



NMR of Solids

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Interactions of nuclear spins in a solid



$\hat{H}_Z =$ Zeeman effect

$\hat{H}_{RF} =$ RF field

$\hat{H}_{CS} =$ Chemical shift

$\hat{H}_J =$ JJ coupling

$\hat{H}_D =$ Dipole interactions

$\hat{H}_Q =$ Quadrupole coupling

$\hat{H}_{ij} =$ Unpaired electron

$$\hat{H}_X = \vec{A} \cdot \vec{T}_X \cdot \vec{B}$$

$\vec{T}_X =$ second rank tensor

$\hat{H}_Z \gg$ other interactions

Very often some effects are masked by the others.

For example $\hat{H}_D \gg \hat{H}_J$

$\hat{H}_X = K$ (spin factor) [space factor $f(\theta)$]

$\theta =$ angle between an axis of the system and B_0

Chemical Shift

CHEMICAL SHIFT δ

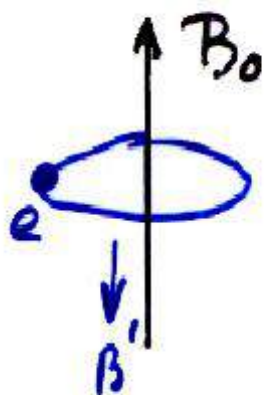
$$\omega = \gamma B$$

$$\text{Sample: } 2\pi\nu_s = \gamma B_0(1 - \sigma_s)$$

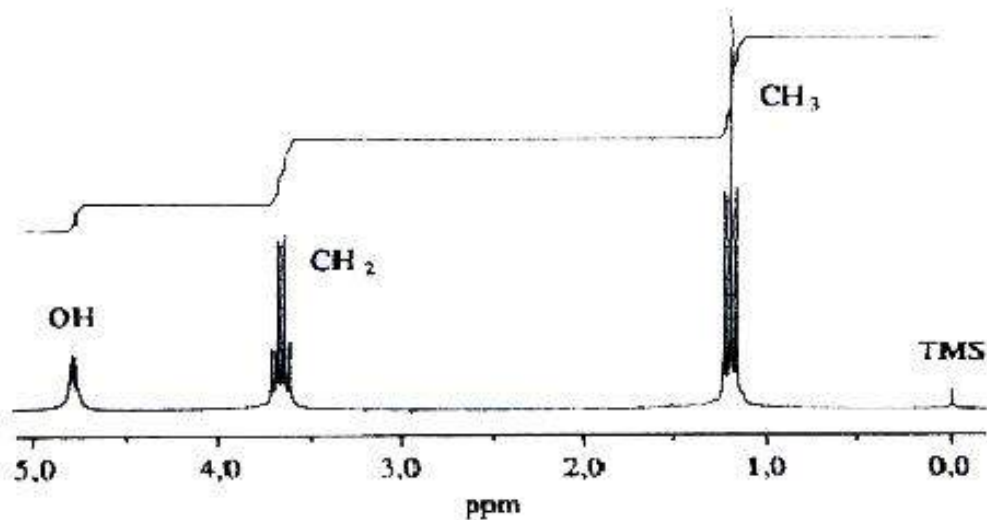
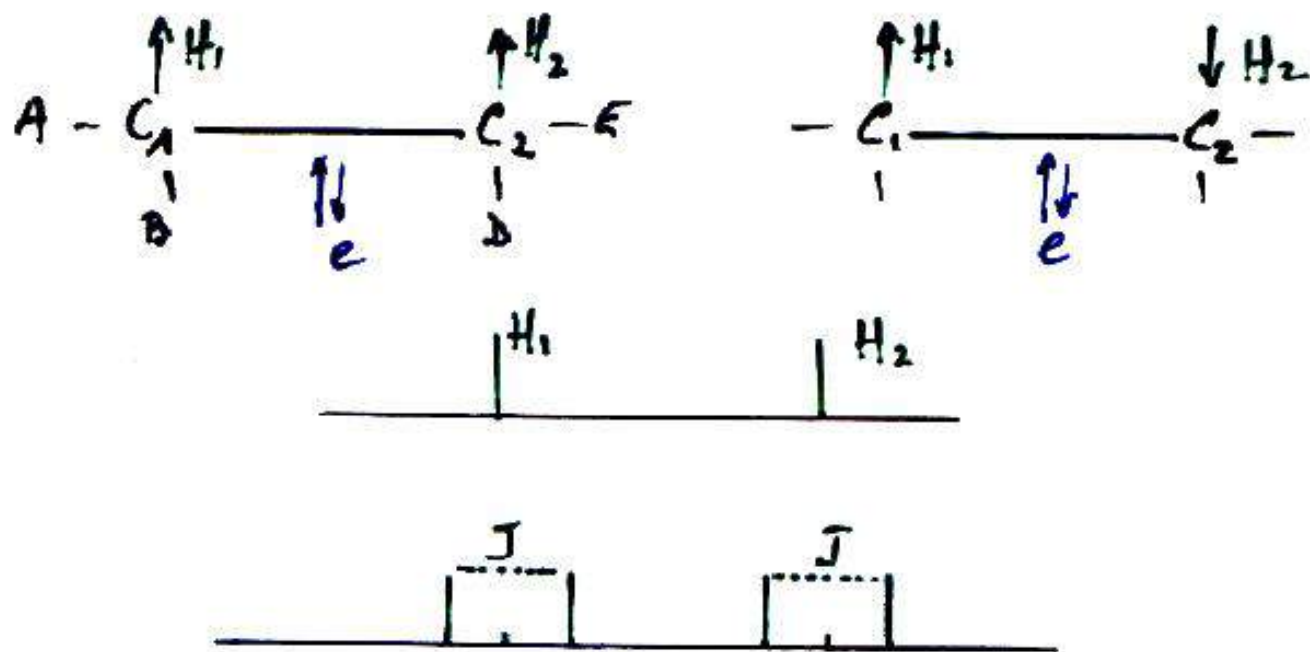
$$\text{Reference: } 2\pi\nu_r = \gamma B_0(1 - \sigma_r)$$

