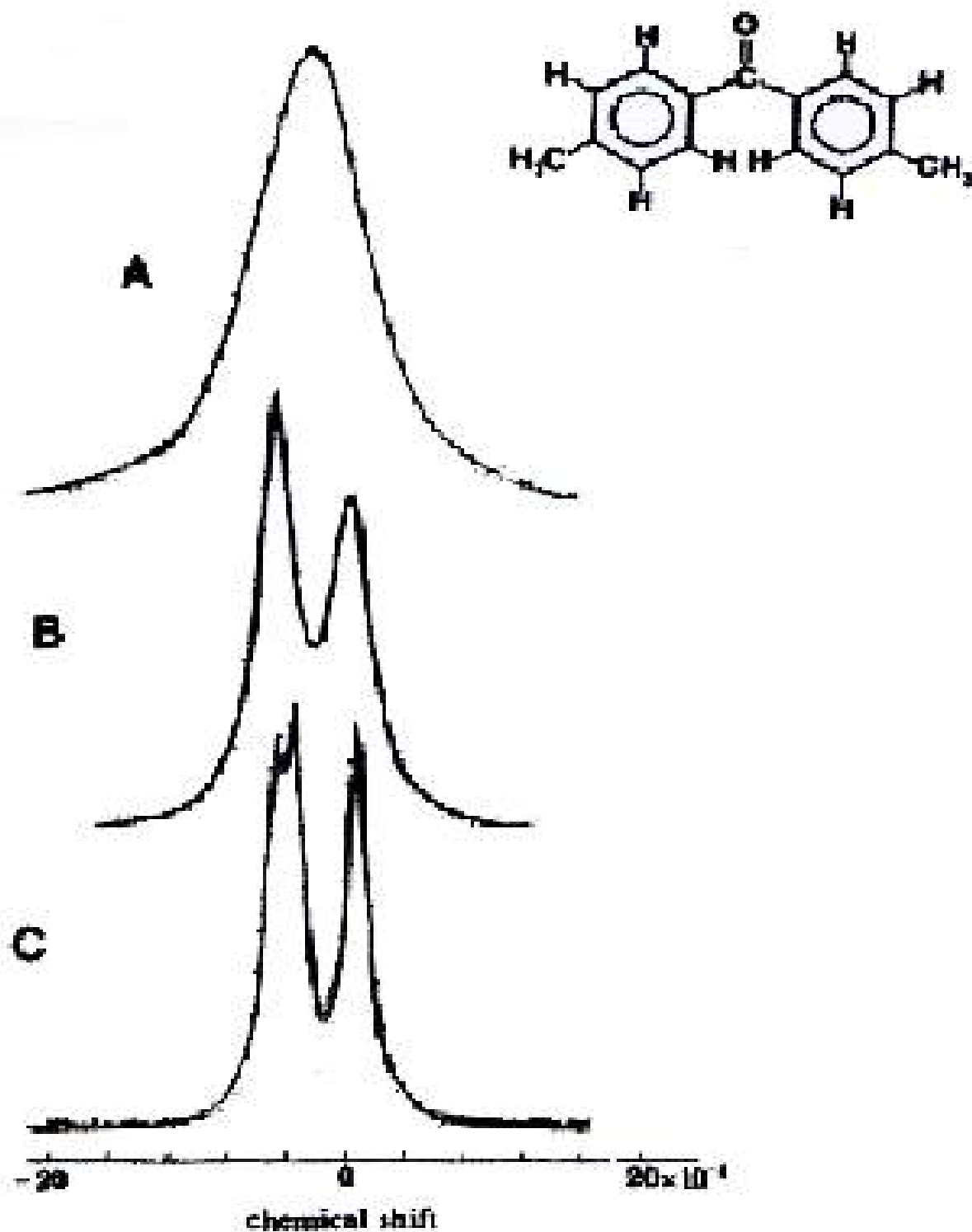
13

← 0.5 GAUSS →



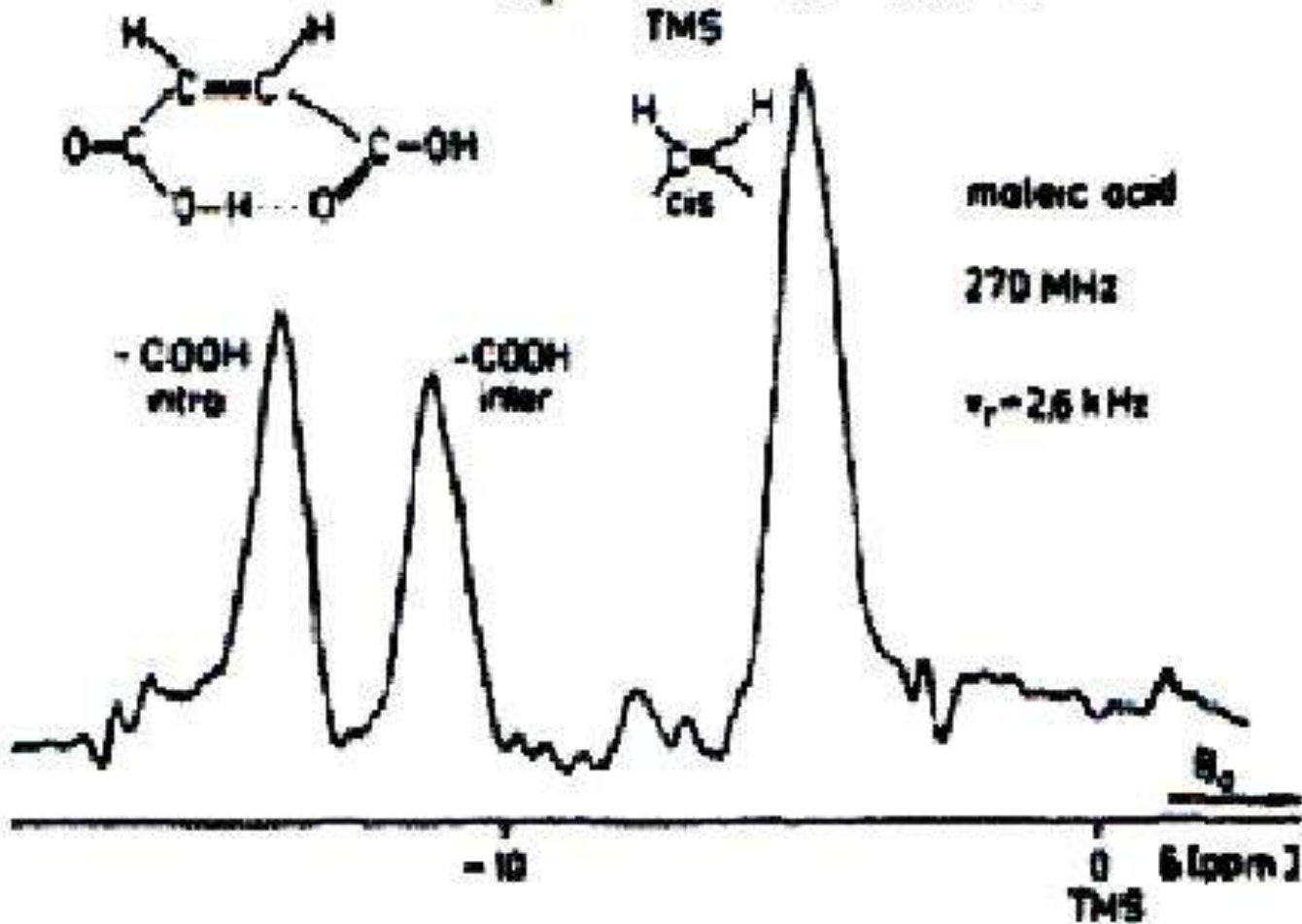
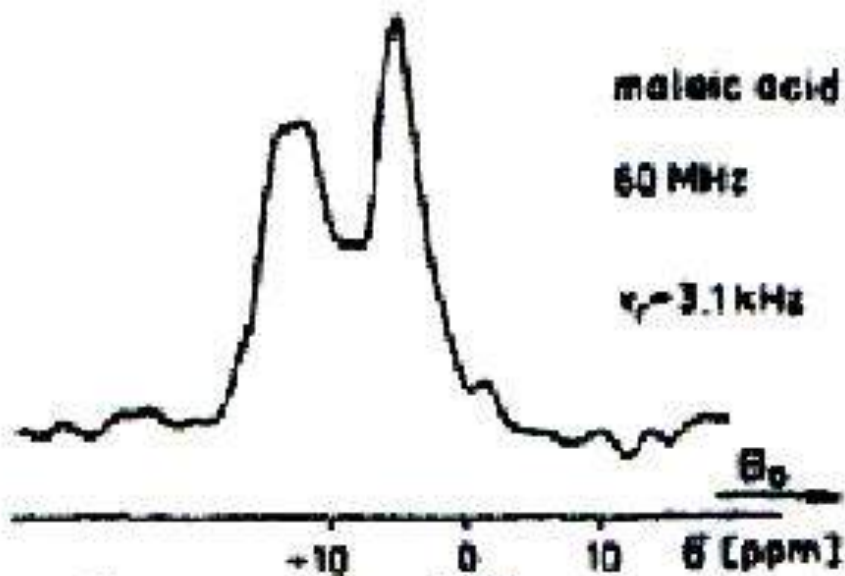
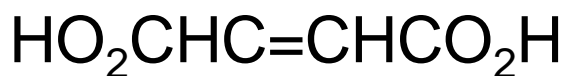
4,4'-dimethylbenzophenone

A: MREV-8; B: MREV-8 + MAS; C: BR24 + MAS

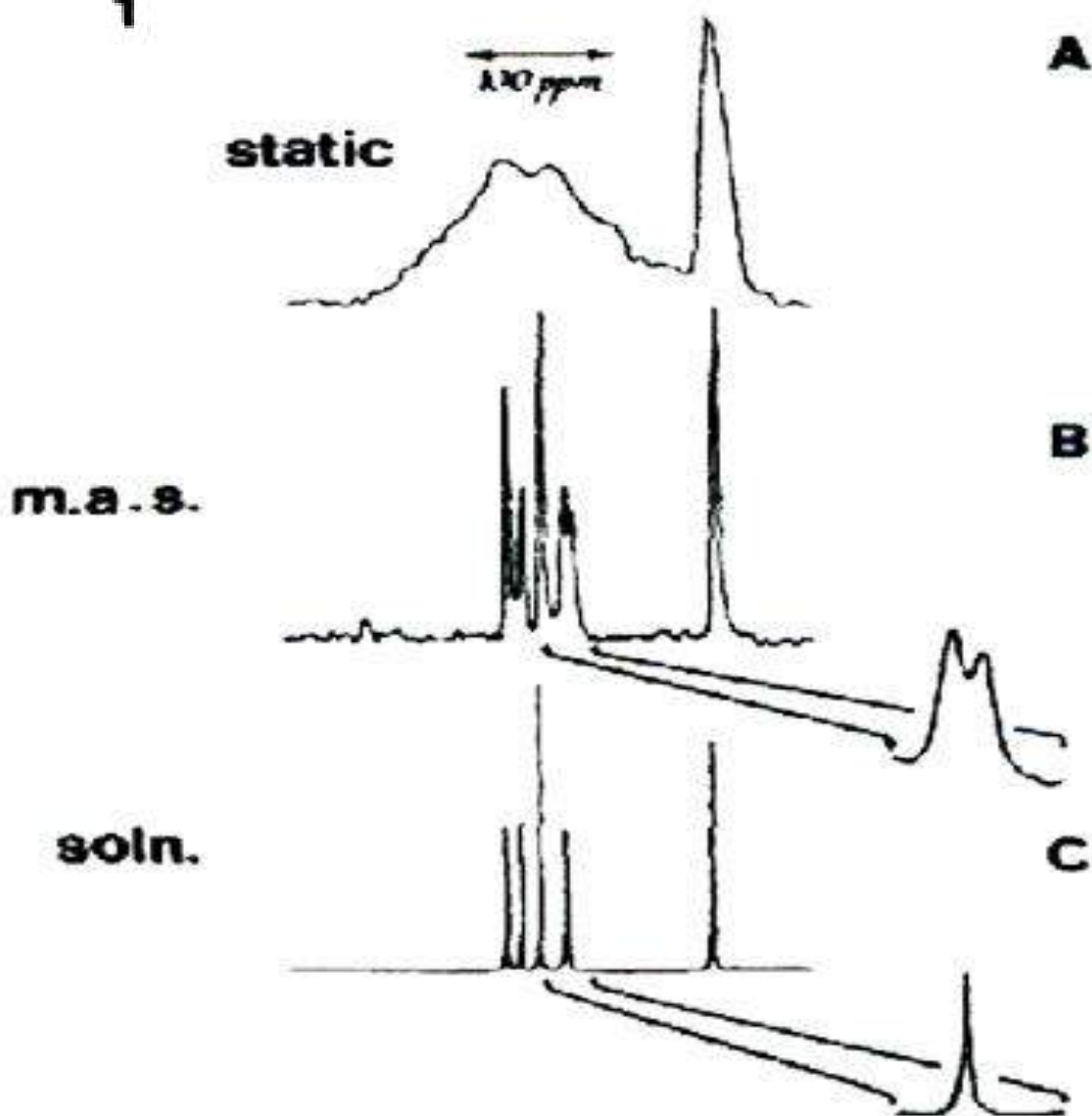
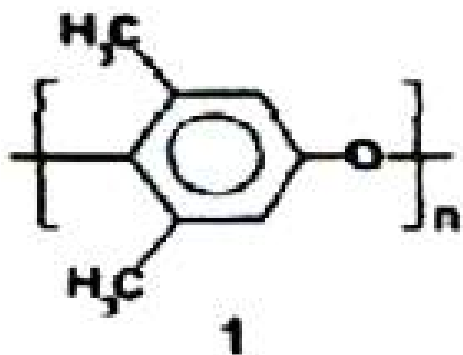


Maleic acid at 60 and 270 MHz

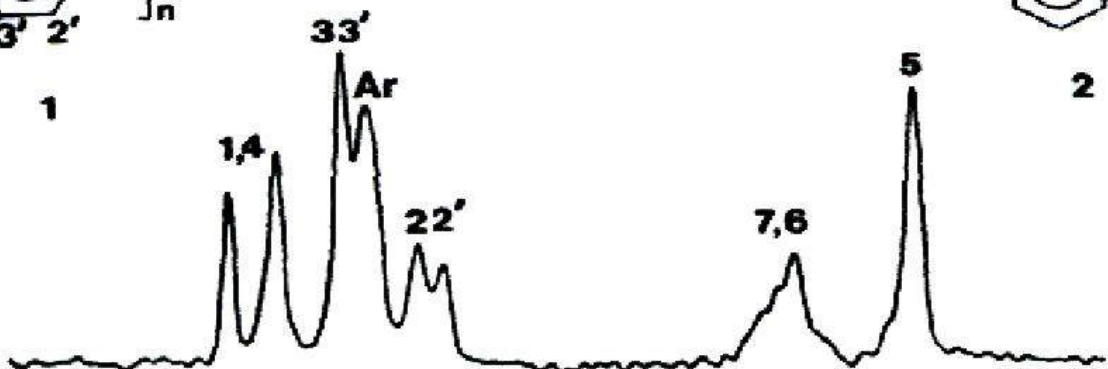
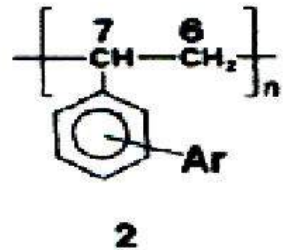
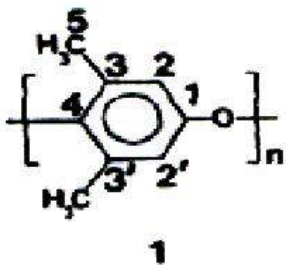
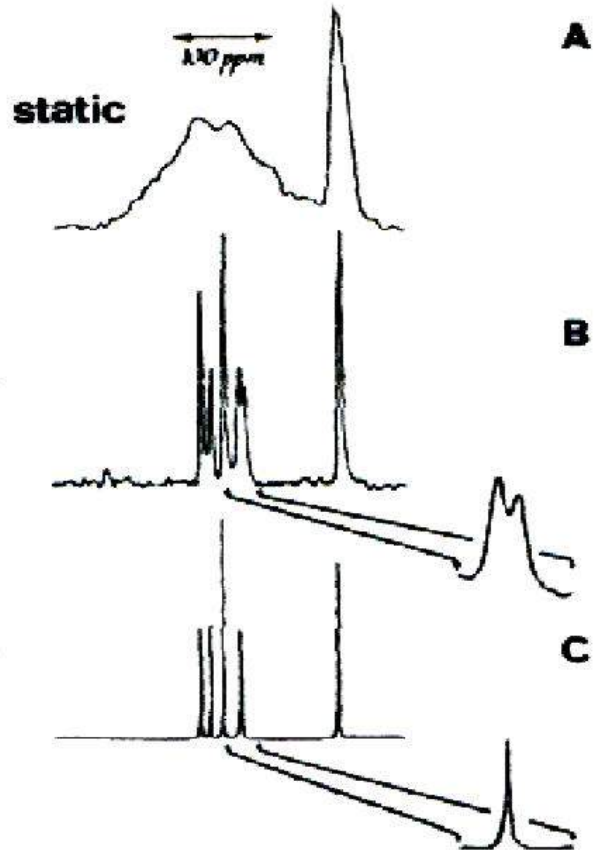
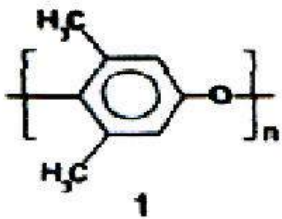
Influence of hydrogen bond



Poly phenylene oxide

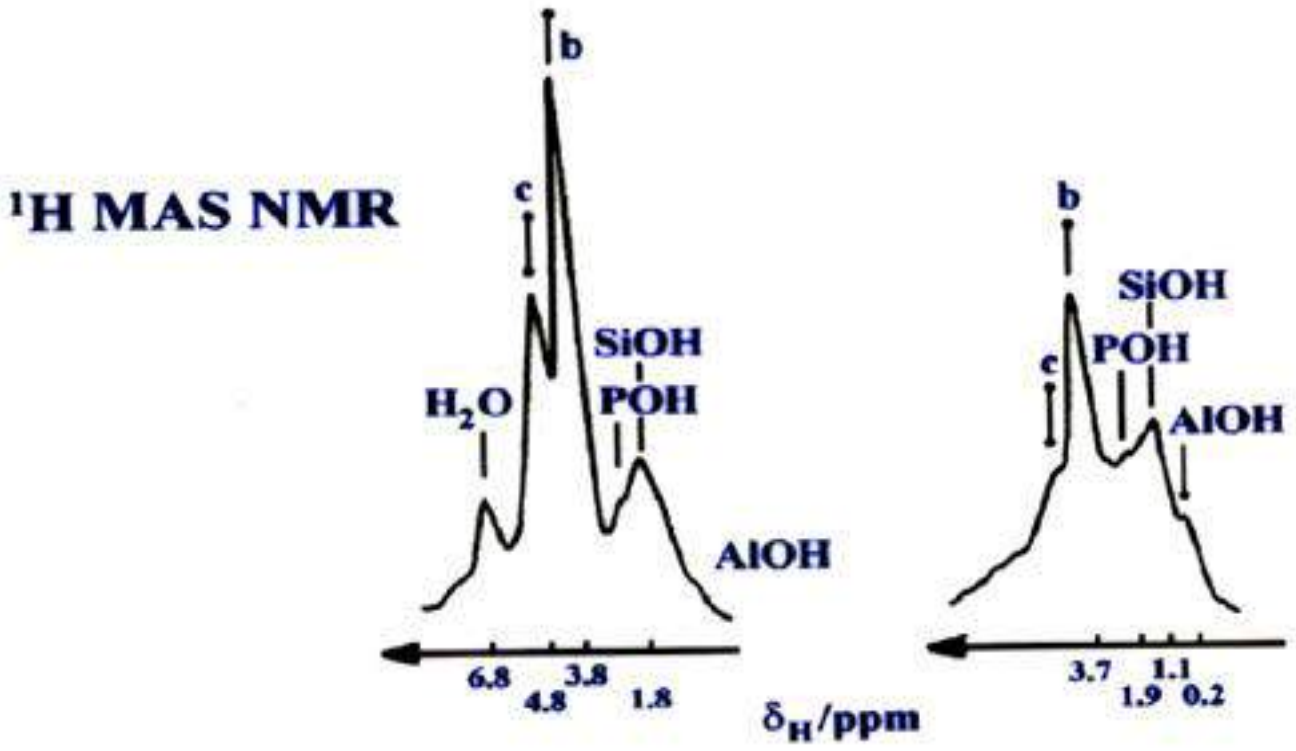
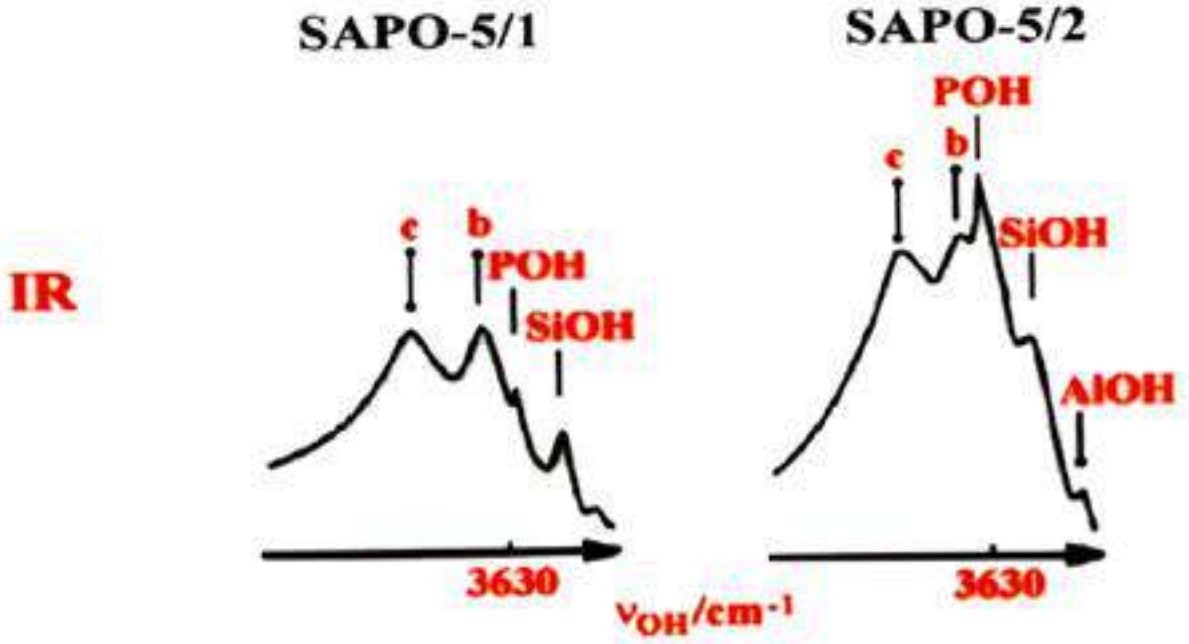