$$\Delta N = \nu_r - \nu_s = \frac{\gamma B_0}{2\pi} (\sigma_s - \sigma_r)$$

$$\delta = \frac{\gamma B_0 / 2\pi (\sigma_s - \sigma_r)}{\gamma B_0 / 2\pi (1 - \sigma_r)} \sim \sigma_s - \sigma_r \quad \text{ppm}$$

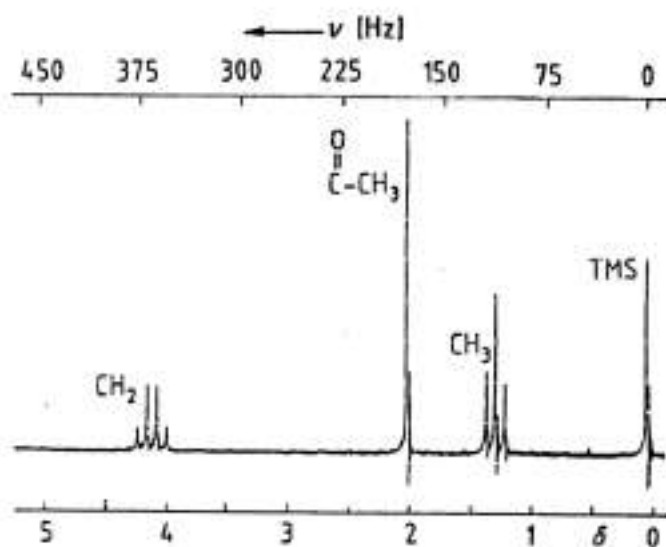
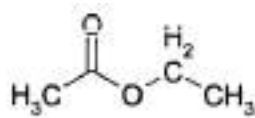


SPIN-SPIN COUPLING J



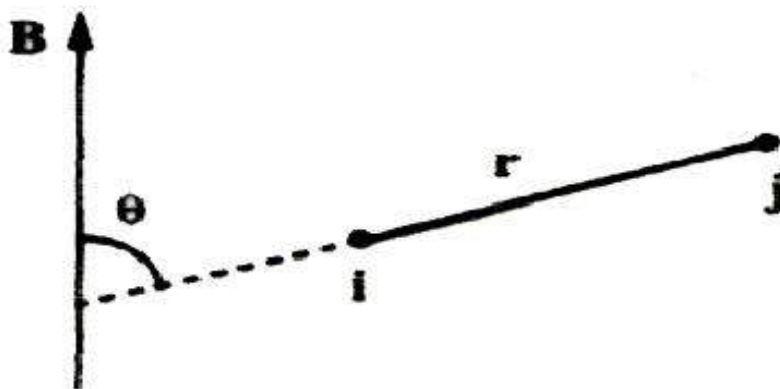
$$2nI + 1$$

Ethyl acetate



Dipolar Magnetic Interaction between two ^1H nuclei

$$\text{DMI} = \text{CONSTANT} \cdot (1 - 3 \cos^2 \theta) \cdot r^{-3}$$



For powder samples the interactions must be summed up over all directions.

$$\text{DMI} = 0 \quad \text{if} \quad \cos \theta = 1/\sqrt{3}$$

$$\theta = 54^\circ 44'$$

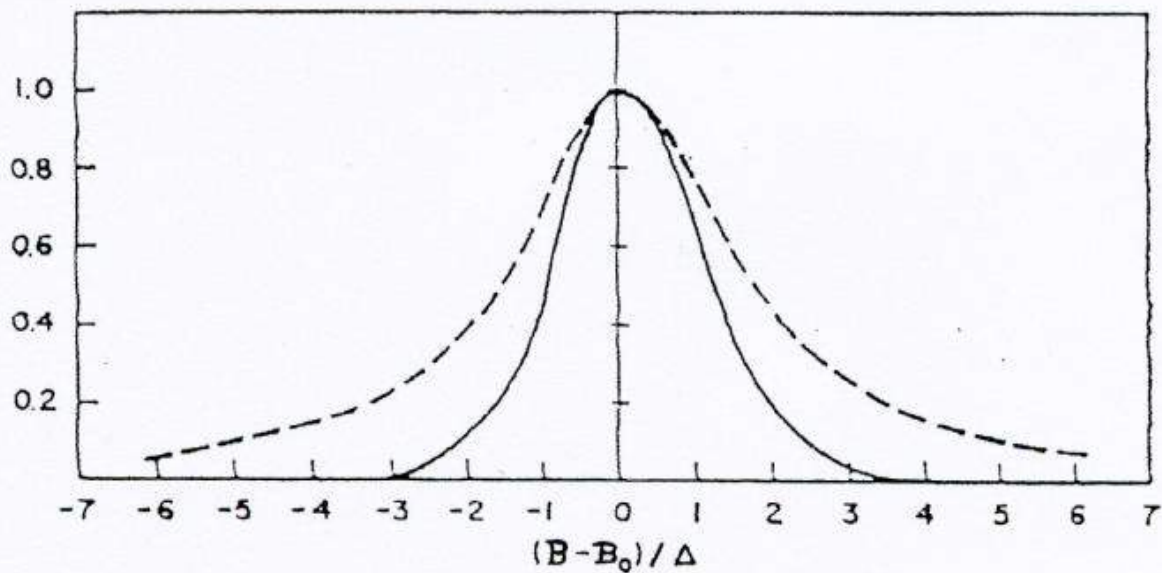
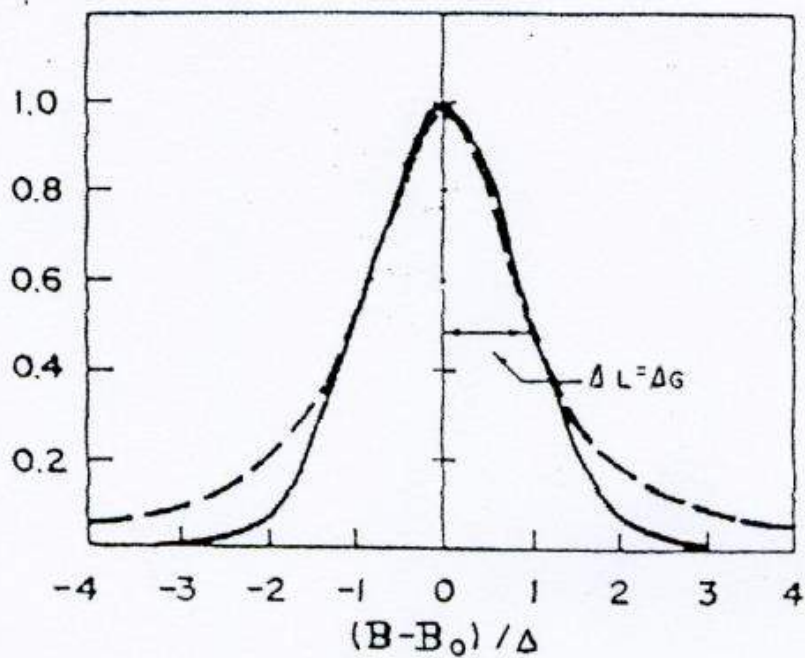


Figure 1. Zero derivative curves for Gaussian (solid line) and Lorentzian (broken line) shape function; (a) curves have the same half-line width half-maximum intensity; (b) curves have the same peak-to-peak line width.