Poly phenylene oxide and blend with polystyrene

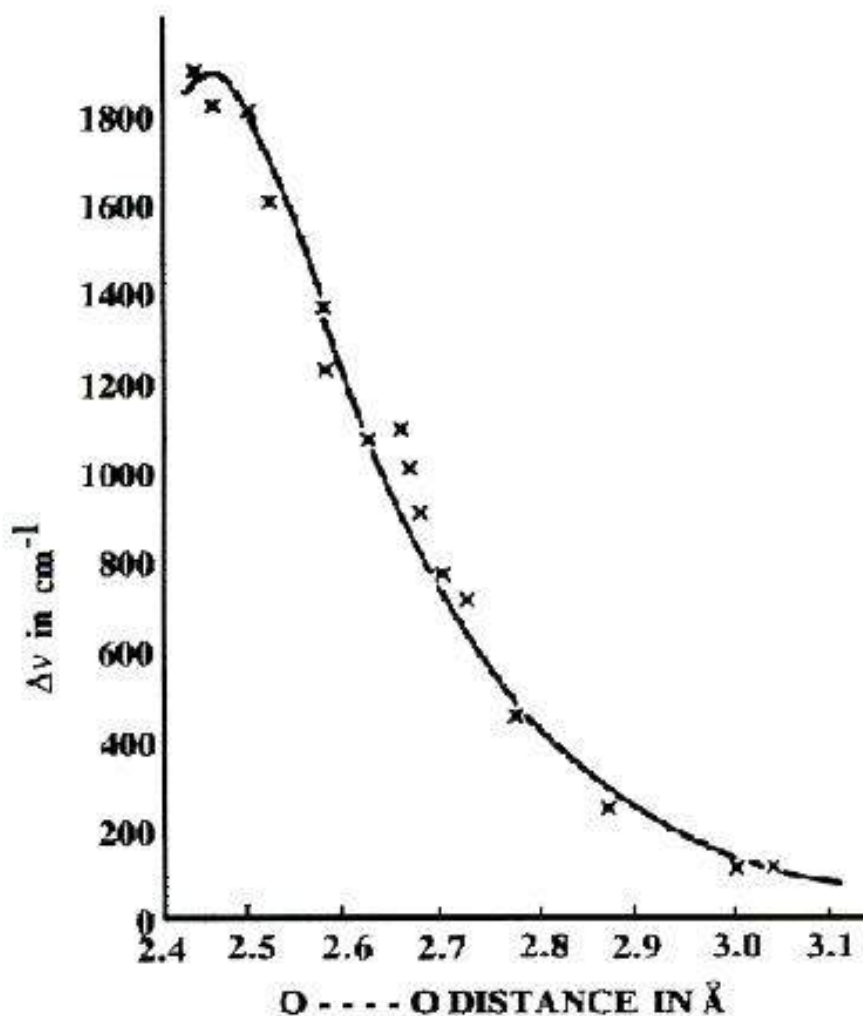


OH groups in zeolites

Hydrogen bonds: δ (OH) and ν (OH)



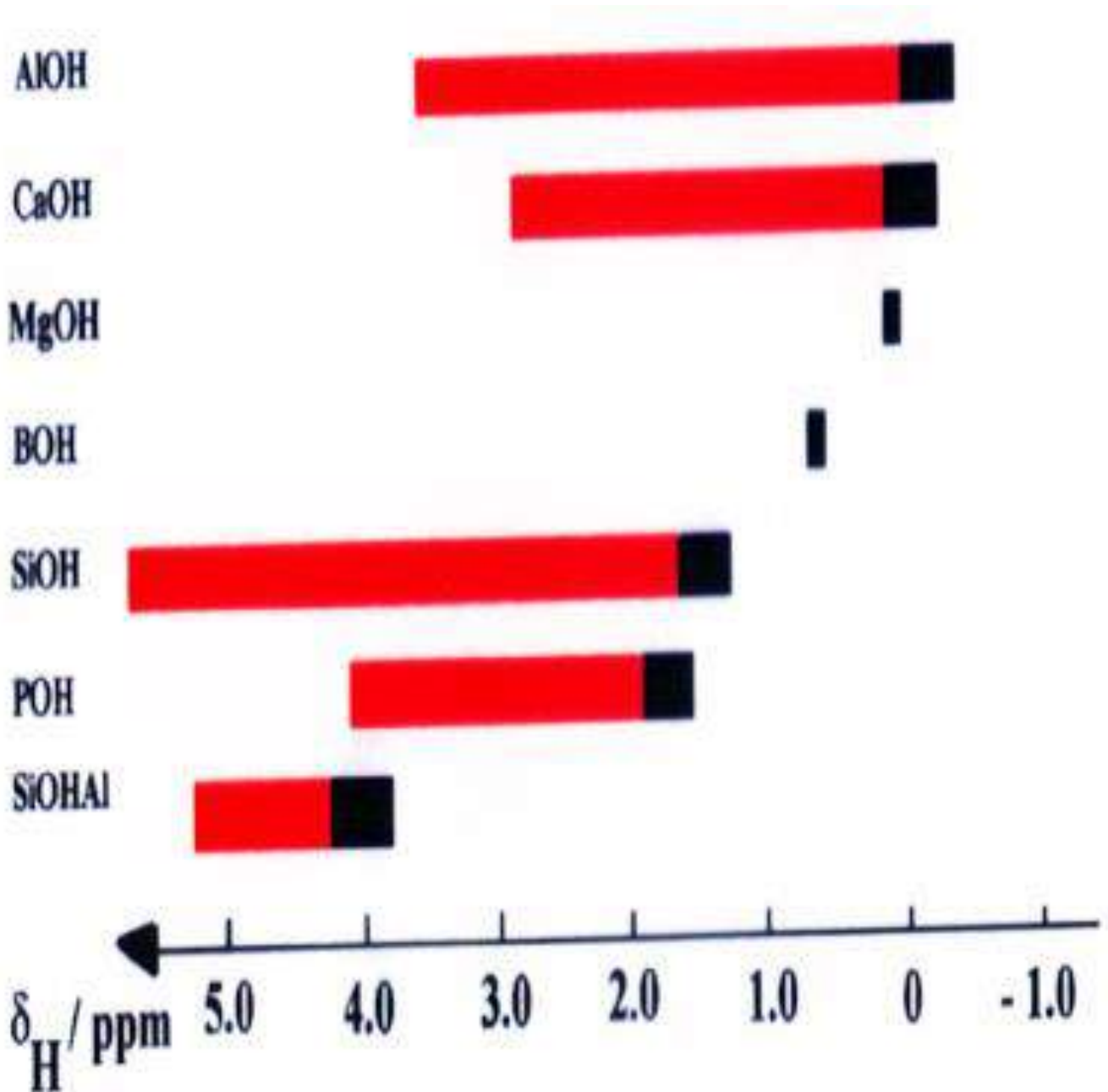
IR: $\Delta\nu$ in cm^{-1} against hydrogen bond



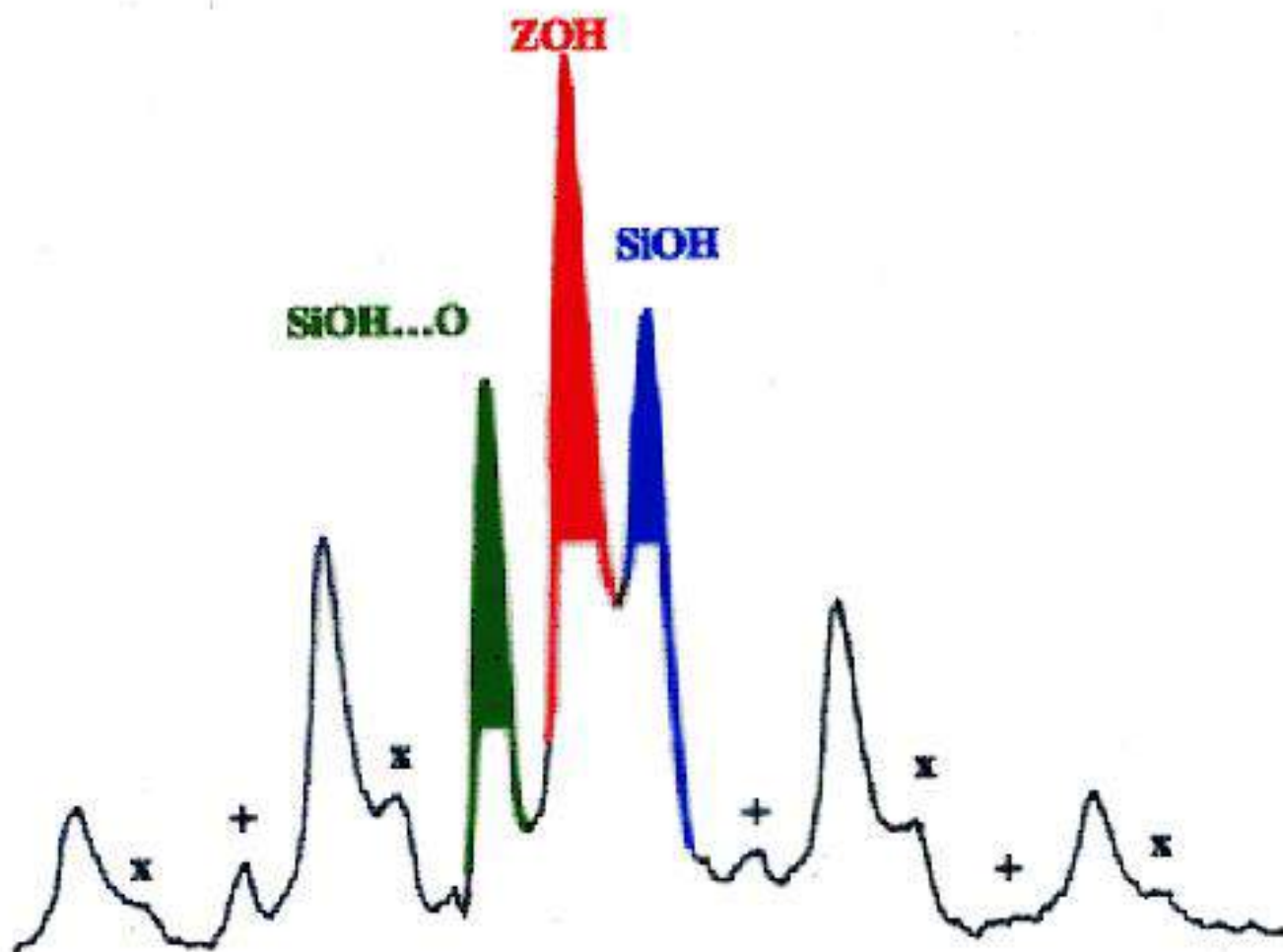
The relation between OH frequency shift and O - - - O distance during hydrogen-bonding interaction

Influence of hydrogen bonds

Experimental chemical shift δ_H of isolated (black) and interacting (red area) groups in zeolites



Anhydrous H-mordenite



Spins with low γ

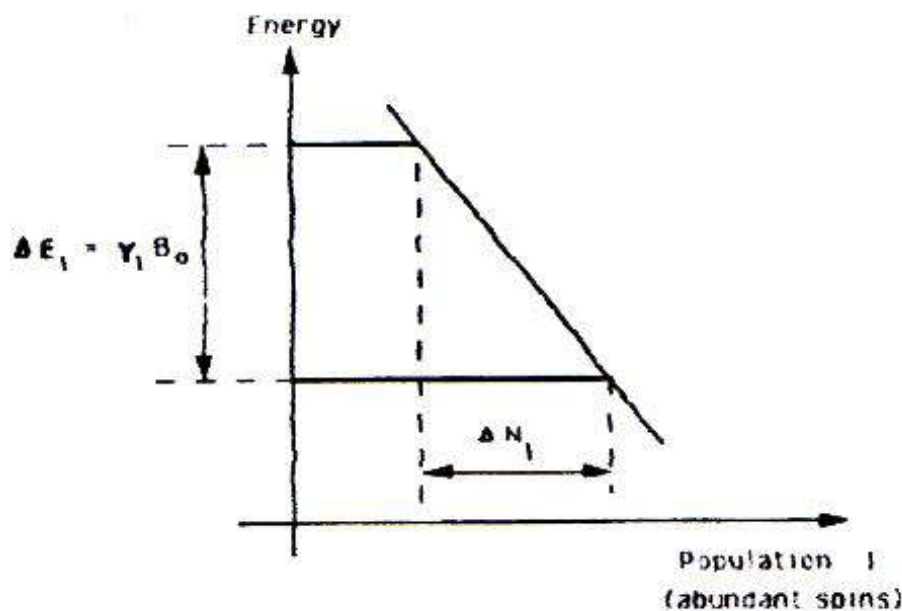
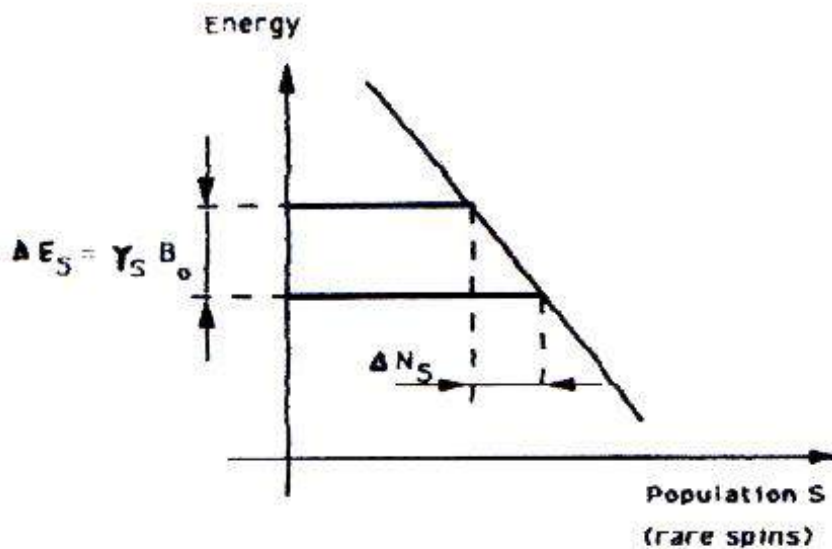
Polarization transfer from abundant spins I (high γ_I) to the low concentration spins S (low γ_S)

-:-:-:-:-:-:-:-

For spins $1/2$,

magnetization : $M = (N/4k_B T) \gamma \hbar B_0$

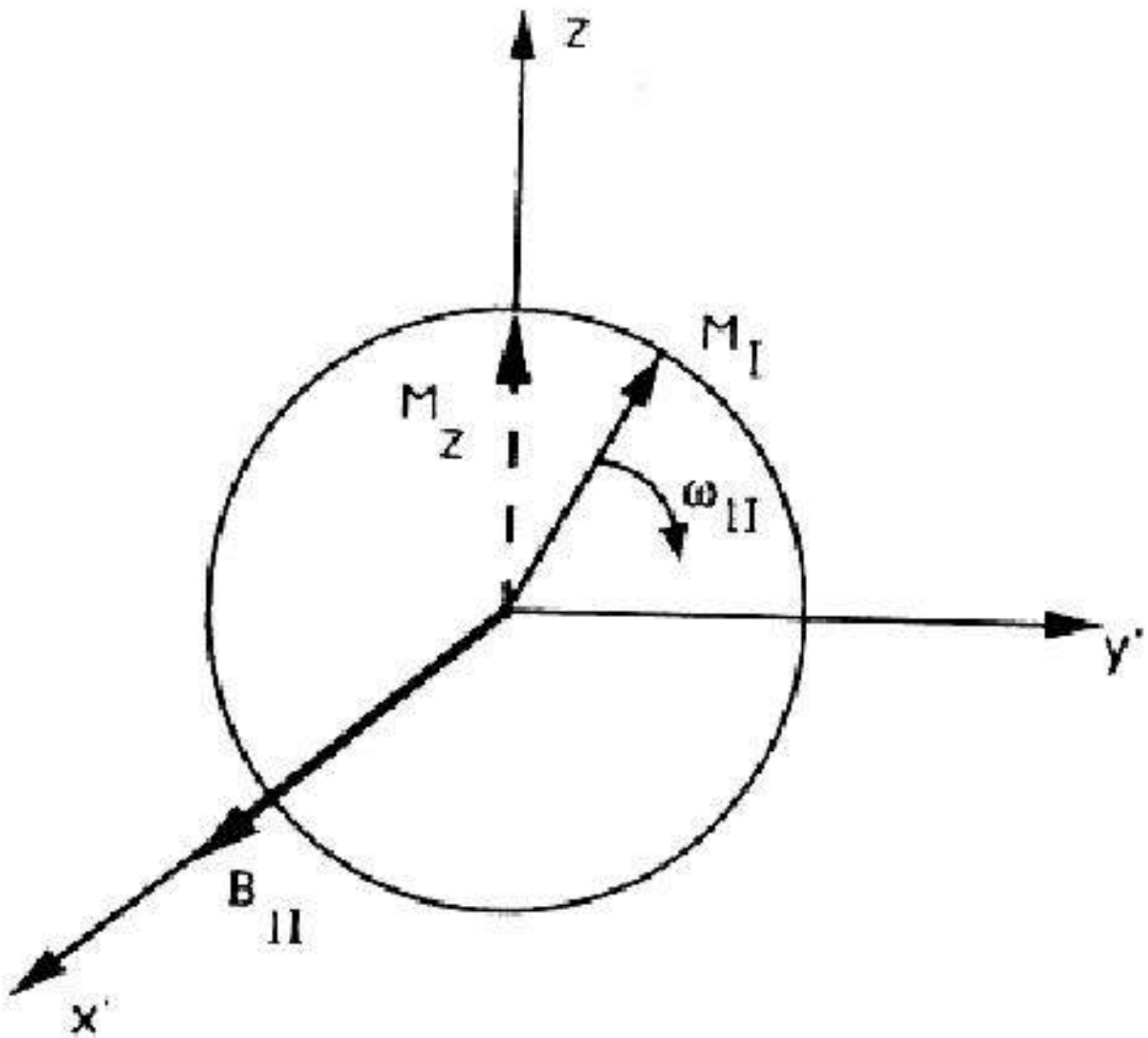
Signal/ noise ratio: $\propto (I+1) N \gamma^{5/2}$

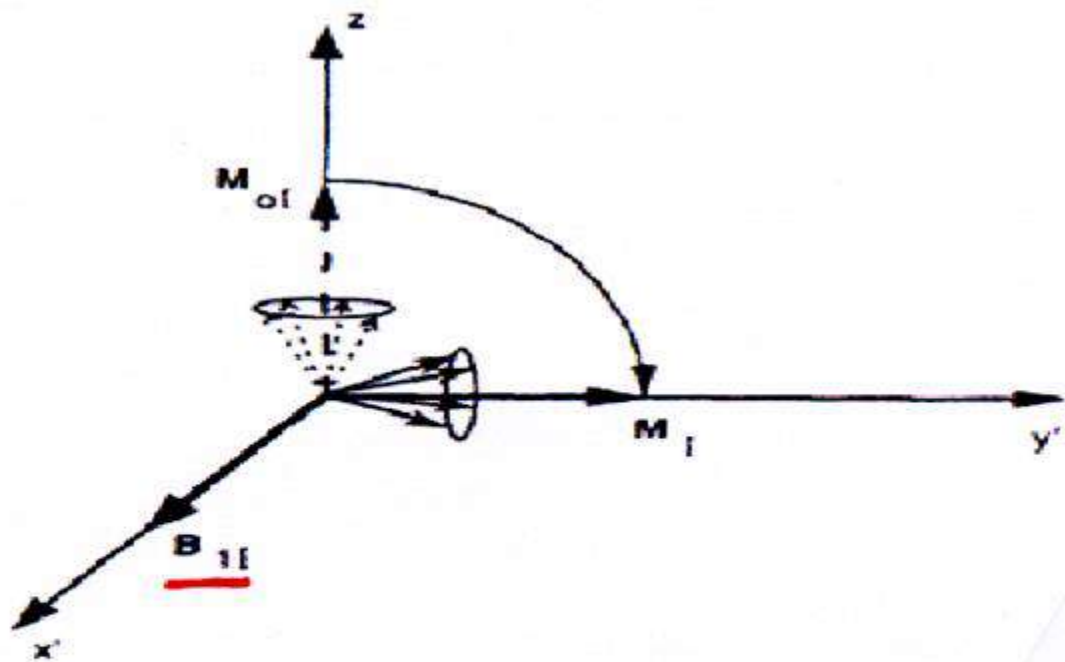


For the same B_0 , ΔN_I and ΔN_S are proportional to γ_I and γ_S .