Spectrum for a two spins magnetic configuration

- - - - theoretical; _____ real

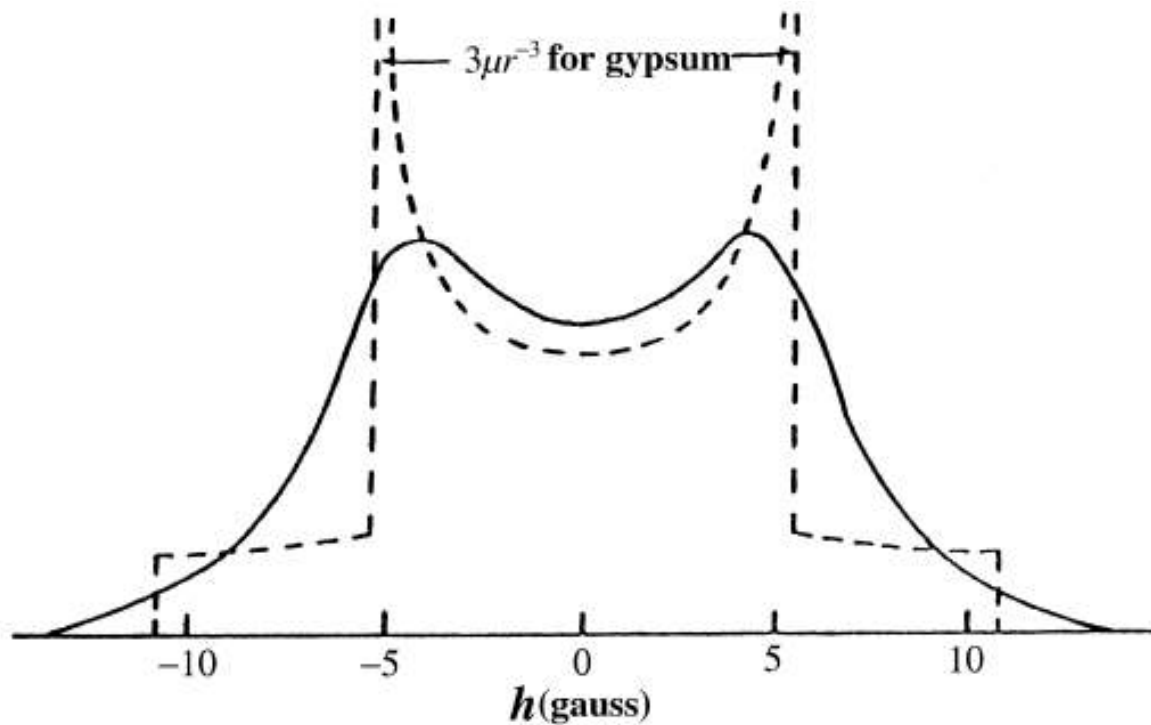
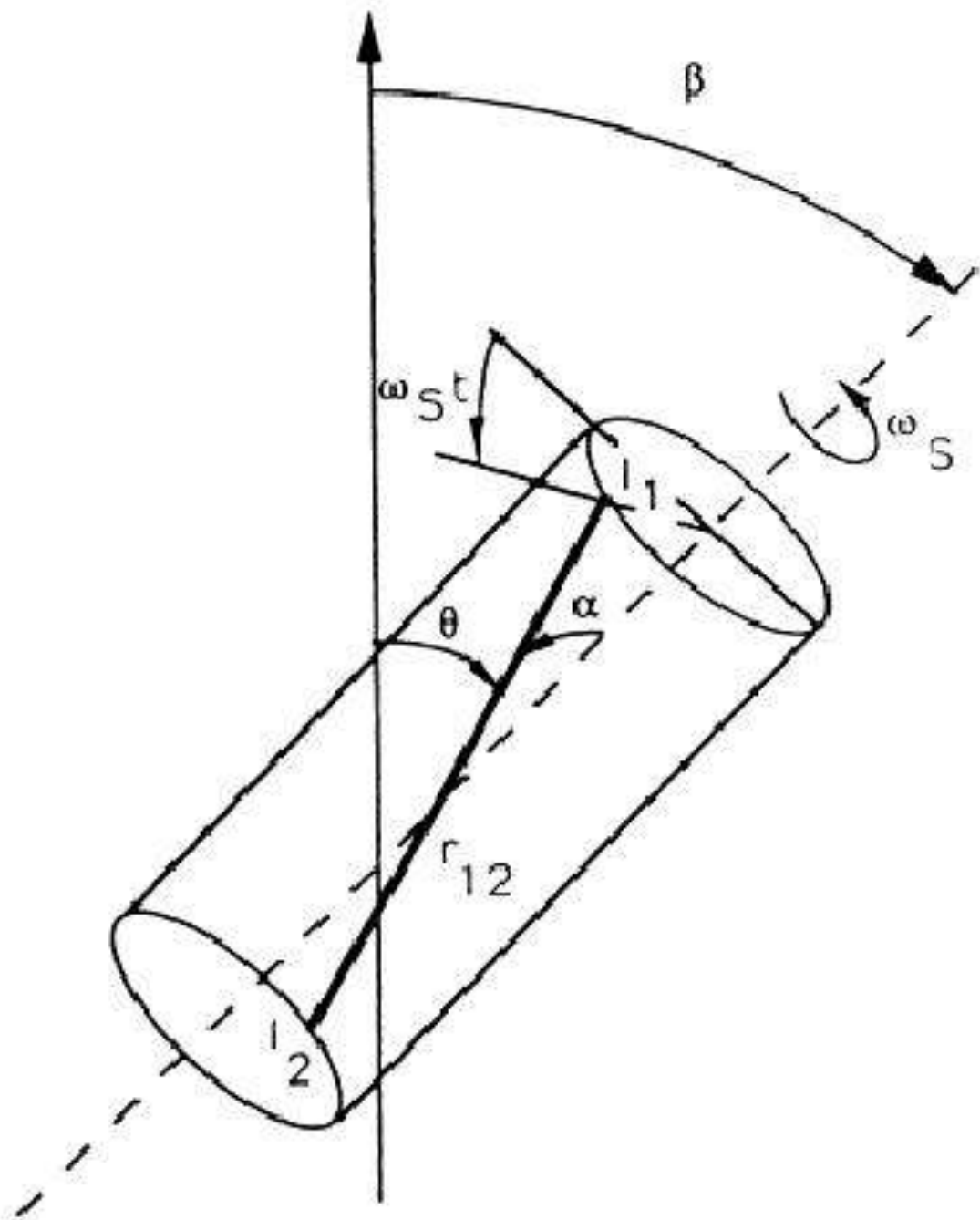
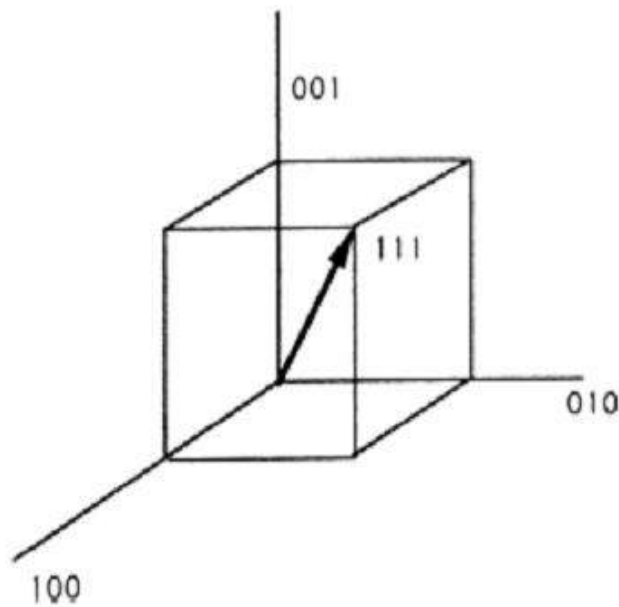