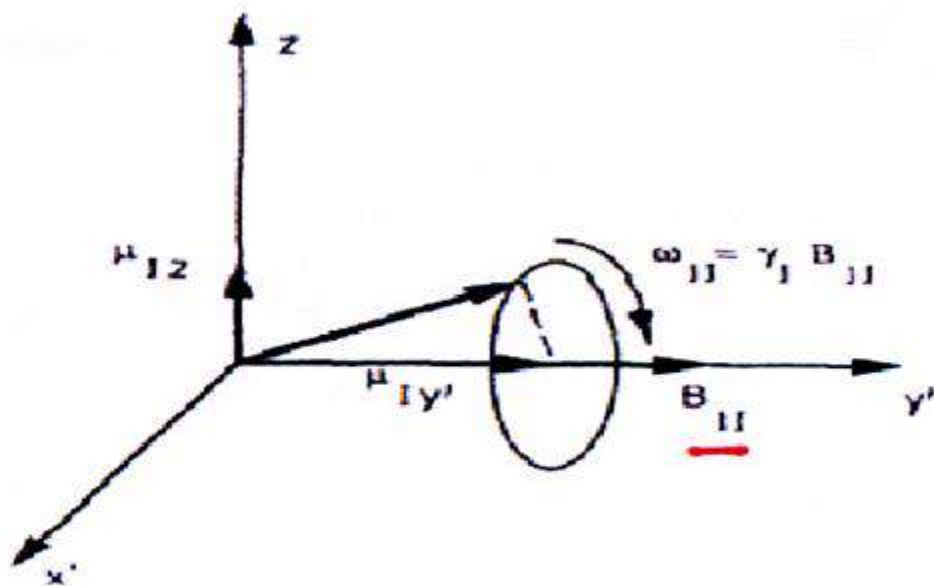
$$\Delta N_I / \Delta N_S = \gamma_I / \gamma_S$$

In the rotating framework
 B_{11} along x' \rightarrow rotation of M_I in the
plane zoy'





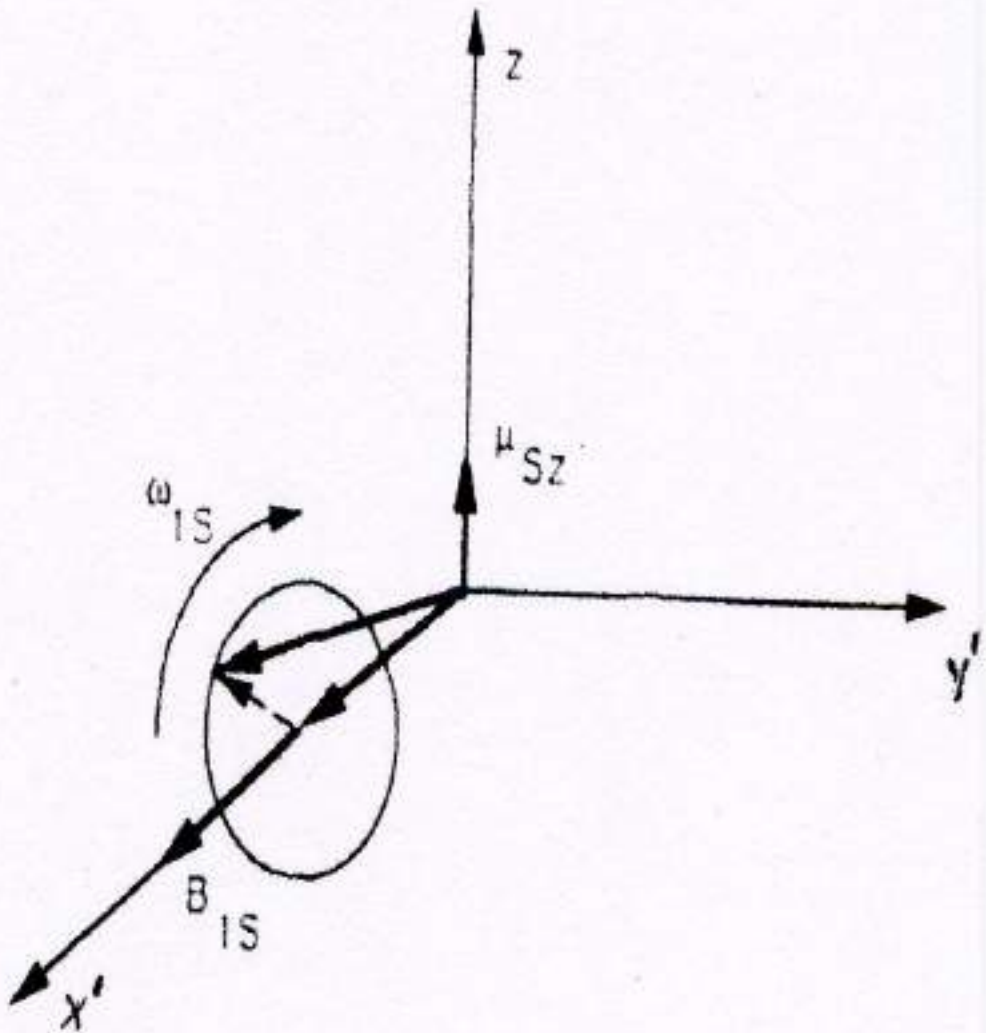
After a $\pi/2$ pulse along x' at frequency ω_{0I} the abundant spin magnetization M_I lies along y' .



Immediately after a second $\pi/2$ pulse along y' the I spins rotate around y' . The resultant magnetization M_I is "spin-locked" on the axis.

Due to another rf field $B_{1,s}$ along X' , individual magnetic moment μ_s turns around X' with a frequency

$$\omega_{1,s} = \gamma_s B_{1,s}$$



Hartmann-Hahn condition

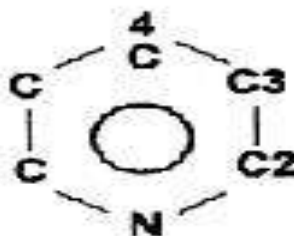
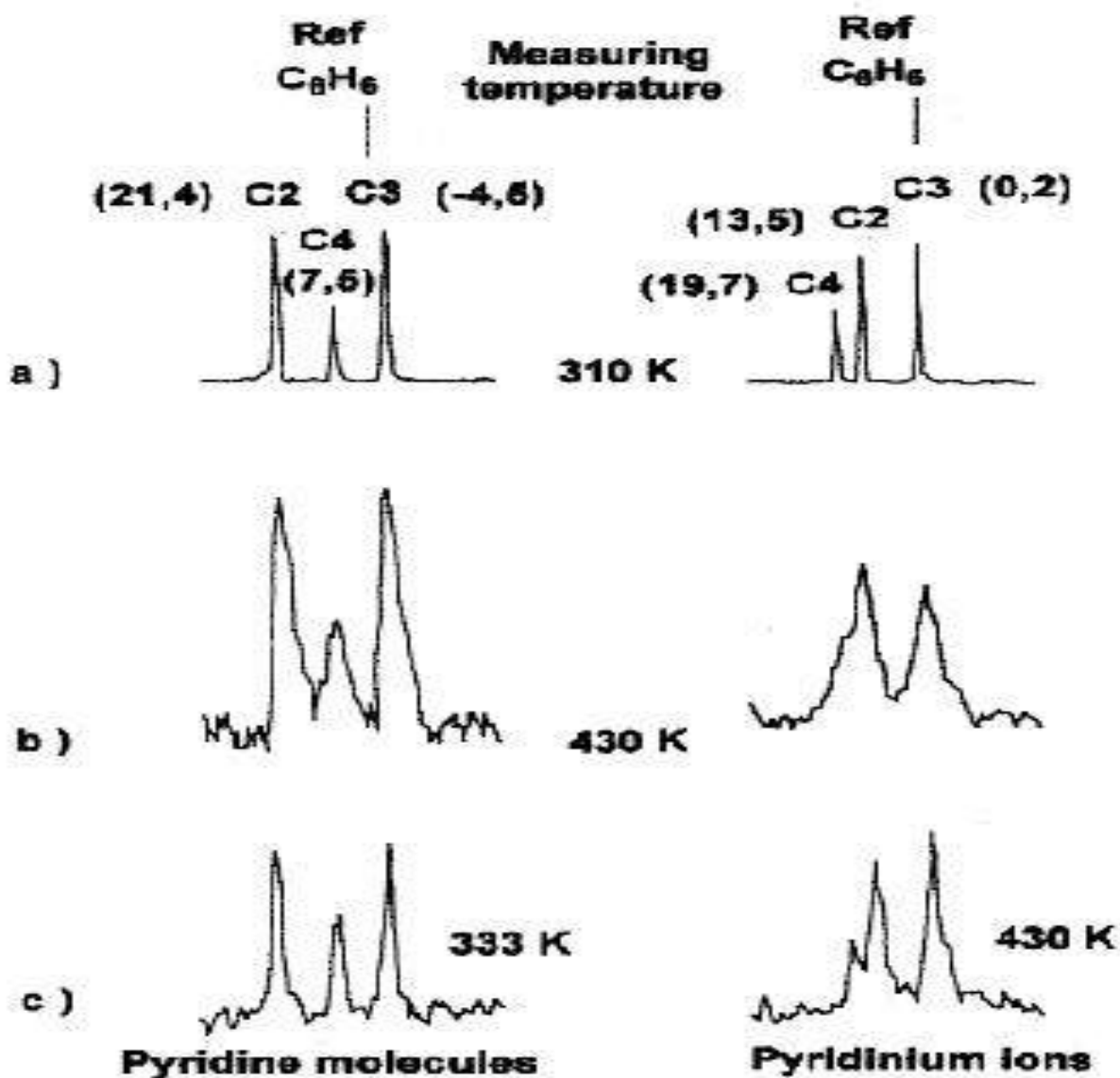
I and S have the oscillating components which may have the same time dependence if

$$\omega_{1I} = \omega_{1S}$$
$$\gamma_S B_{1S} = \gamma_I B_{1I}$$

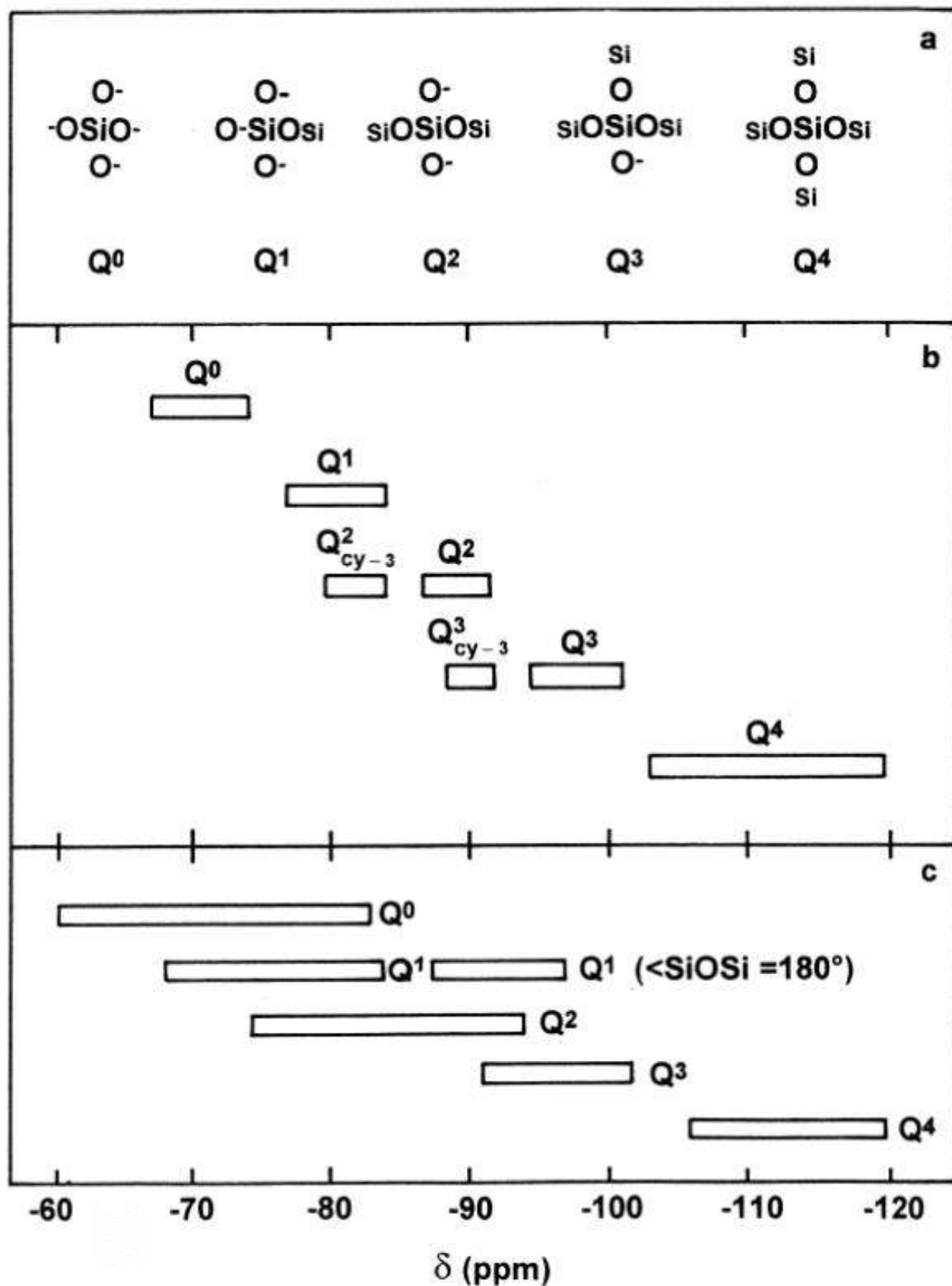
^{13}C NMR of Pyridine

a: liquid (left) and in H_2SO_4 (right)

b and c: adsorbed on NaY (left) and HY (right)

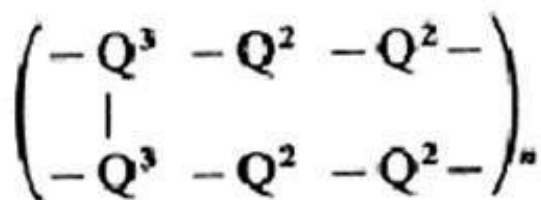
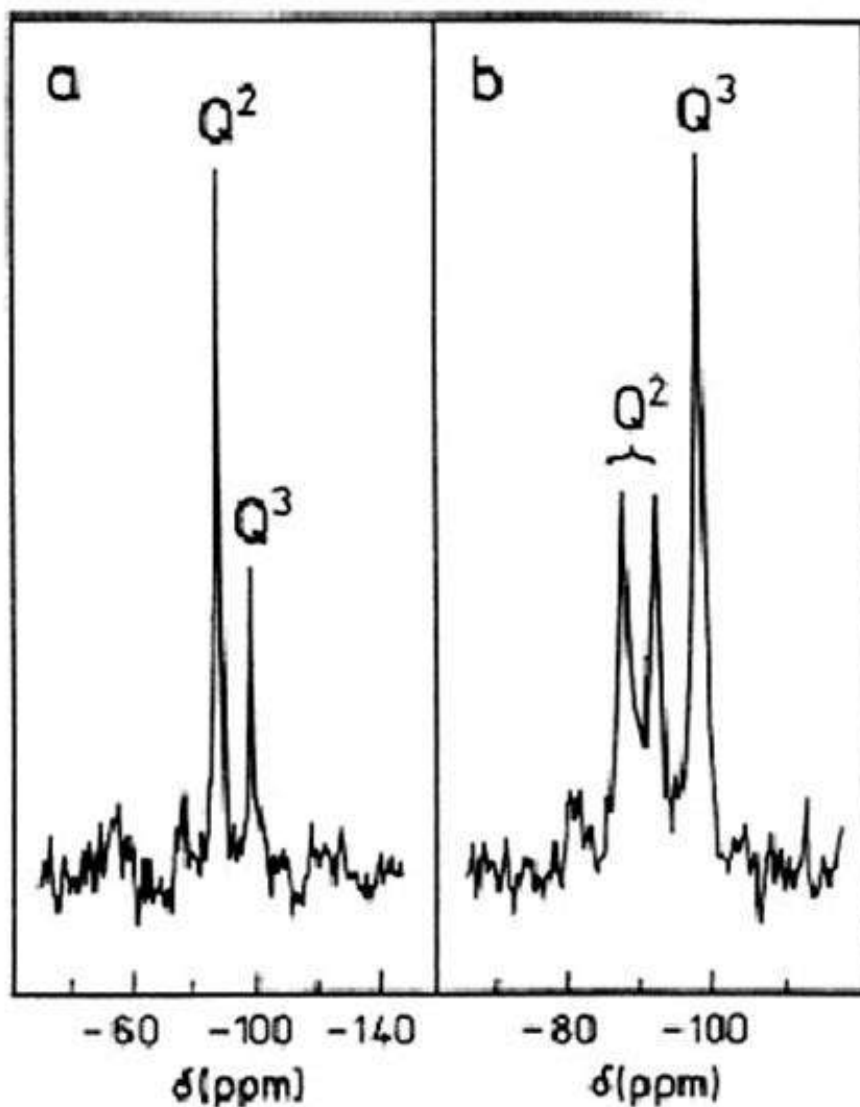


$\delta(^{29}\text{Si})$ for silicates Q_n

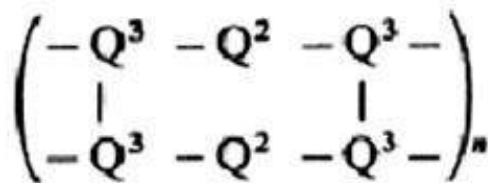


δ (Si)

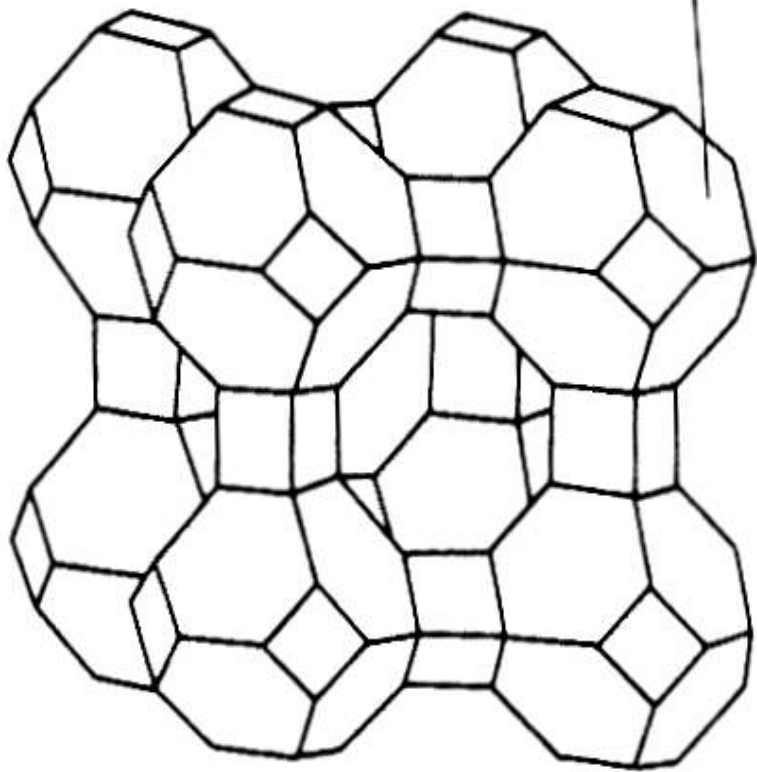
Xonolite Tremolite



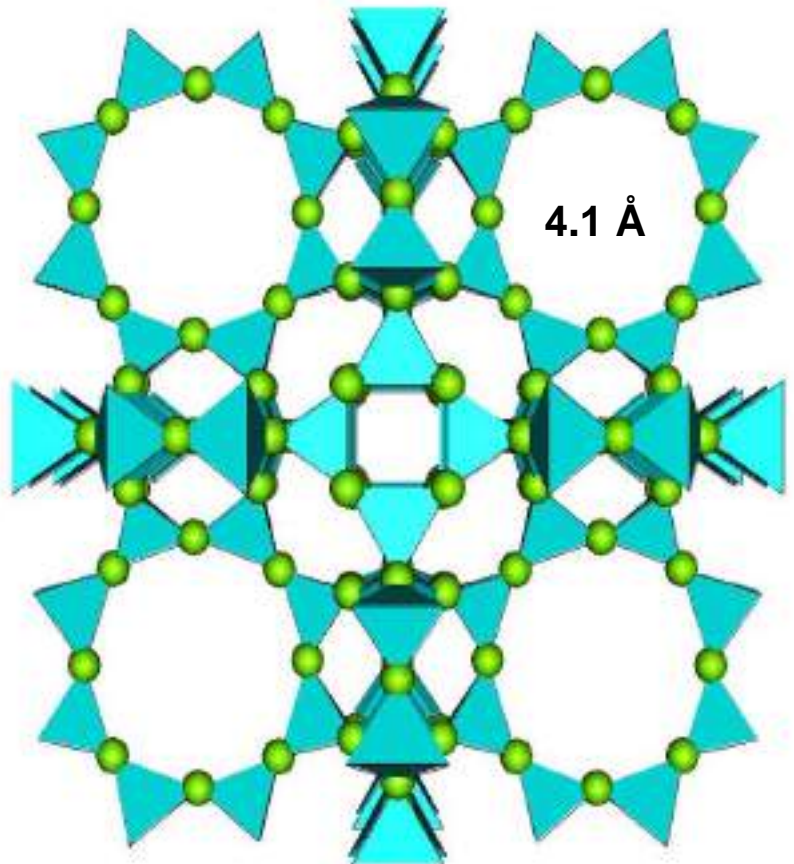
Xonolite $Ca_6Si_6O_{17}(OH)_2$

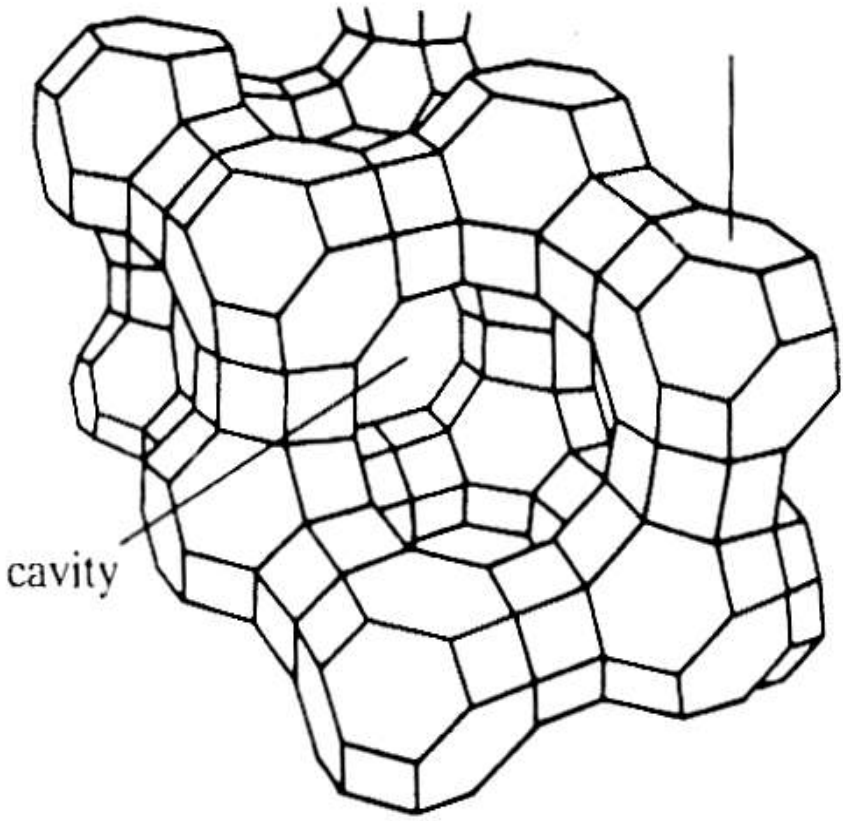


tremolite $Ca_2Mg_5(Si_4O_{11})_2(OH)_2$

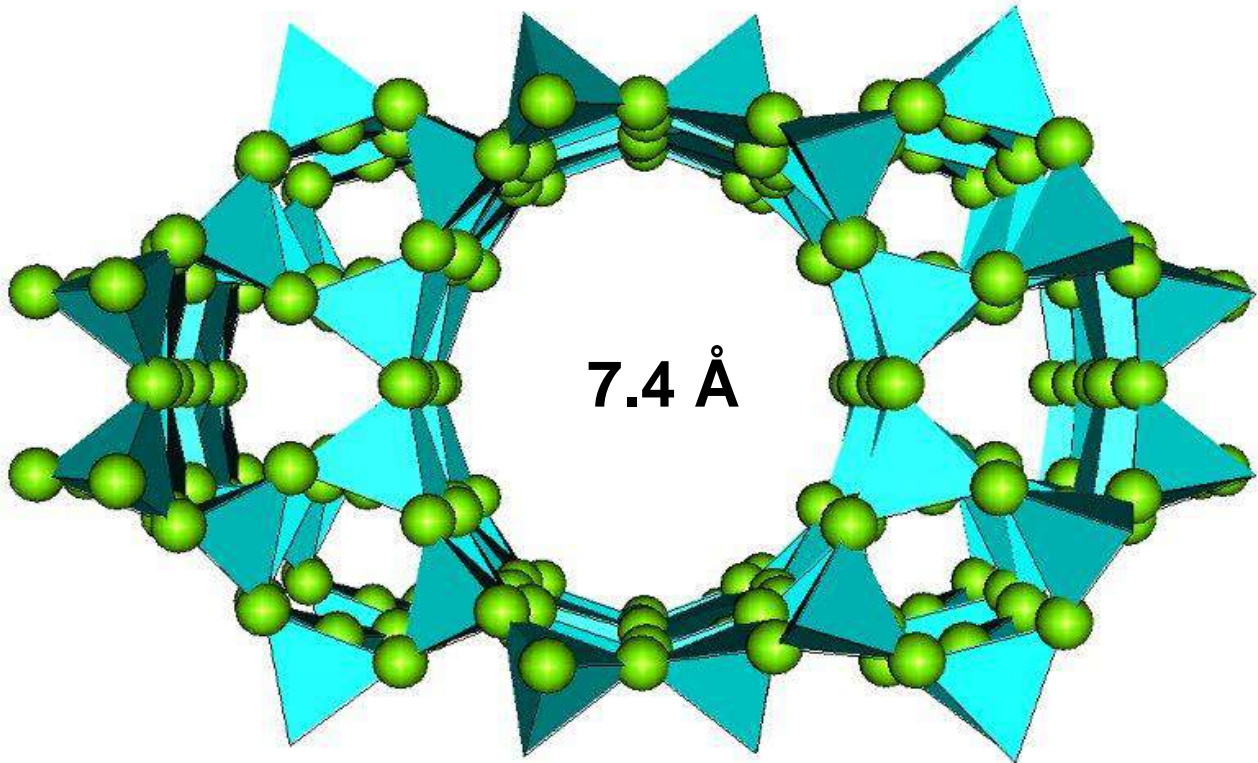


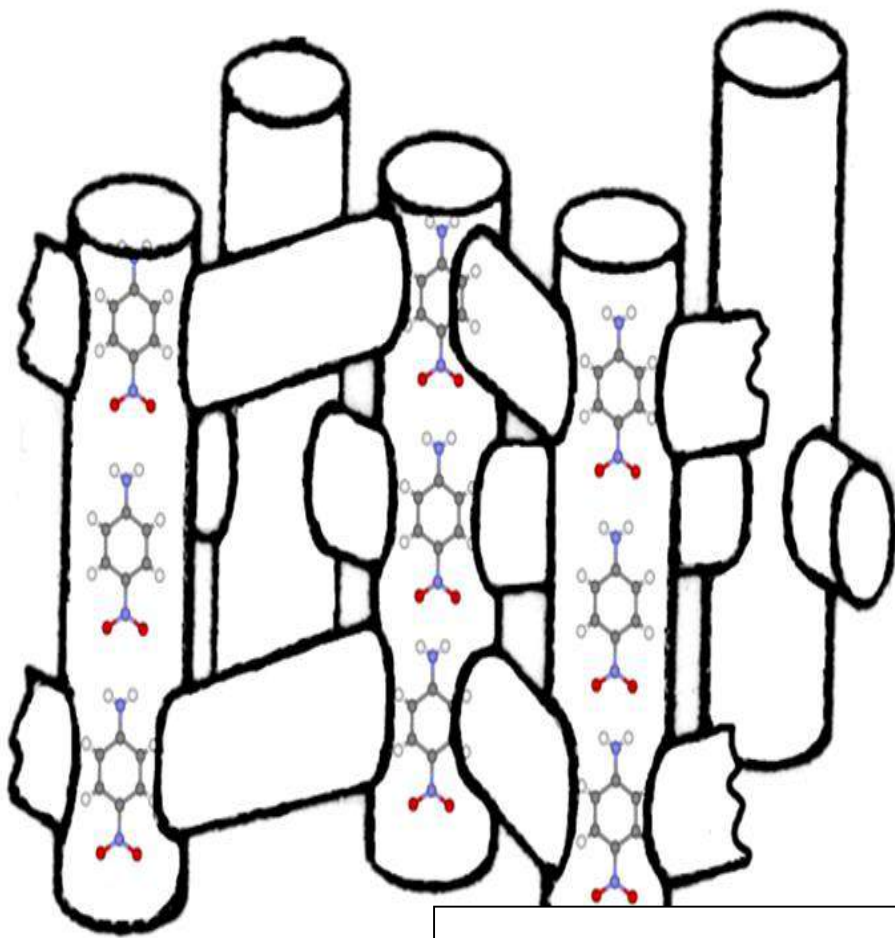
Zeolite A



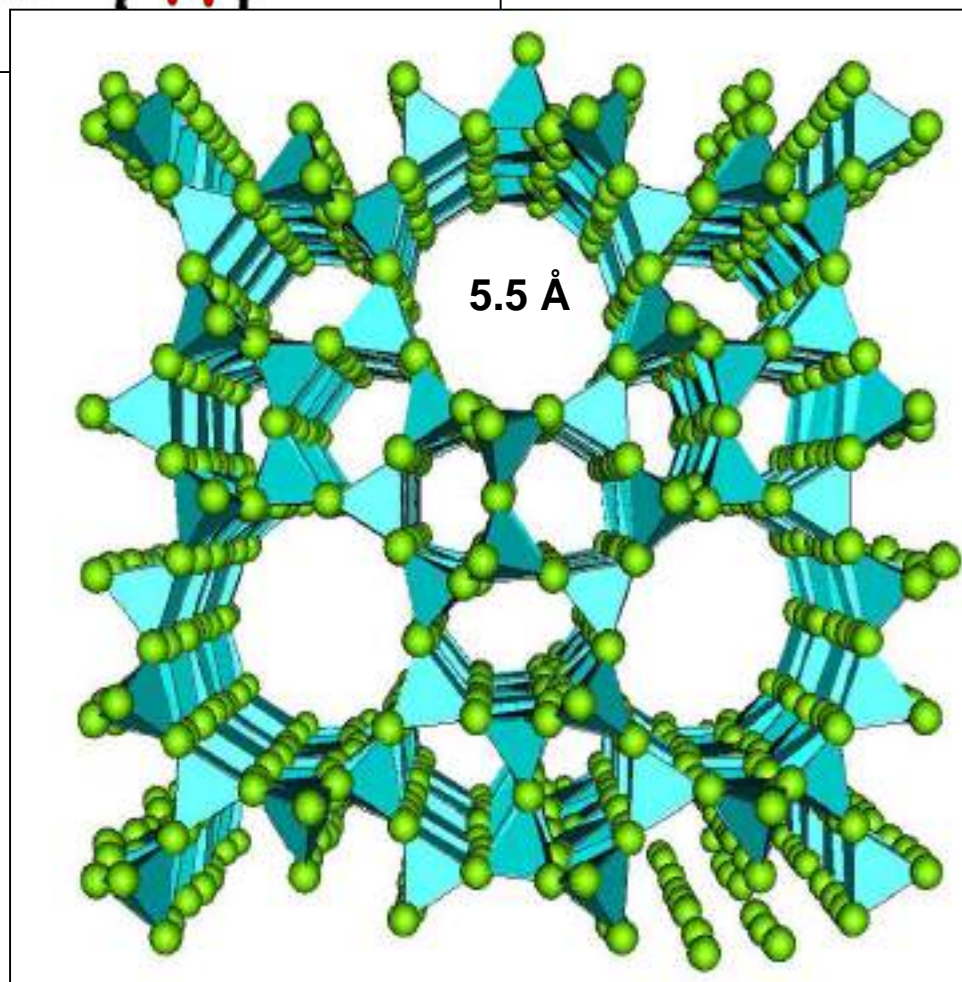


Zeolite Y
(Faujasite)





Zeolite ZSM-5



$\delta(^{29}\text{Si})$ in units $Q_4(n \text{ Al})$



-80

-90

-100

-110

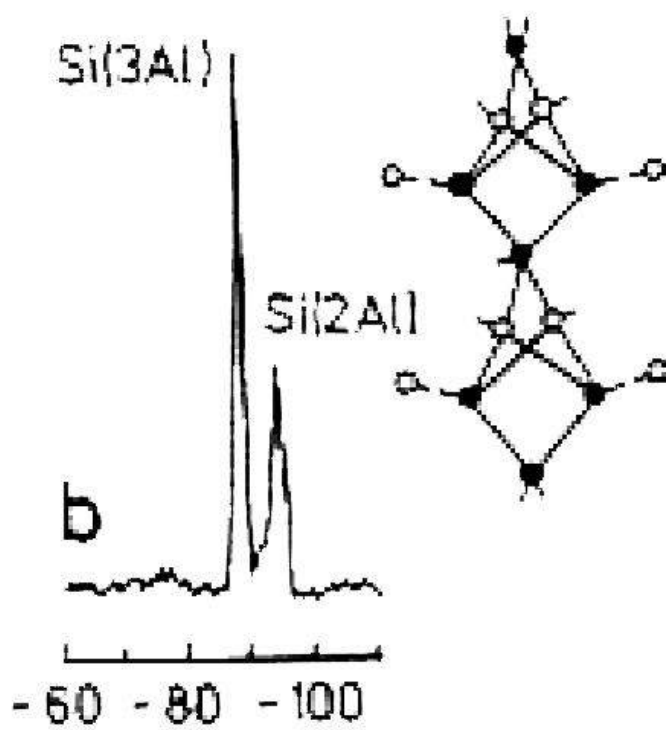
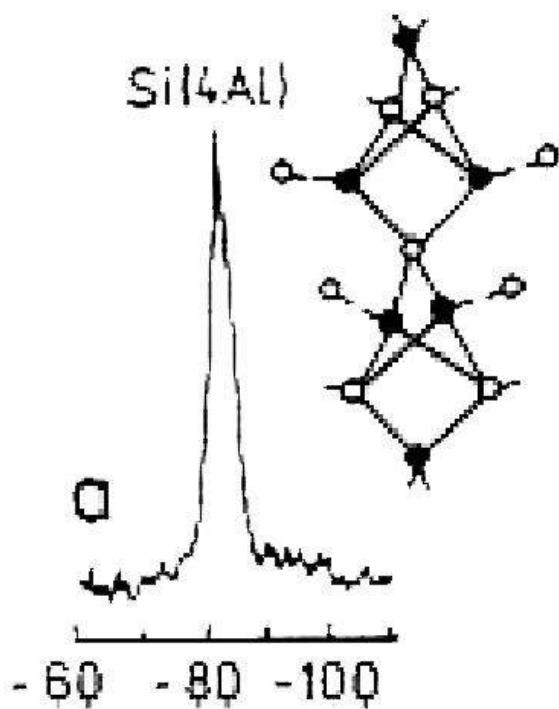
-120