FIG. 3.10 – Spectres théorique (courbe en pointillée) et réel (trait plein) pour une configuration magnétique à deux spins dans une poudre.

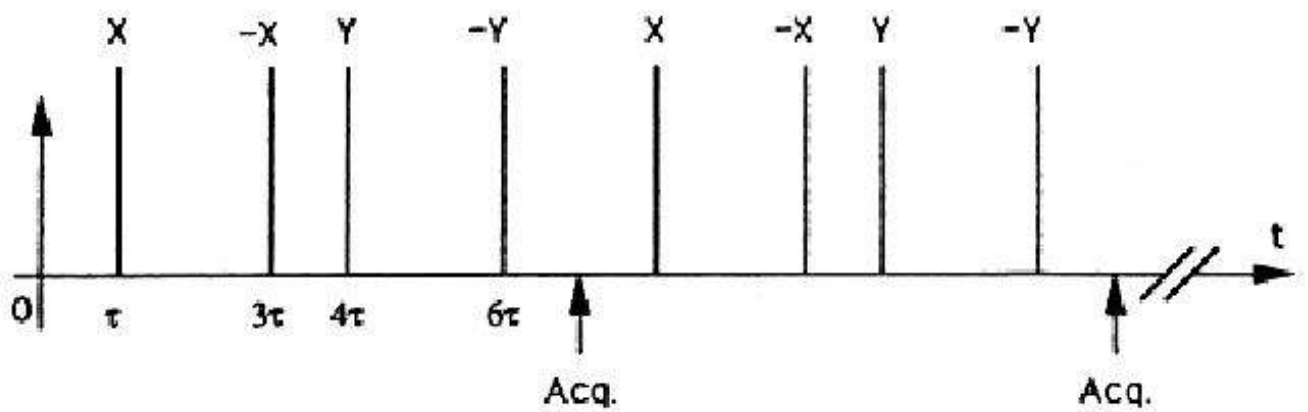
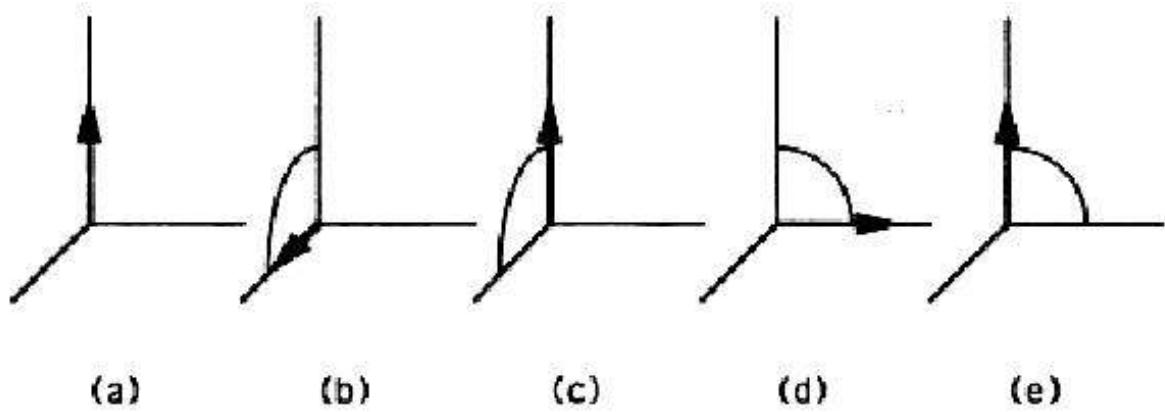
Magic angle spinning (MAS)