$\delta(\text{ppm})$

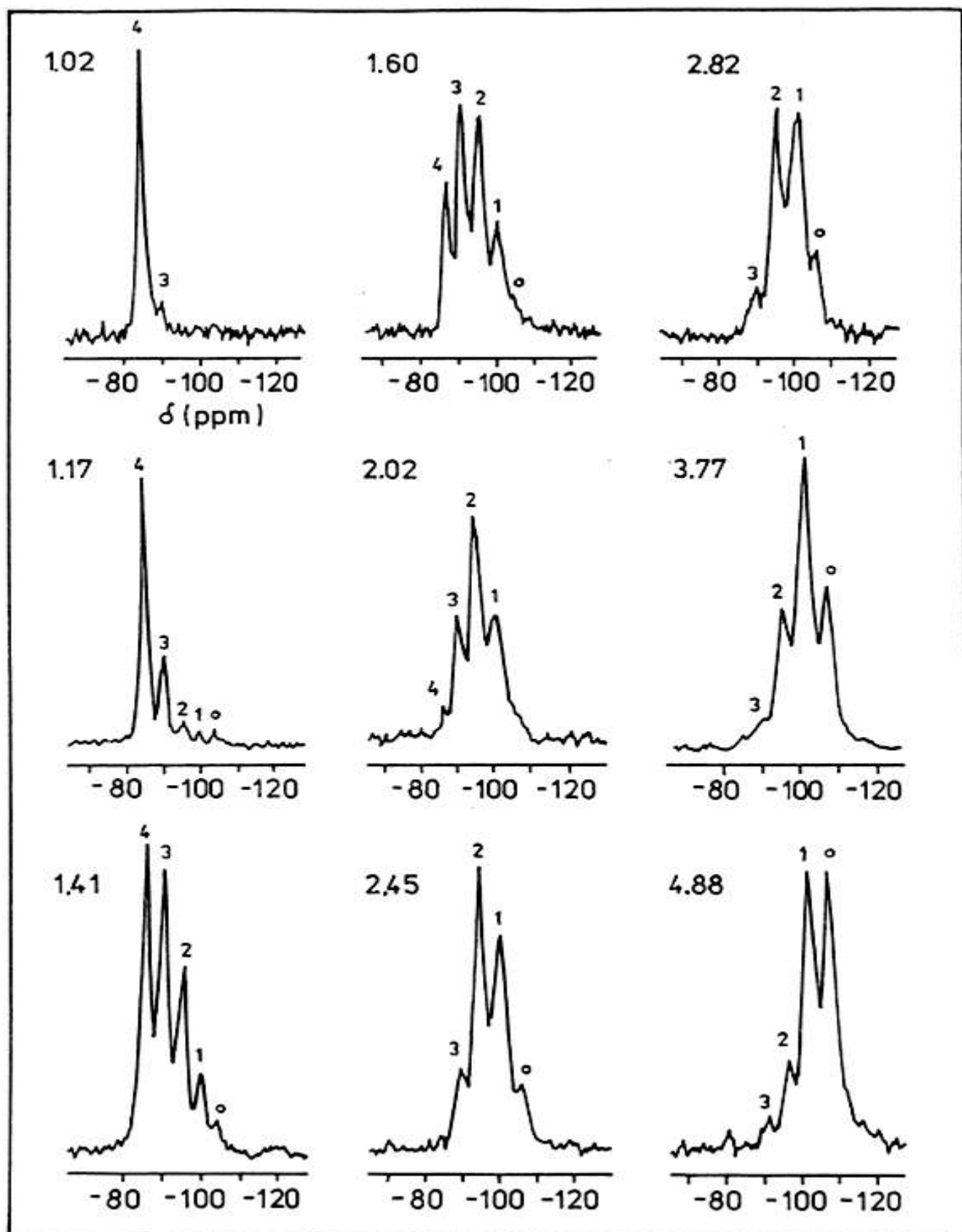
Thomsonite

Natrolite

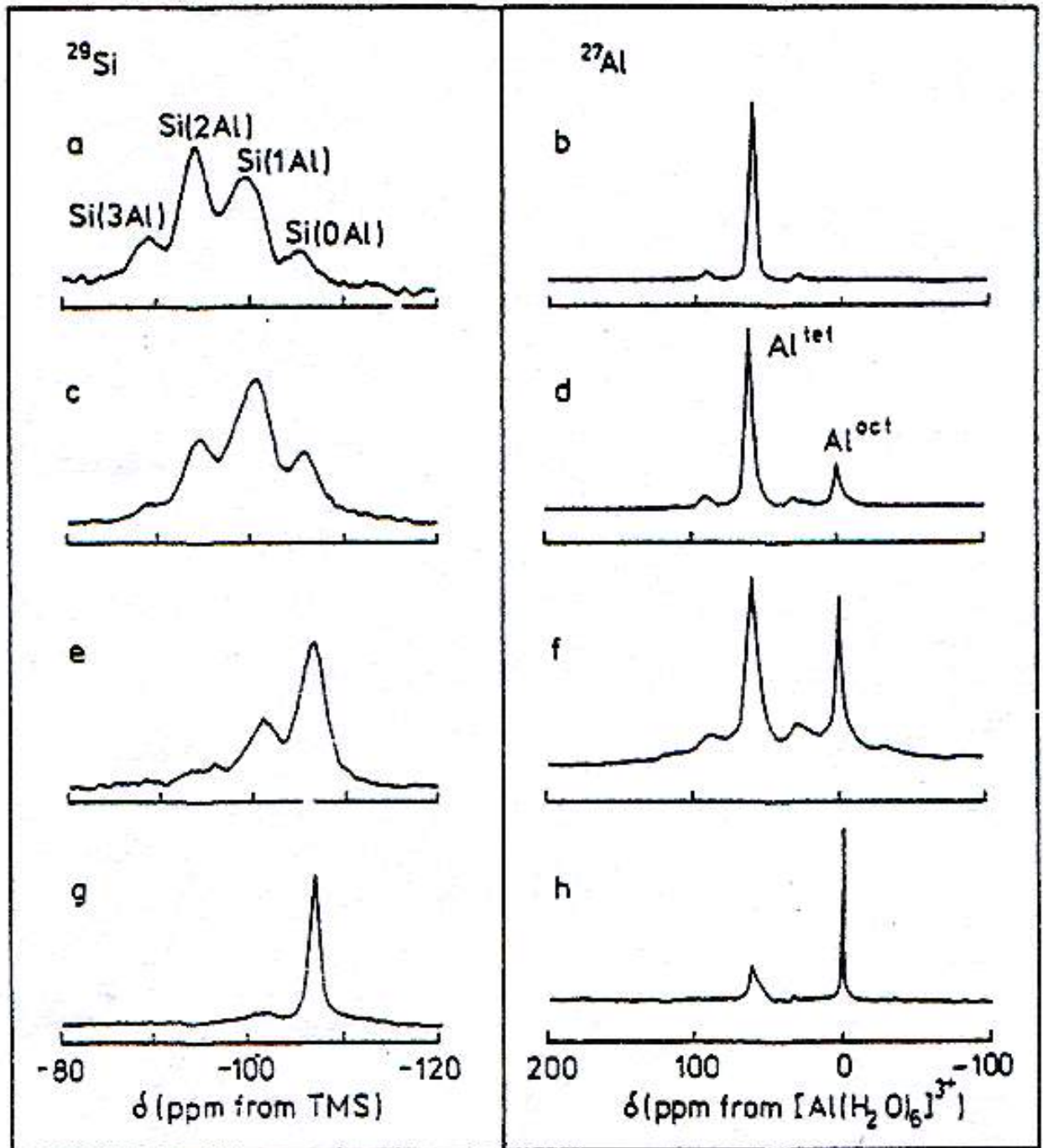
● Si ○ Al



Variation of ^{29}Si -NMR with Si/Al ratio of faujasite

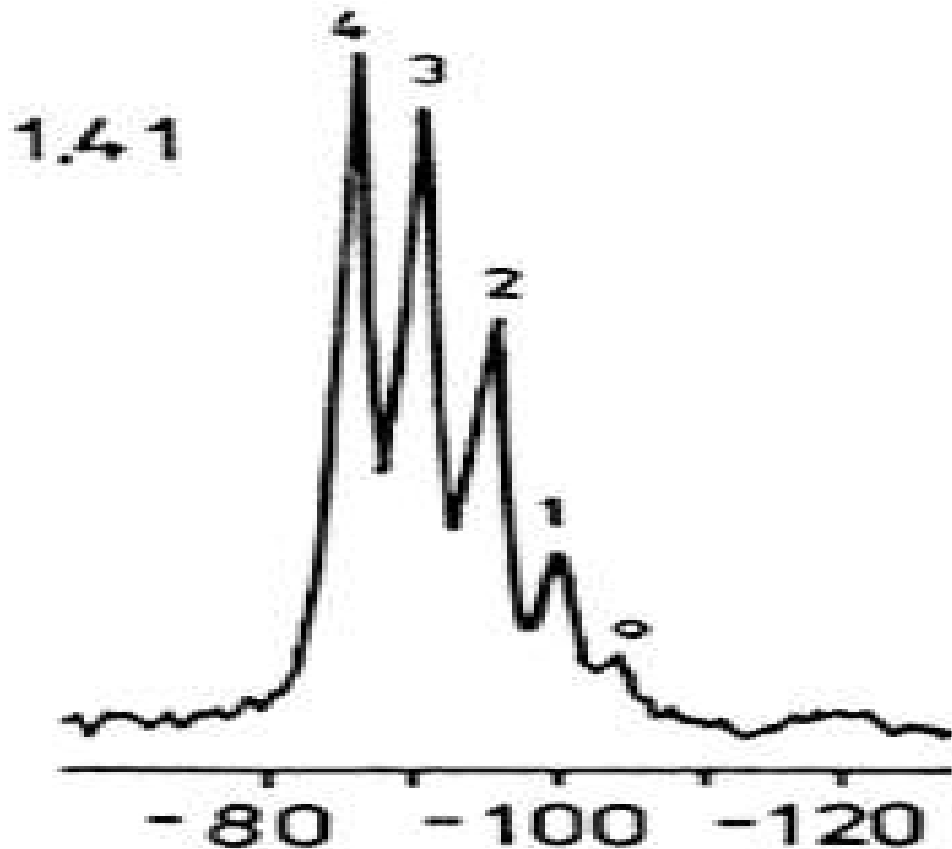


Dealumination of Y zeolite

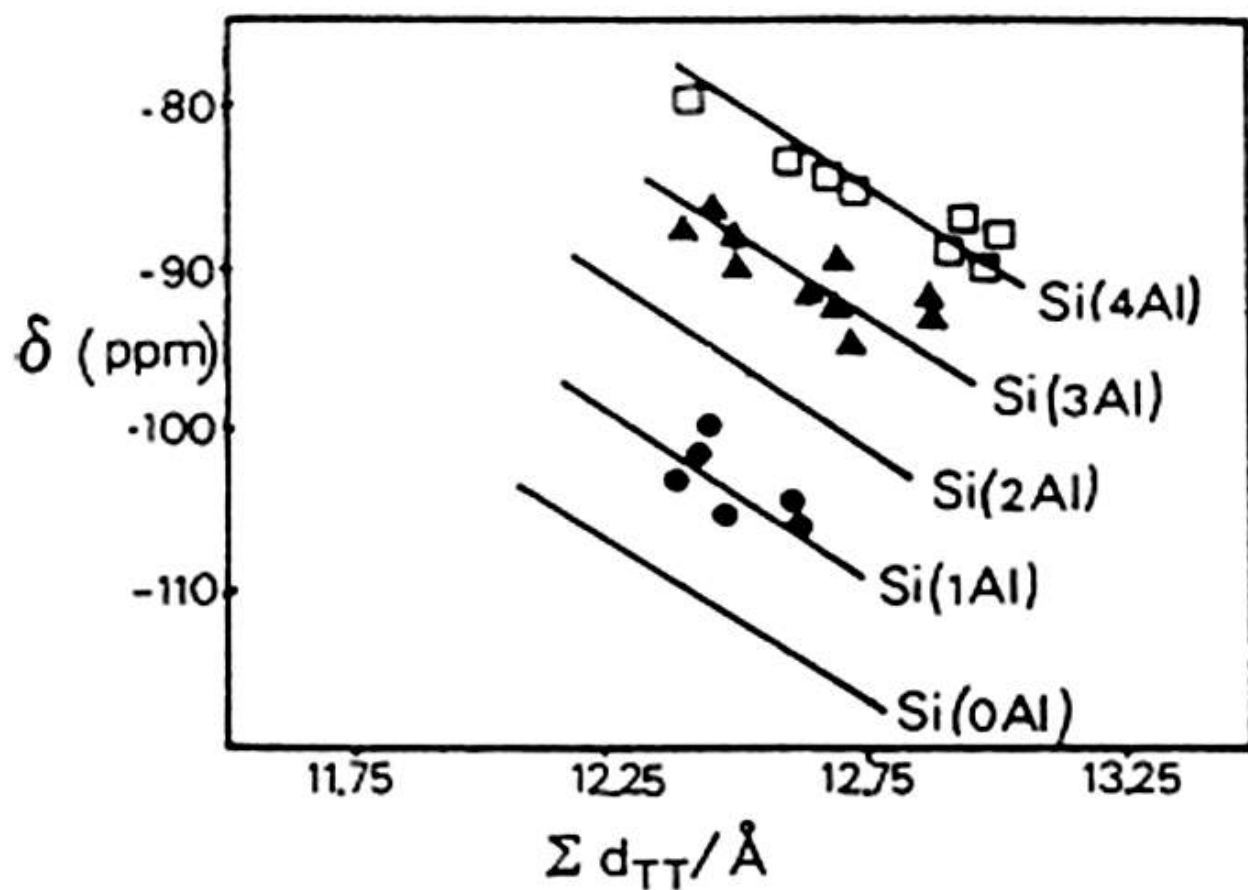


Determination of the ratio Si/Al

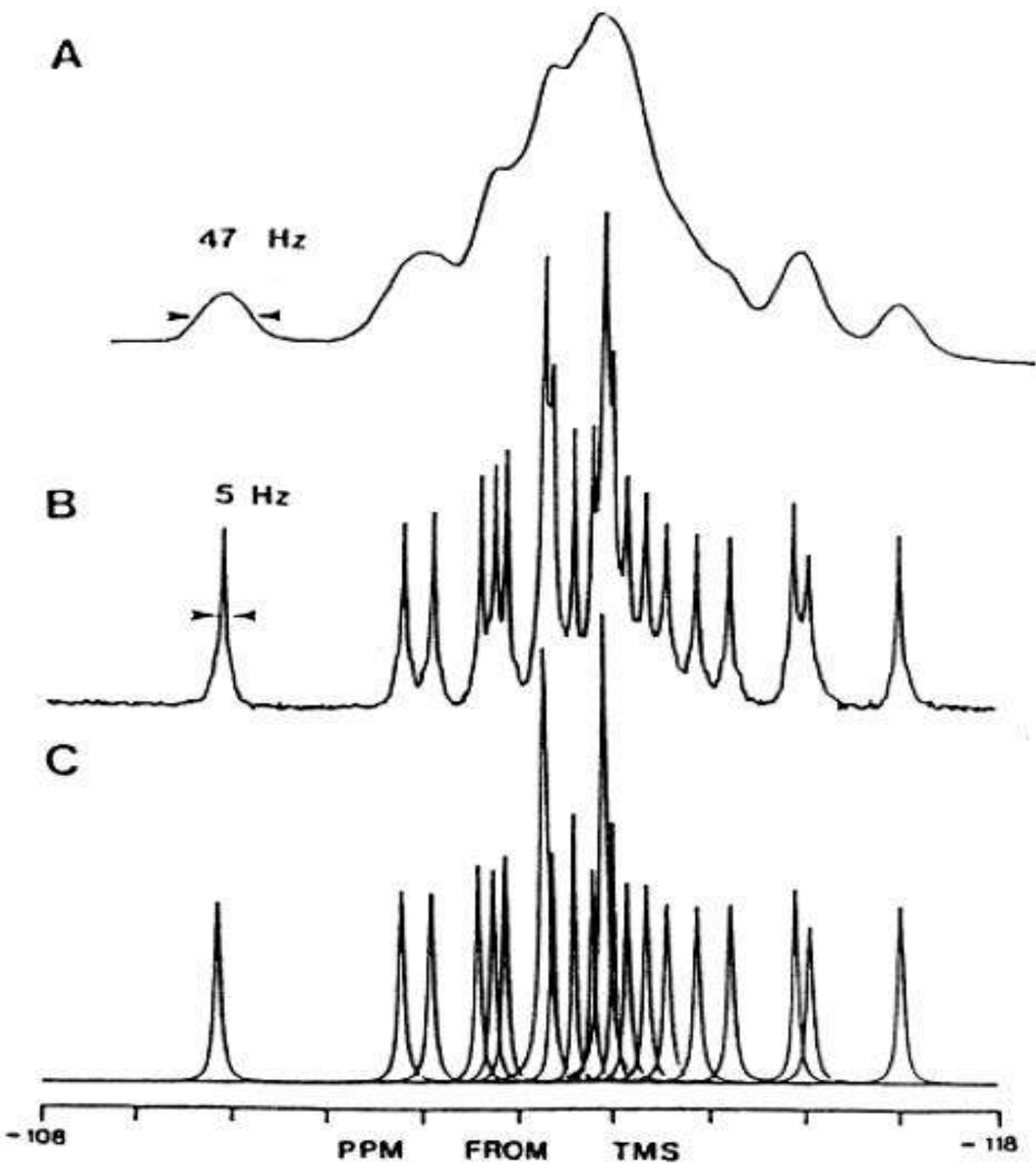
$$Si / Al = \sum_{n=0}^4 I_{Si(nAl)} / \sum_{n=0}^4 \frac{n}{4} I_{Si(nAl)}$$



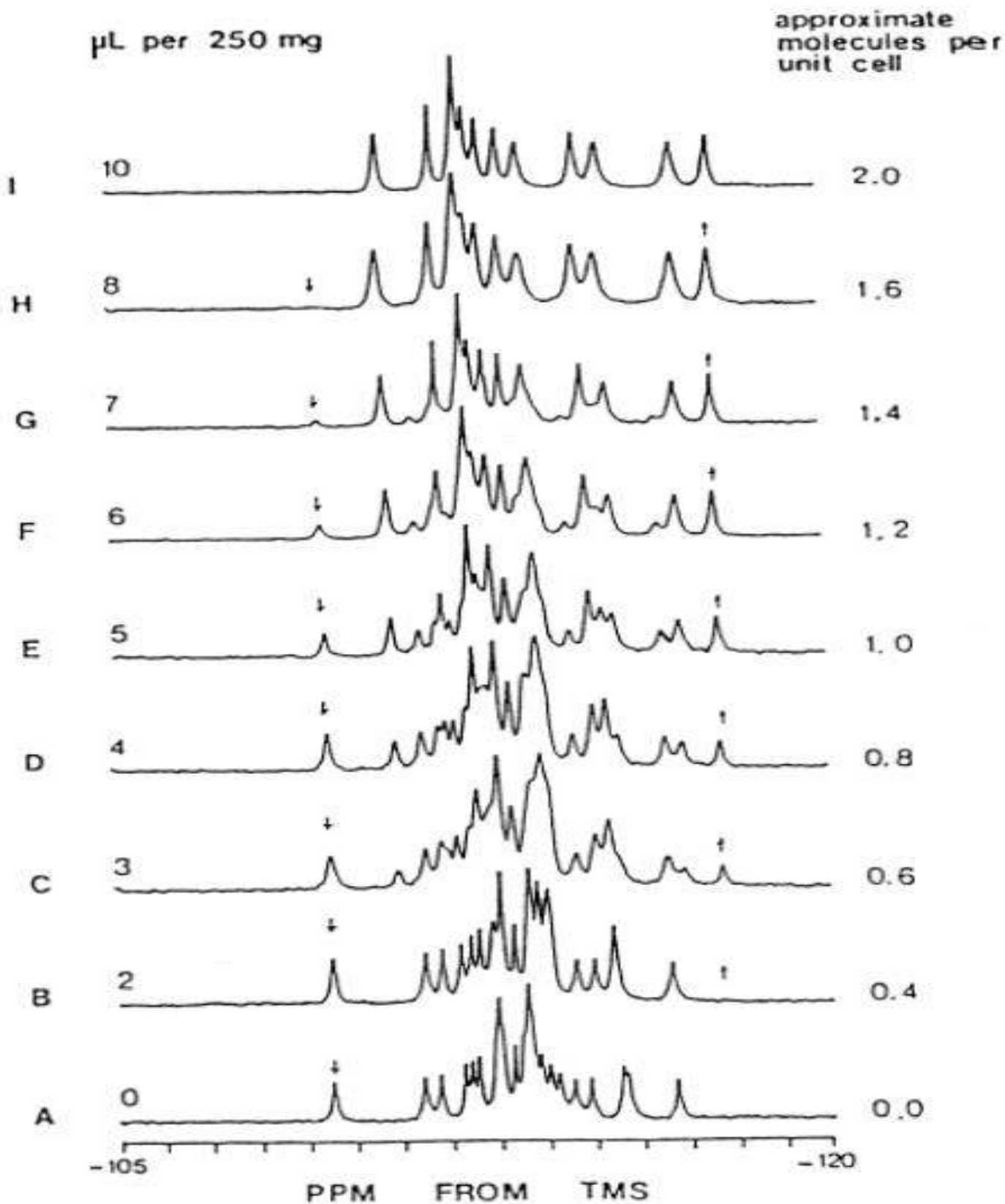
Variation of $\delta(^{29}\text{Si})$ against distance TT



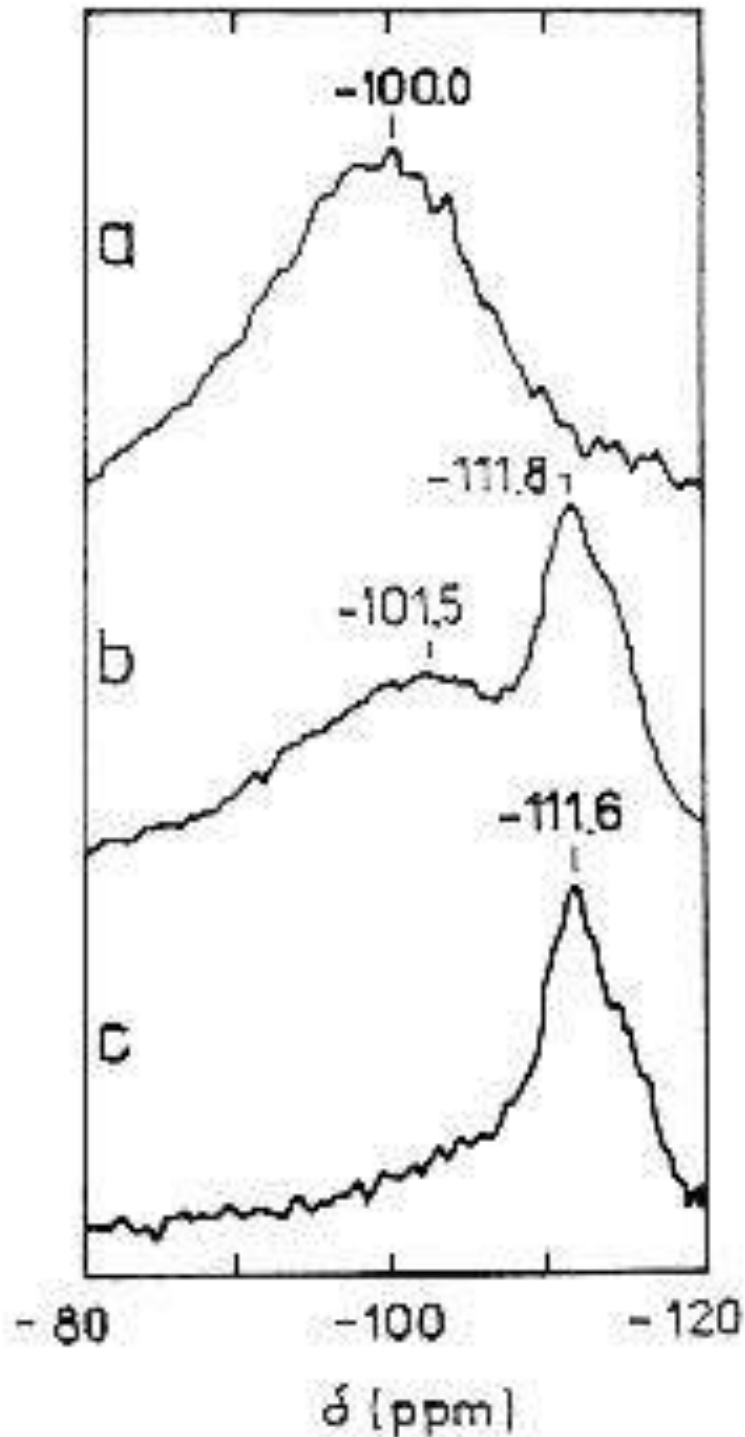
ZSM5. A: static; B: MAS; C: simulation



^{29}Si -MAS-NMR of silicalite. Influence of p-xylene concentration. Transformation of monoclinic into orthorhombic symmetry

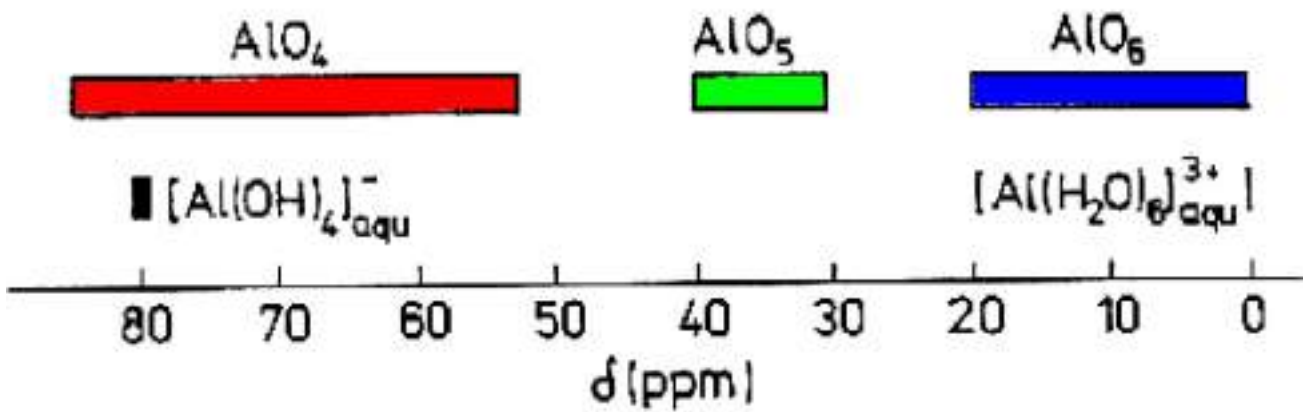


$\delta(^{29}\text{Si})$ during the synthesis of ZSM5
crystallinity: a) 0% Si/Al=1.8
b) 45% Si/Al=5; c) 100%



$\delta(^{27}\text{Al})$ of AlO_n

reference $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$



Variation of $\delta^{27}\text{Al}$ versus Al-O-Si angle

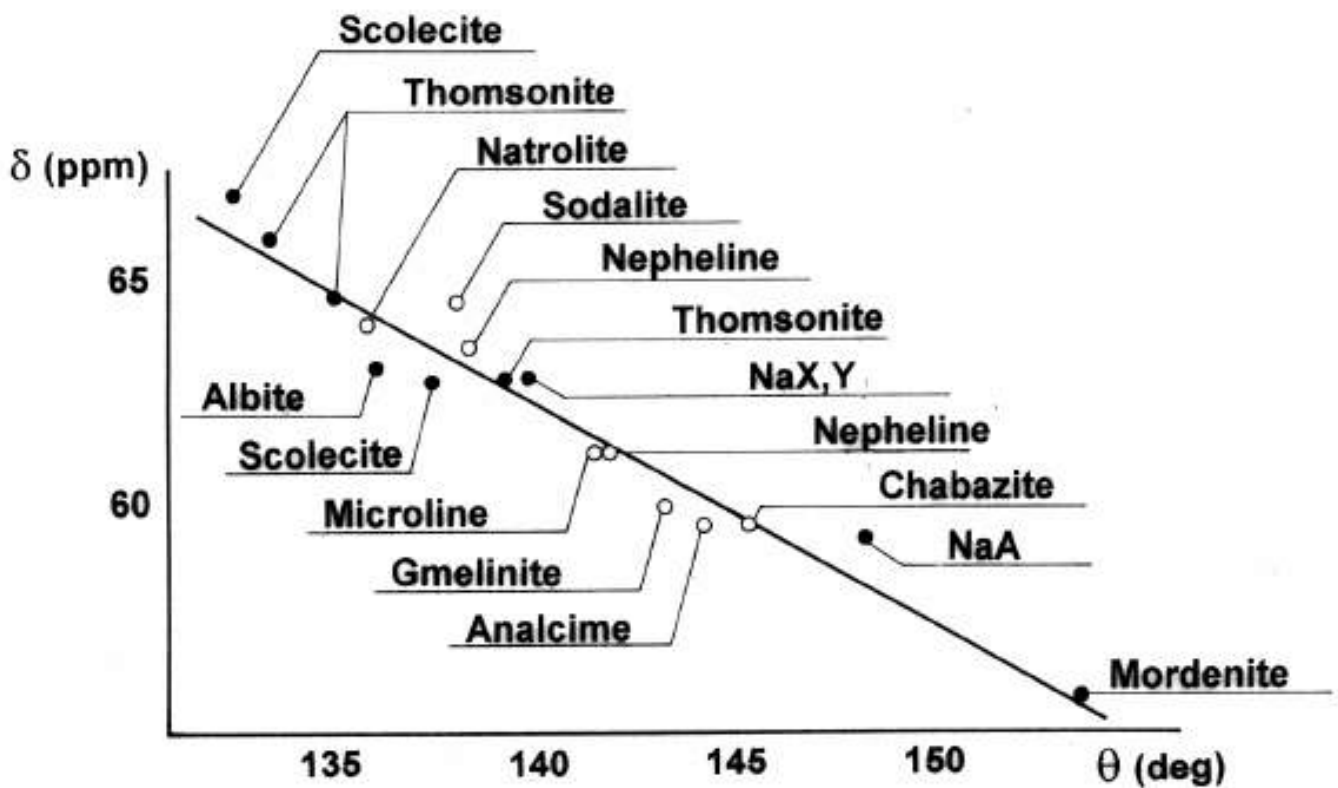
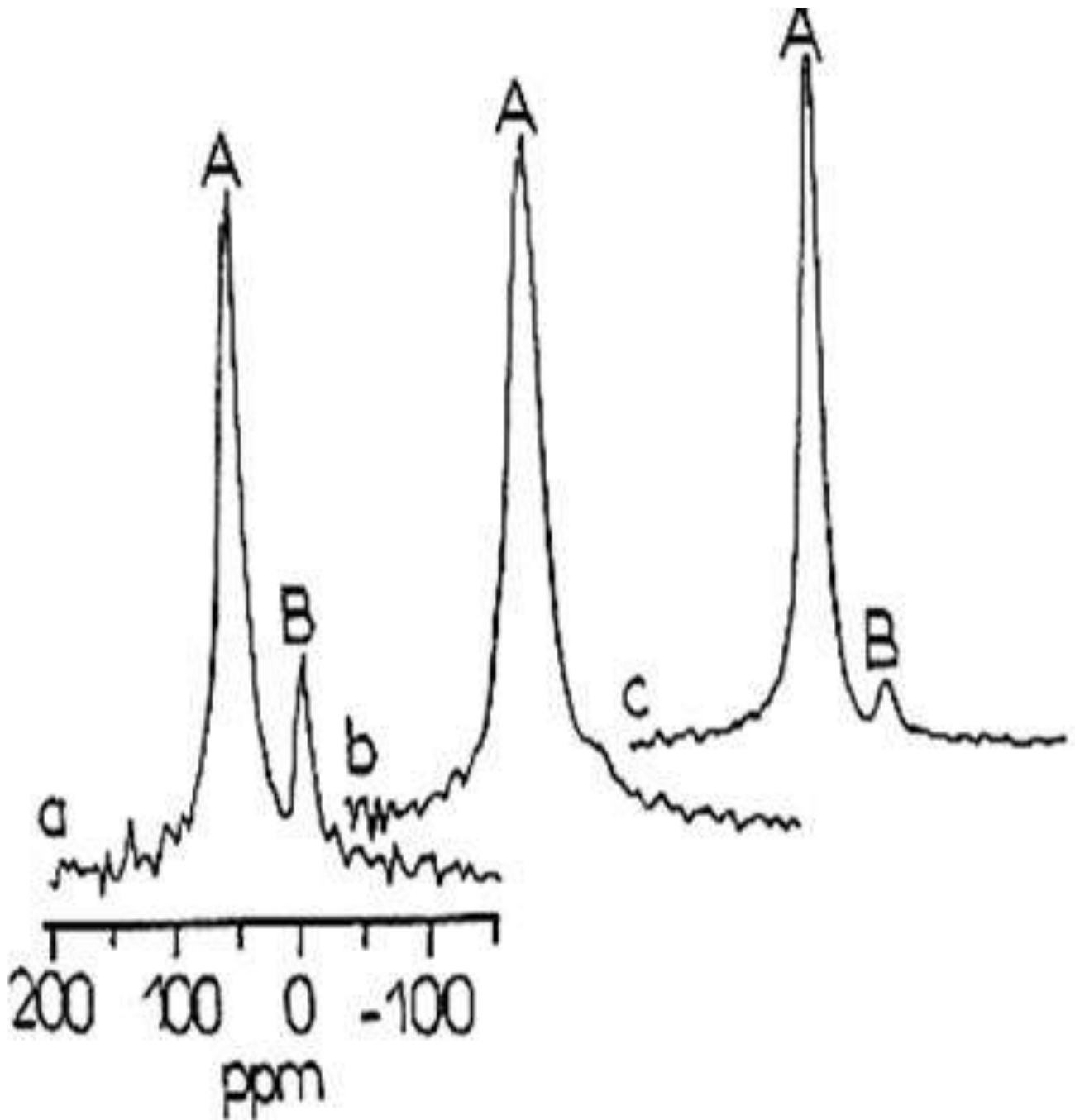


FIG. 3.36 – Variation de $\delta(^{27}\text{Al})$ avec l'angle Al-O-Si.

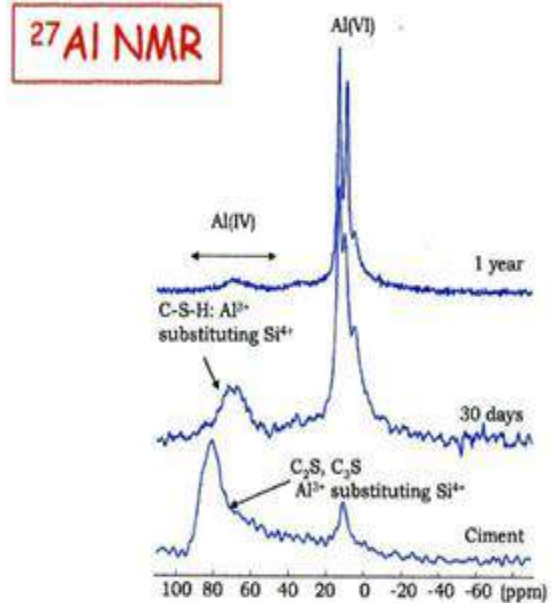
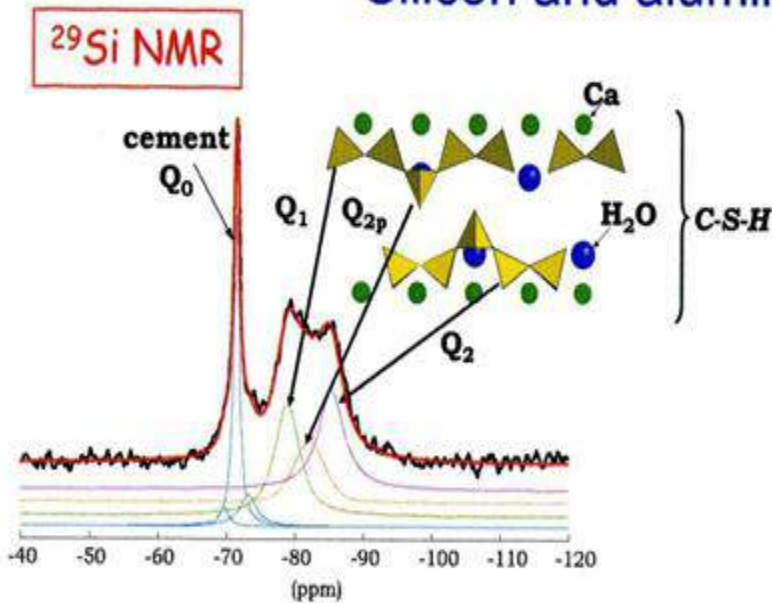
^{27}Al NMR of HZSM5

- a) before cooking;
- b) 10% coke;
- c) after partial regeneration



NMR spectroscopy in cement science

Silicon and aluminum coordination



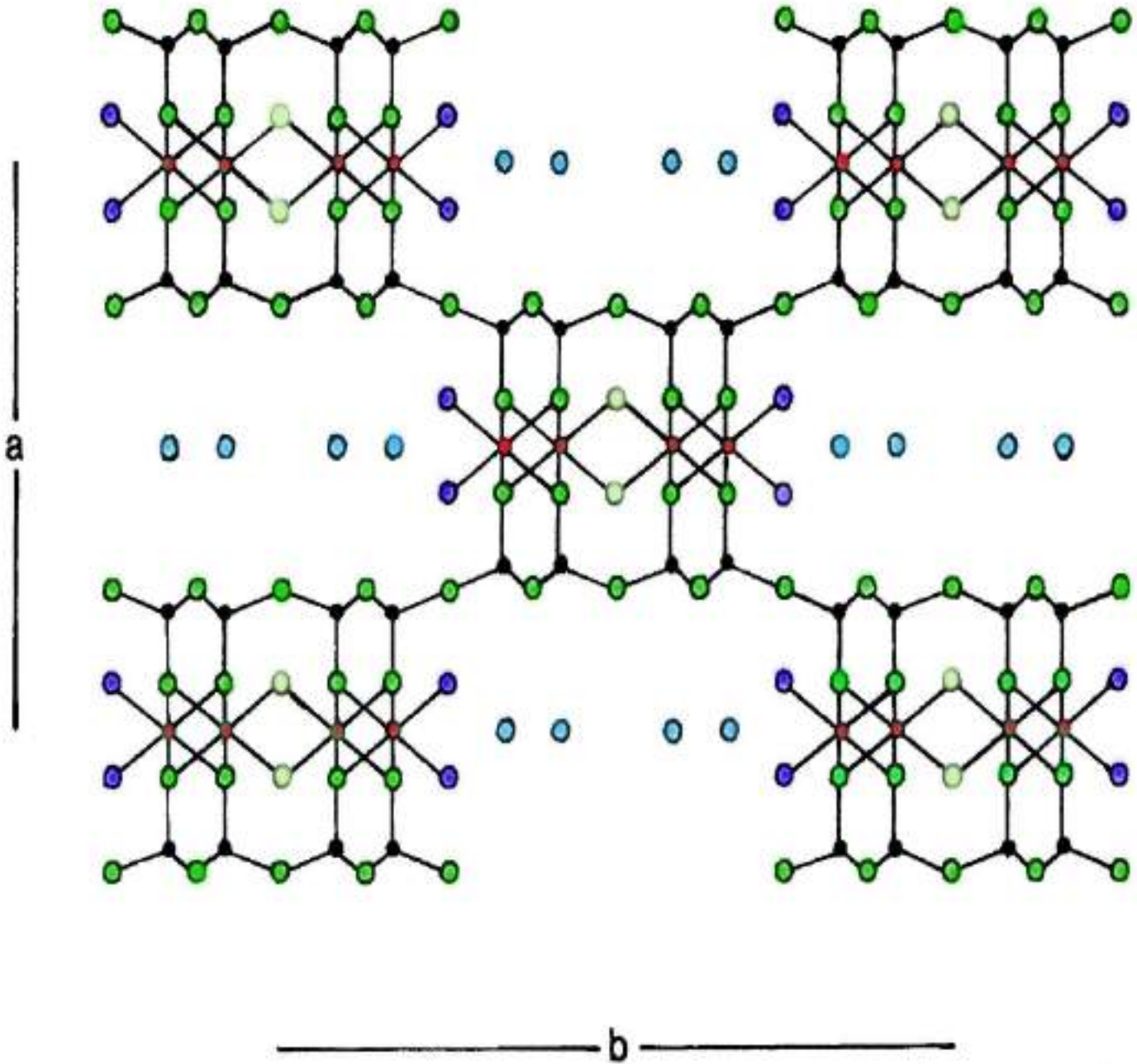
- Solid-state NMR spectroscopy is extensively utilized (^{29}Si , ^{27}Al , ^1H):
 - « Application of NMR spectroscopy to cement science » Gordon and Breach, 1994
 - « NMR spectroscopy of cement based materials » Springer 1998

- $\text{CaO} \cdot \text{SiO}_2 \cdot \text{Al}_2\text{O}_3 \cdot \text{Fe}_2\text{O}_3 \cdot \text{SO}_3 \cdot \text{Na}_2\text{O} \cdot \text{MgO} \cdot \text{CO}_2 \cdot \text{H}_2\text{O}$
- ^{43}Ca , ^{25}Mg , ^{33}S