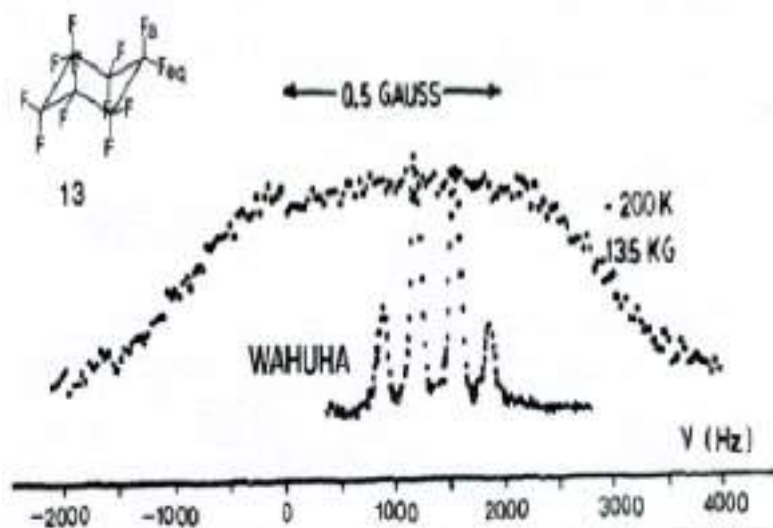
The angle between the diagonal of the cube and the side is = the magic angle