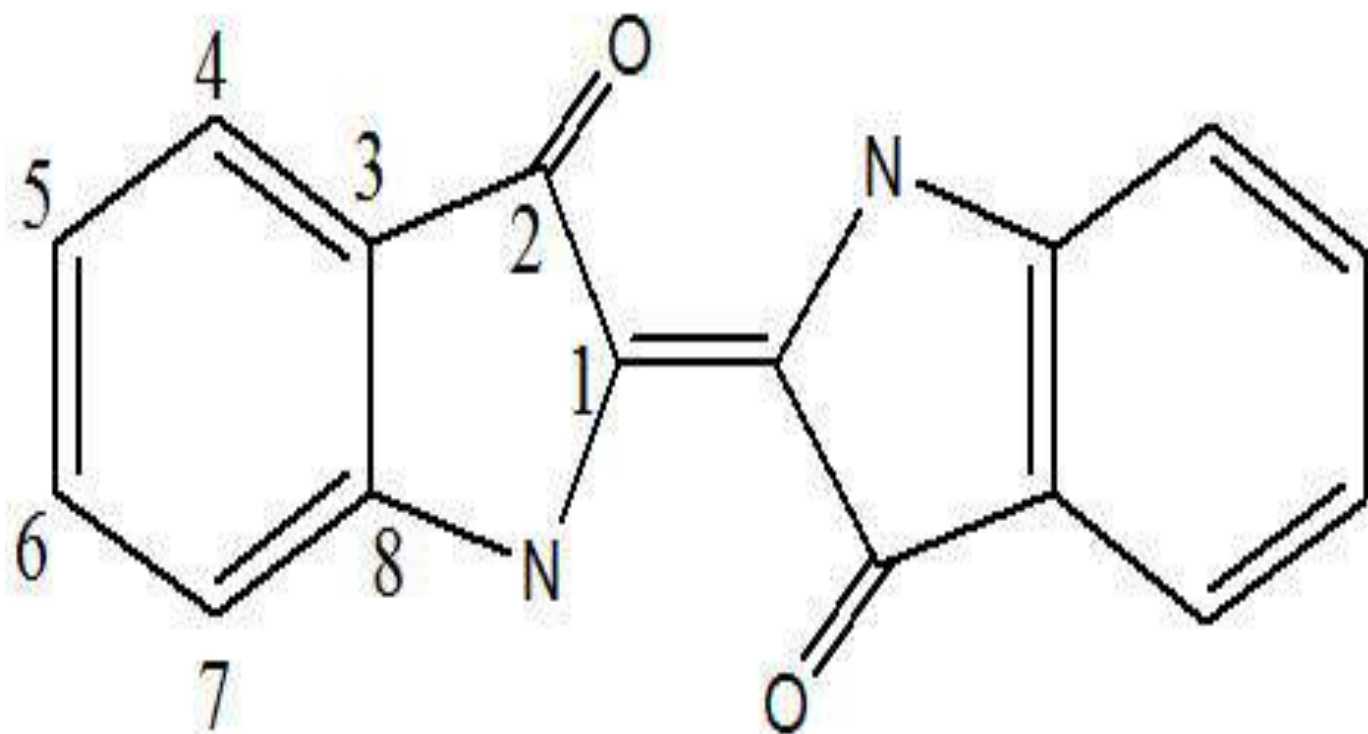
MAYA Blue: Palygorskyte clay + indigo



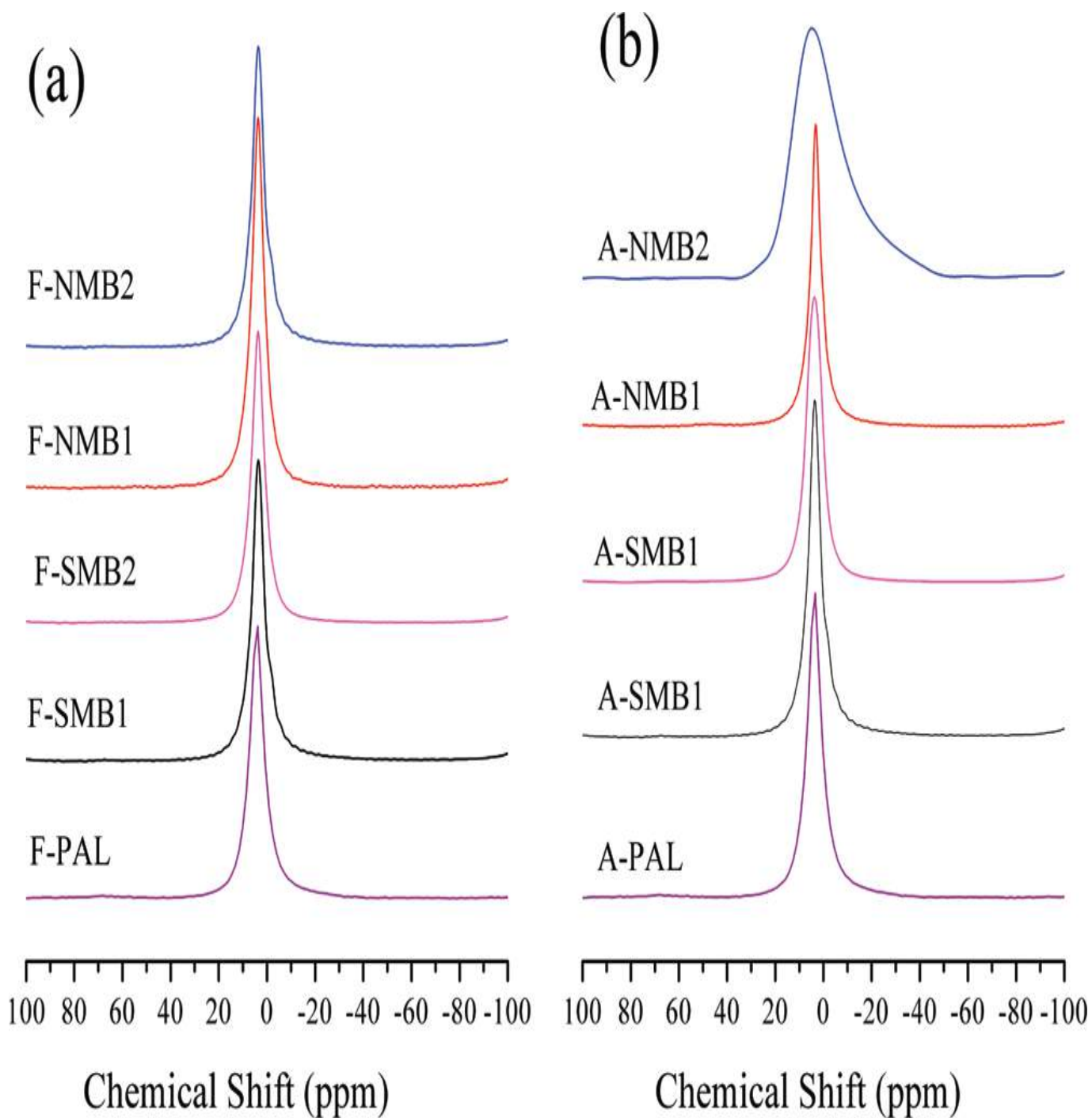
Palygorskite clay



Indigo

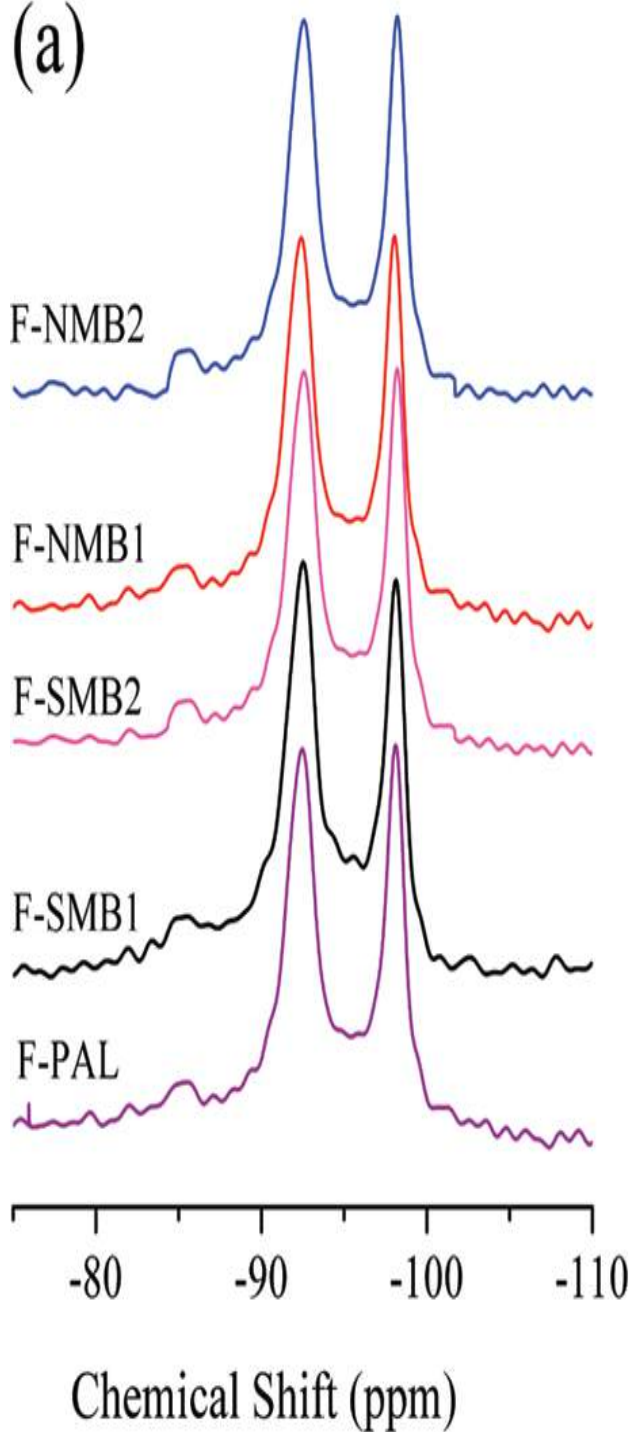


27Al MAS NMR spectra of fresh (a) and aged (b)
Maya
Blue-like pigments.

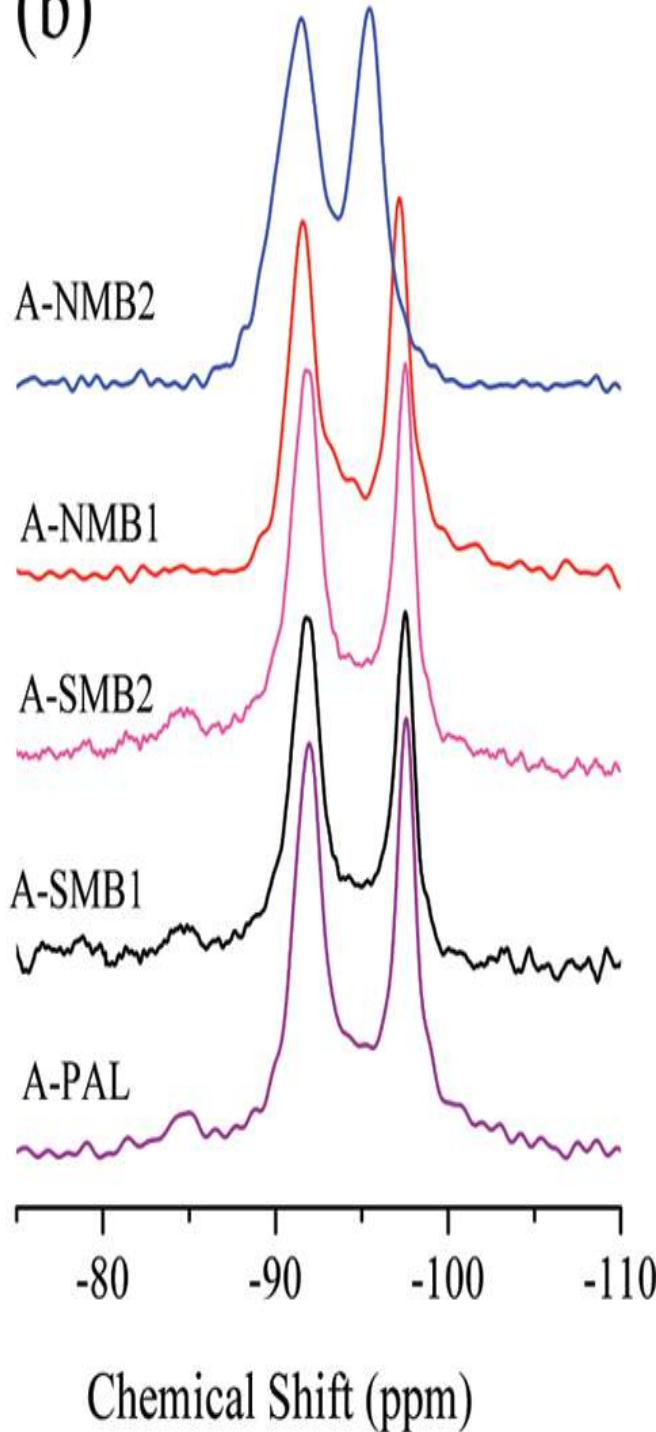


29Si MAS NMR spectra of fresh (a) and aged (b)
Maya Bluelike pigments.

(a)



(b)



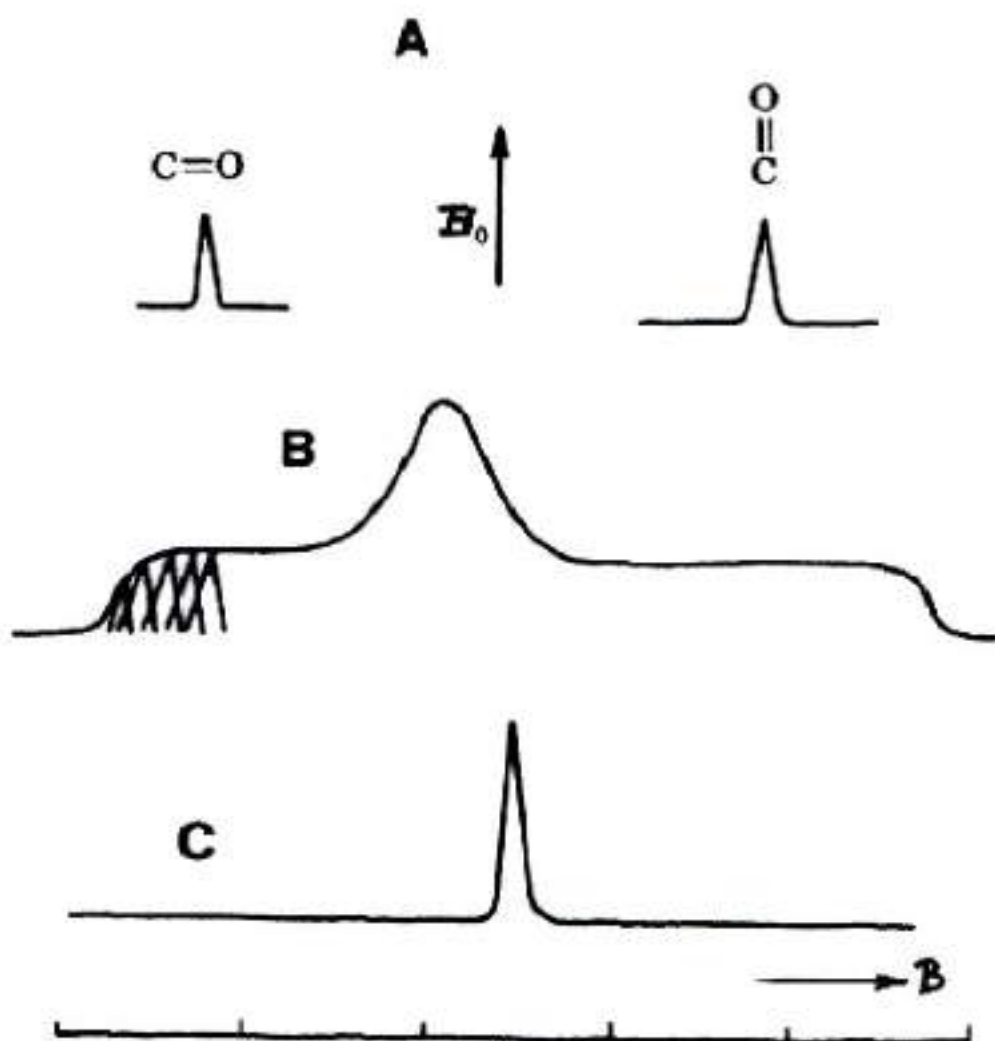
Chemical shift anisotropy

Schematic representation of the ^{13}C NMR absorption of a carbonyl functionality

A- single crystal in two different orientations/ B_0

B- In a polycrystalline sample where there are contributions from the random distribution of orientations.

C- In solution



Chemical shift anisotropy

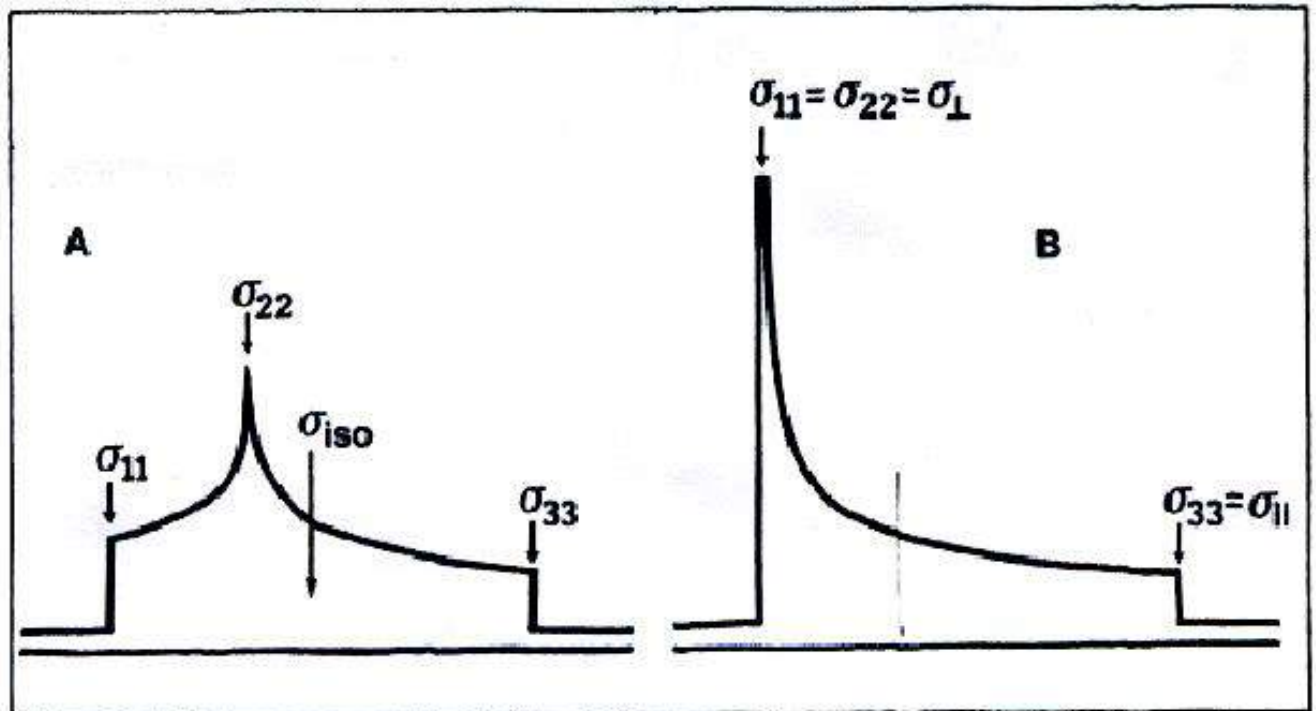
MAS removes all solid-state interactions.
Multi-pulse sequence does not remove the
chemical shift anisotropy.

Asymmetric shift anisotropy

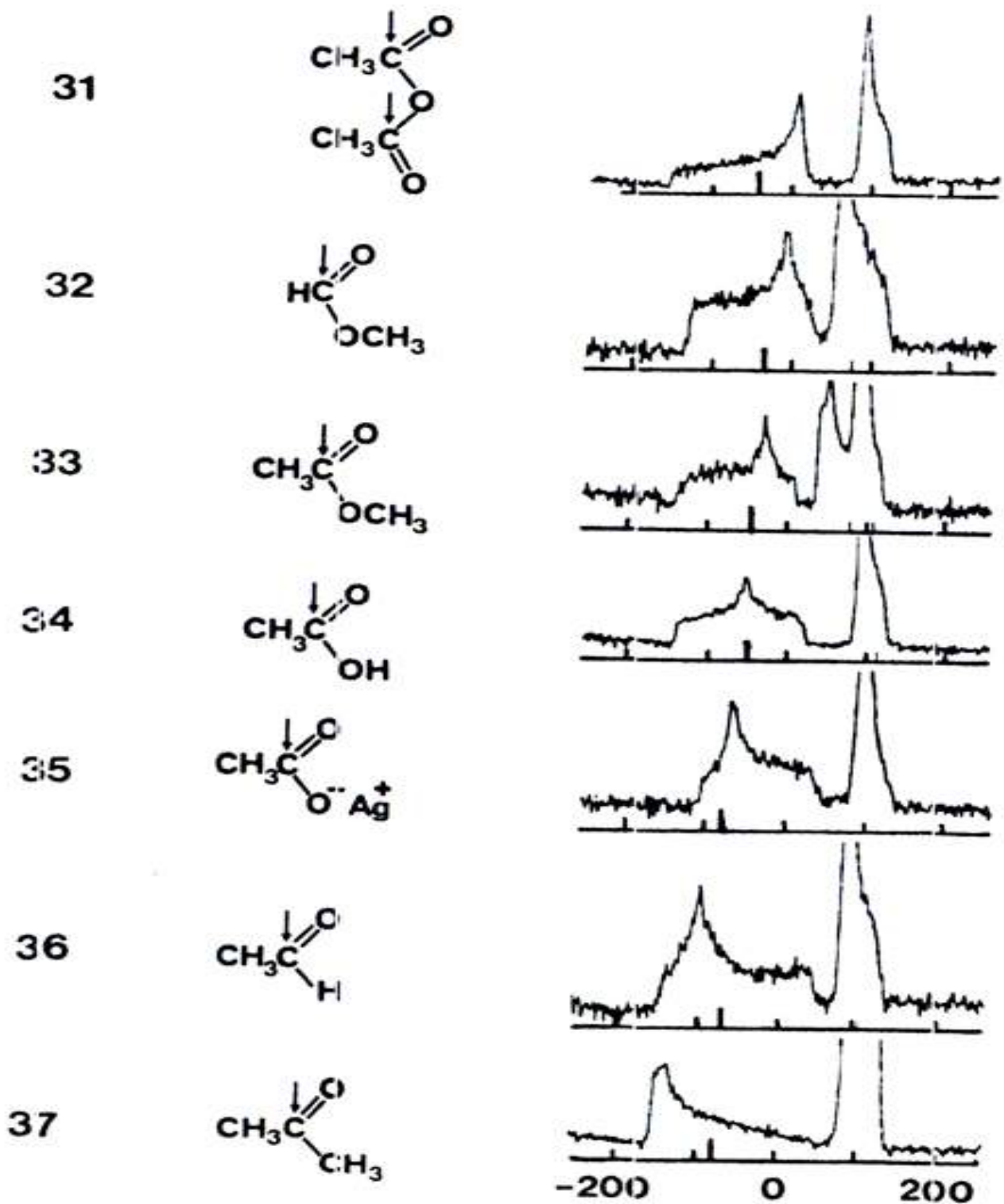
$$\sigma_{iso} = \sigma_{11} + \sigma_{22} + \sigma_{33}$$

Axially shift anisotropy

$$\sigma_{11} = \sigma_{22} = \sigma_{\perp} \quad \sigma_{33} = \sigma_{\parallel}$$