Pulse sequences

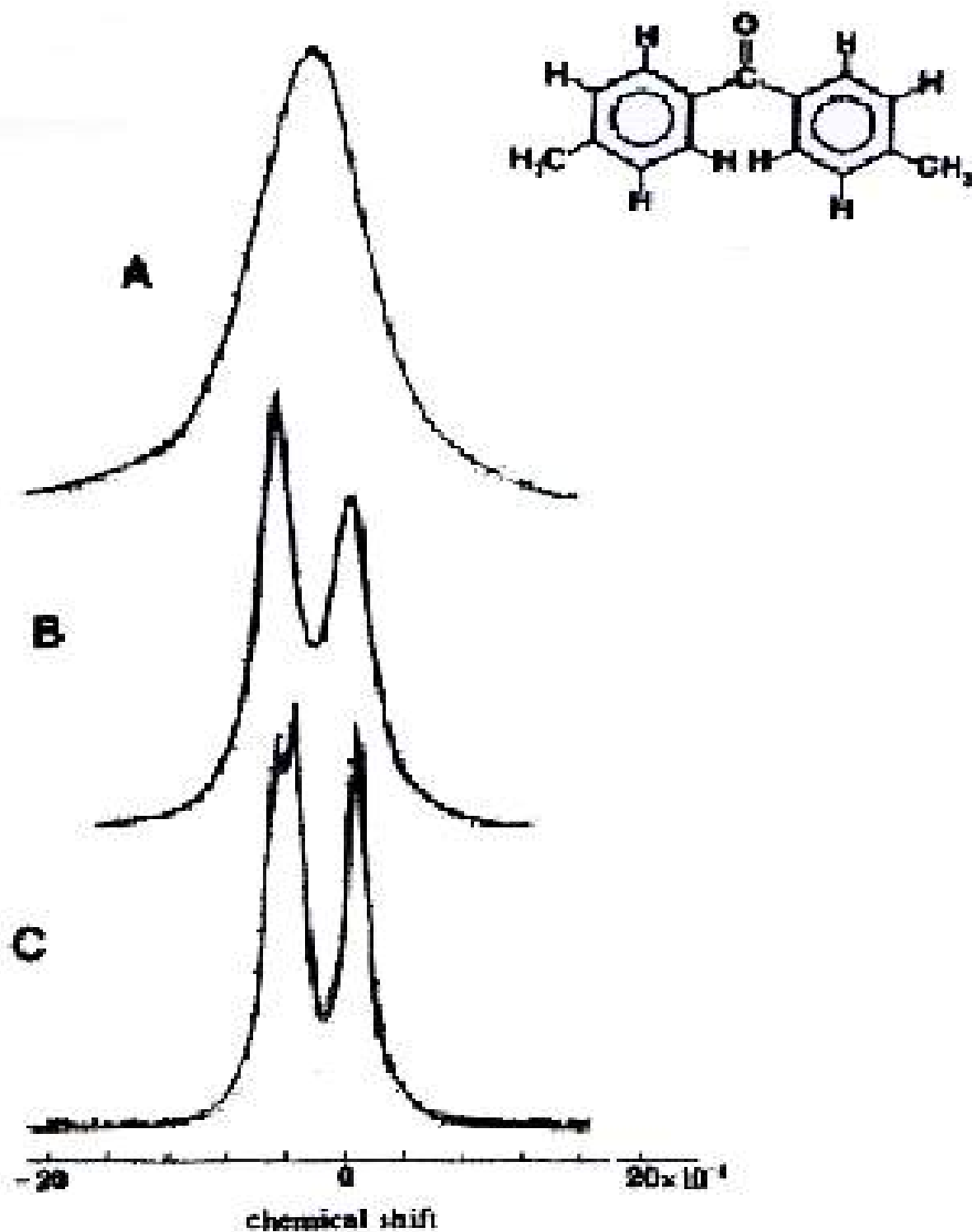


^{19}F NMR. Application of the Wahuha sequence to perfluorocyclohexane C_6F_{12} at 200 K

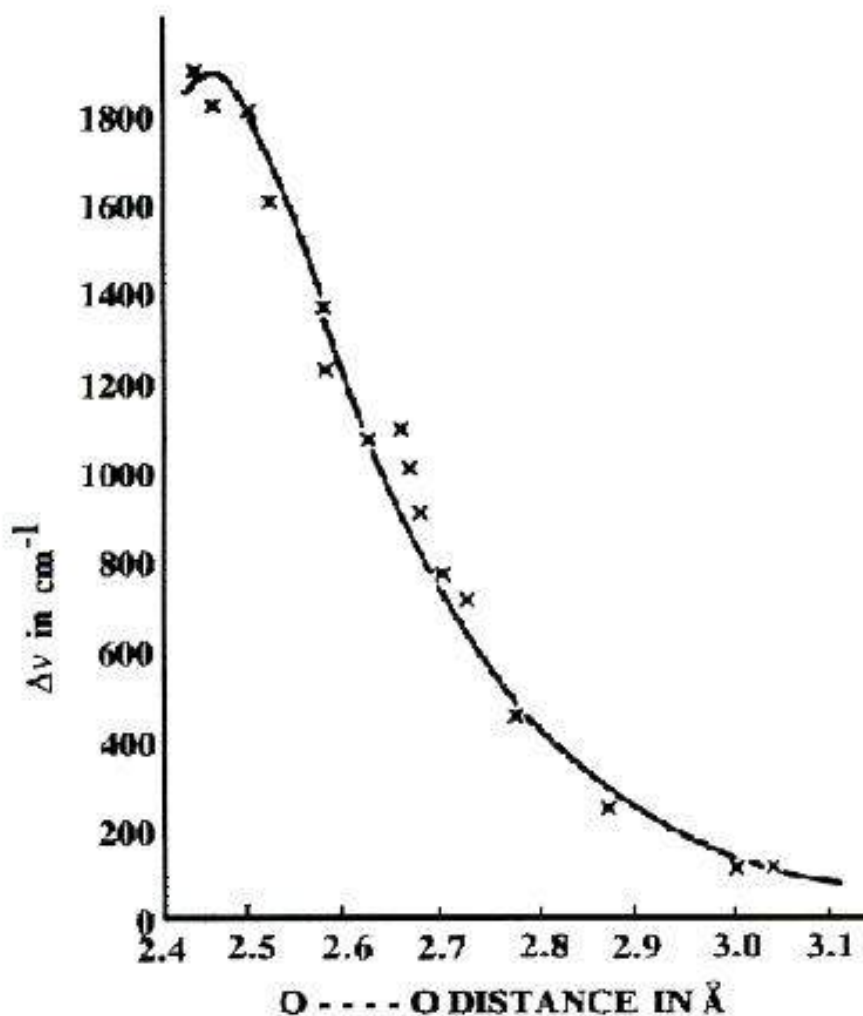


4,4'-dimethylbenzophenone

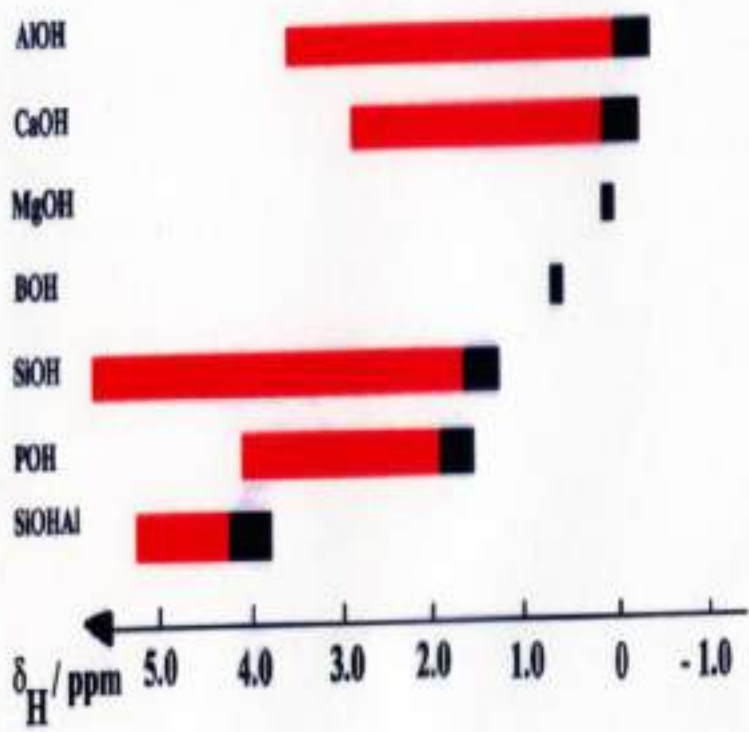
A: MREV-8; B: MREV-8 + MAS; C: BR24 + MAS