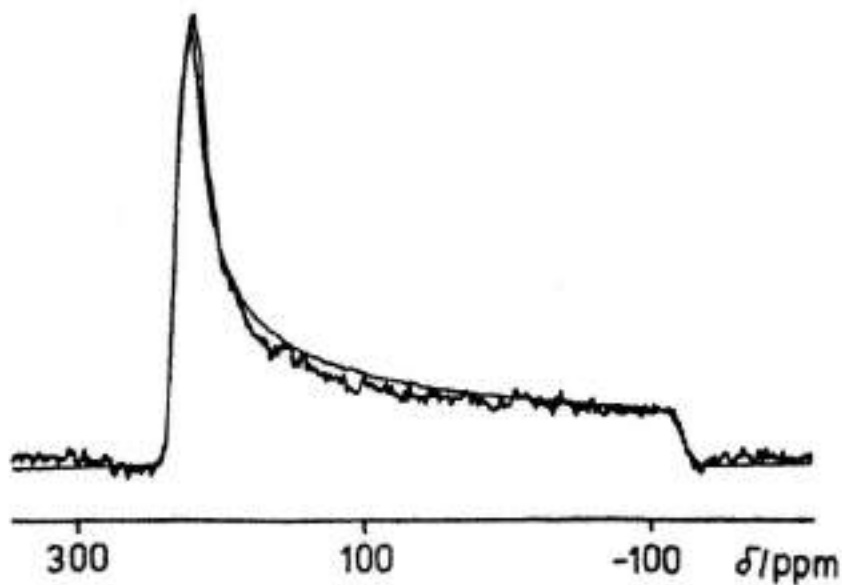


^{13}C spectra of polycrystalline compounds containing carbonyl groups.
Low-field: CO; high field: CH_3

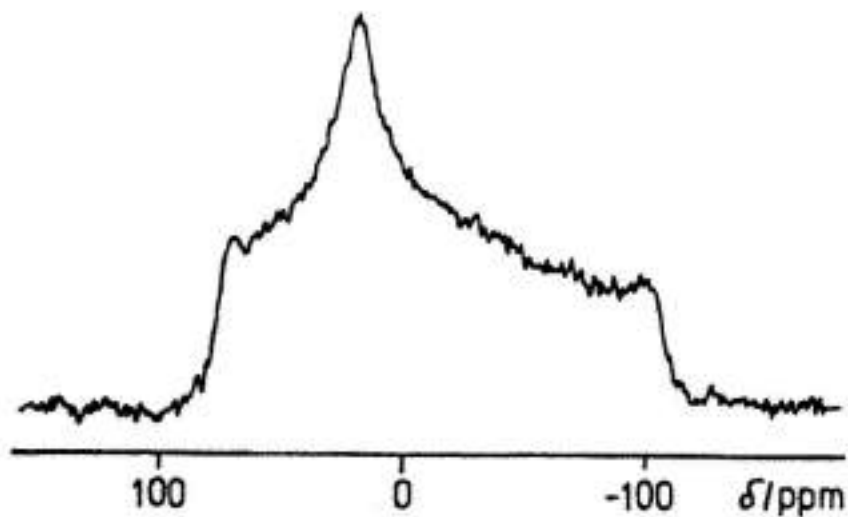


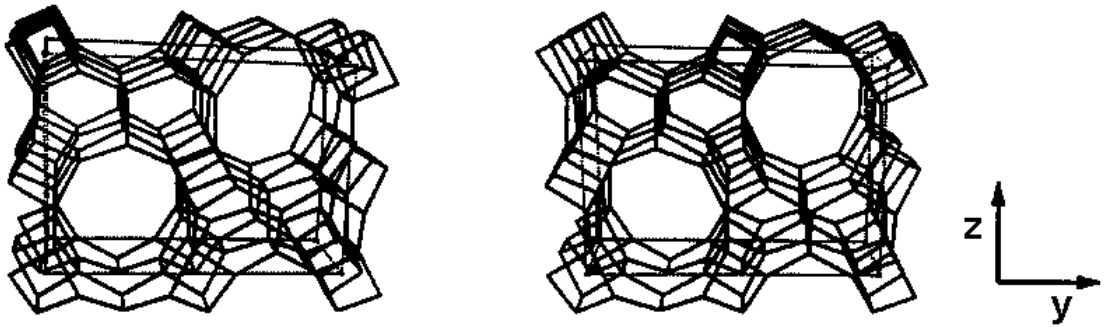
^{31}P NMR

P_4O_6

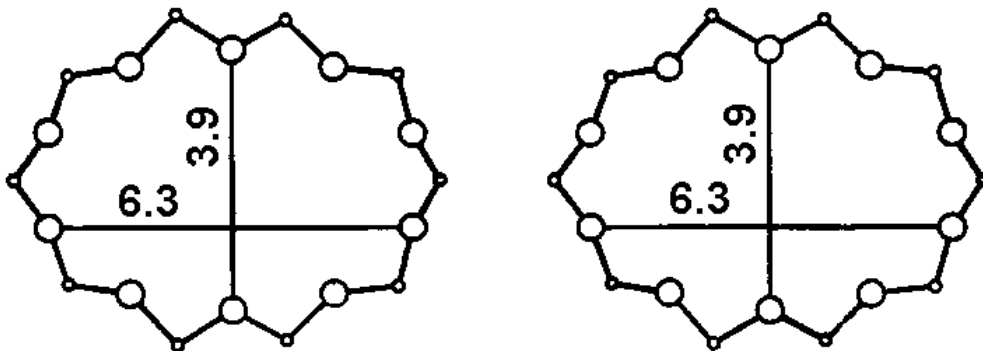


$\text{Ba}(\text{Et})_2\text{PO}_4$



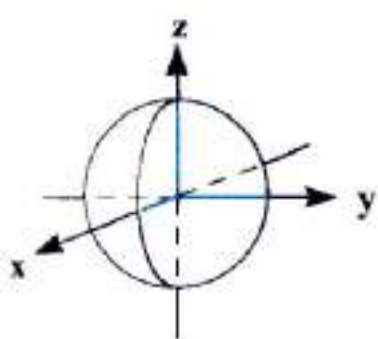
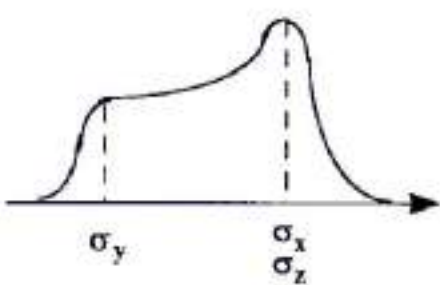
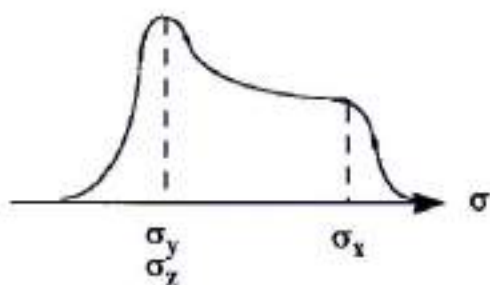
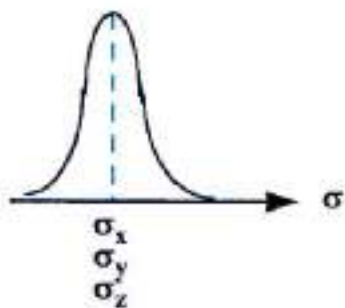
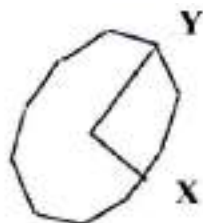


Framework viewed along [100]

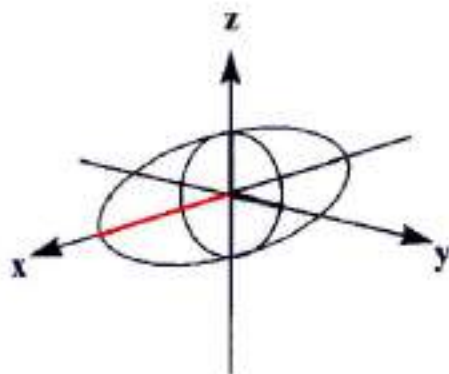


10-ring viewed along [100]

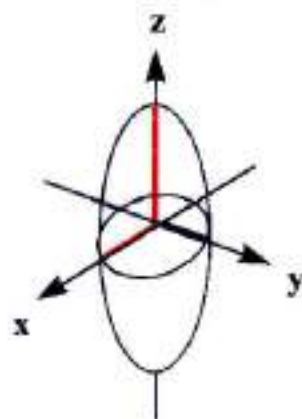
Anisotropy of chemical shift



$$\sigma_x > \sigma_y = \sigma_z$$

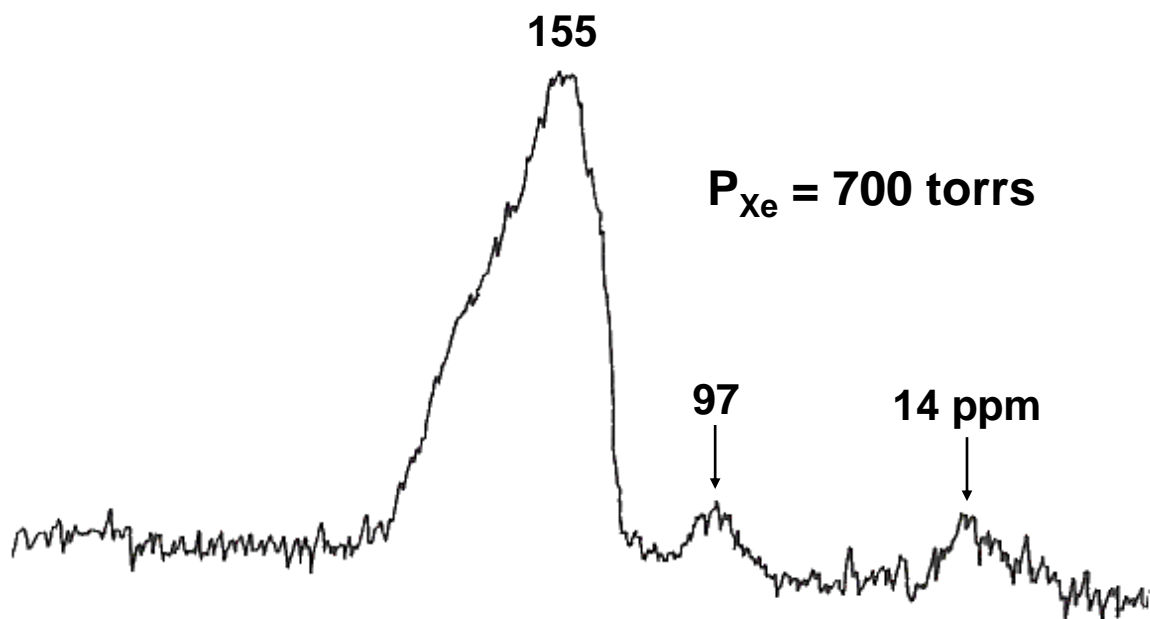
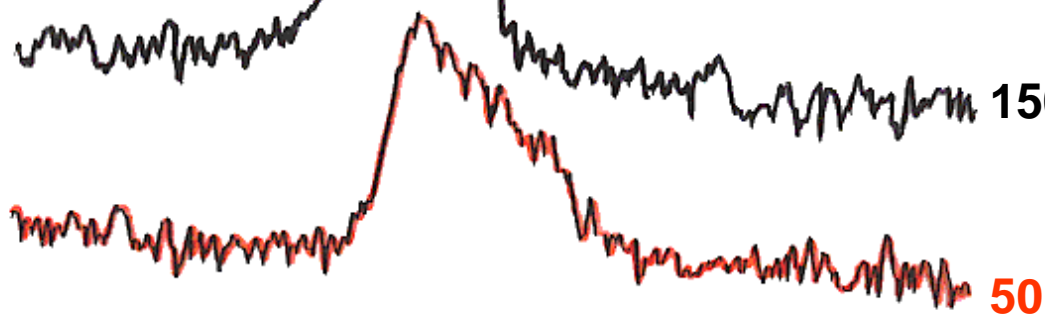
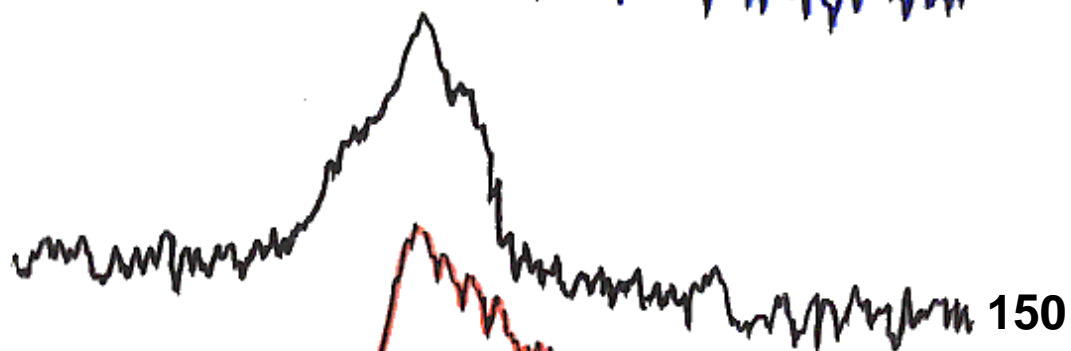
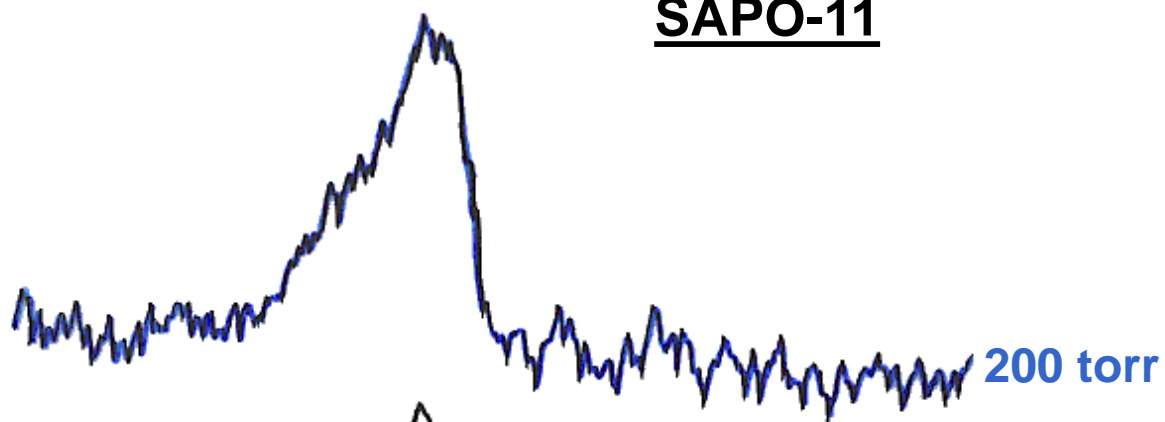


$$\sigma_x > \sigma_y = \sigma_z$$



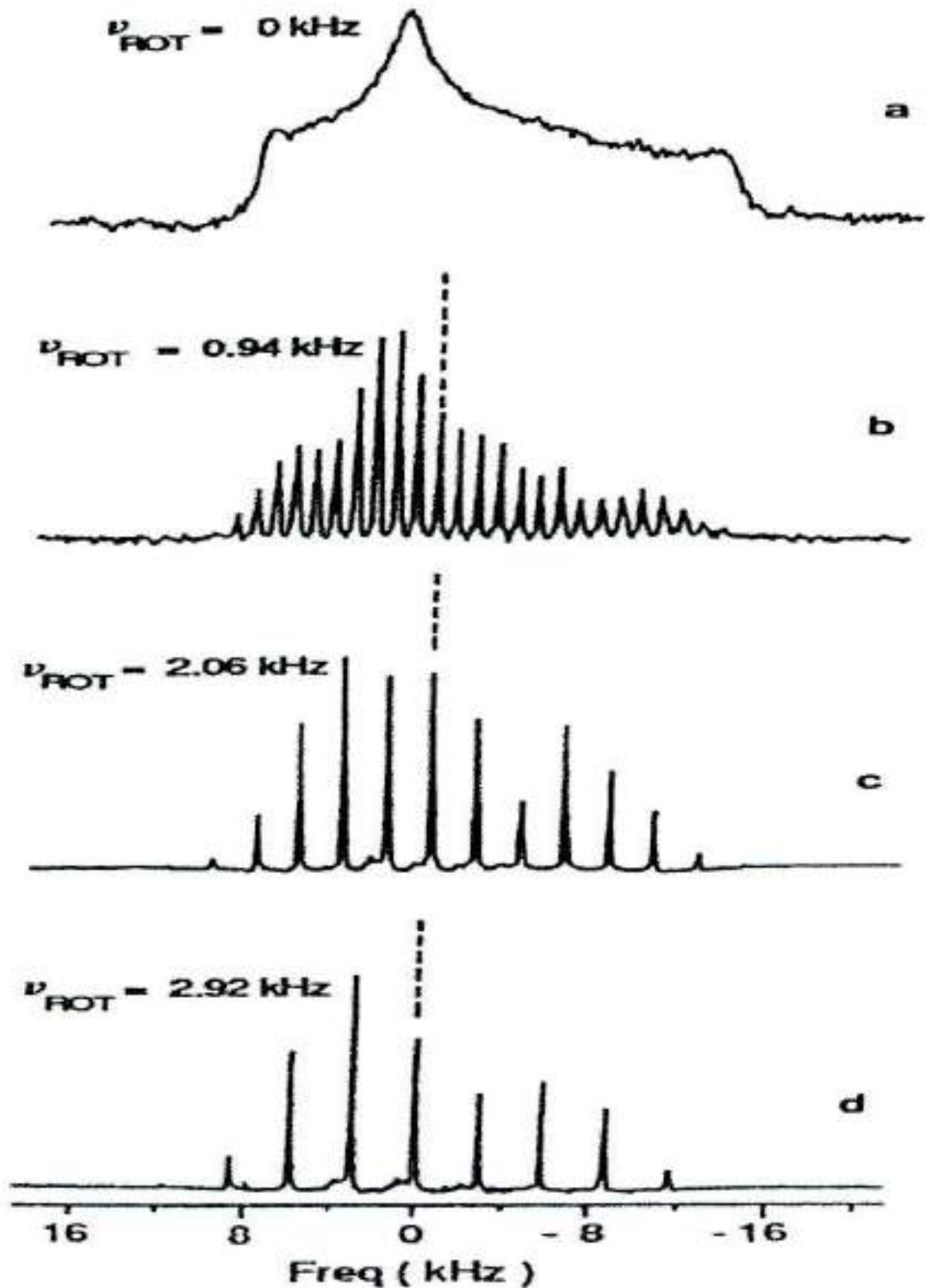
$$\sigma_y < \sigma_x = \sigma_z$$

SAPO-11

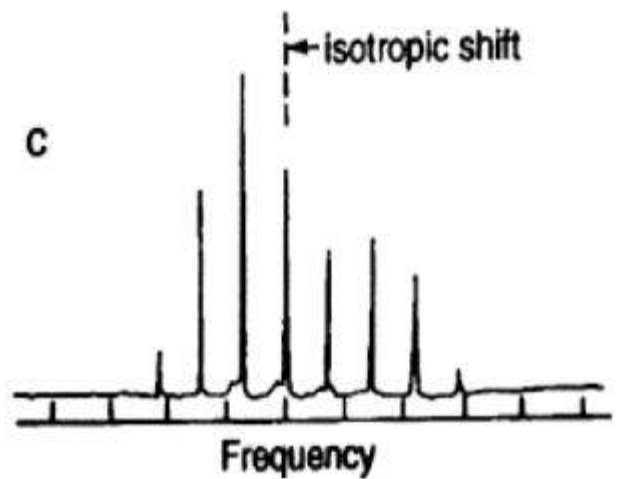
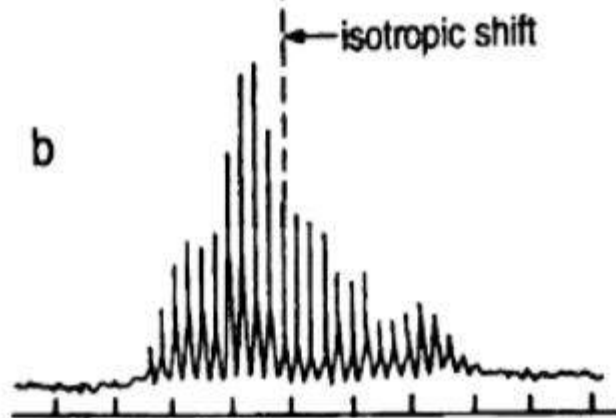
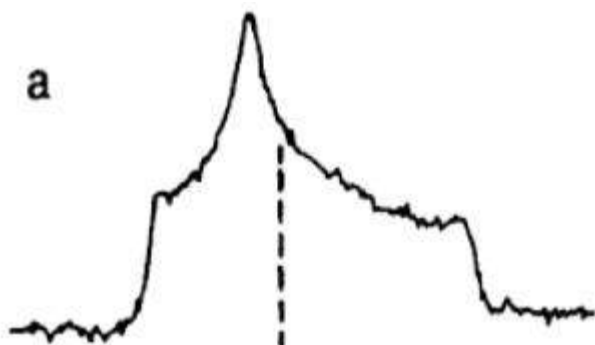


SAPO 11-3

Influence of the rotation on the sidebands



a) Static; b) low spinning;
c) fast spinning side bands



End of the second part