IR: $\Delta\nu$ in cm^{-1} against hydrogen bond

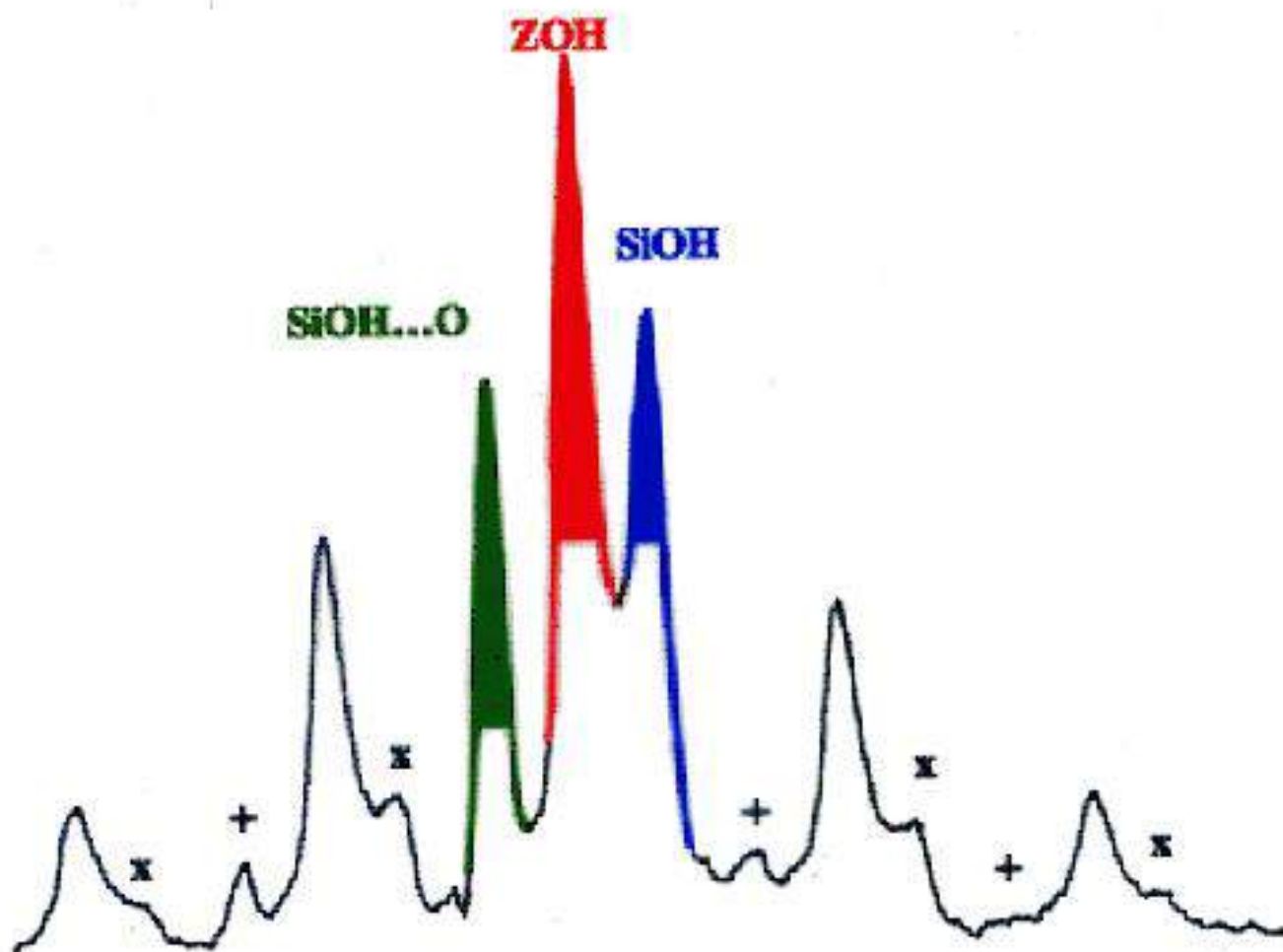


The relation between OH frequency shift and O - - - O distance during hydrogen-bonding interaction

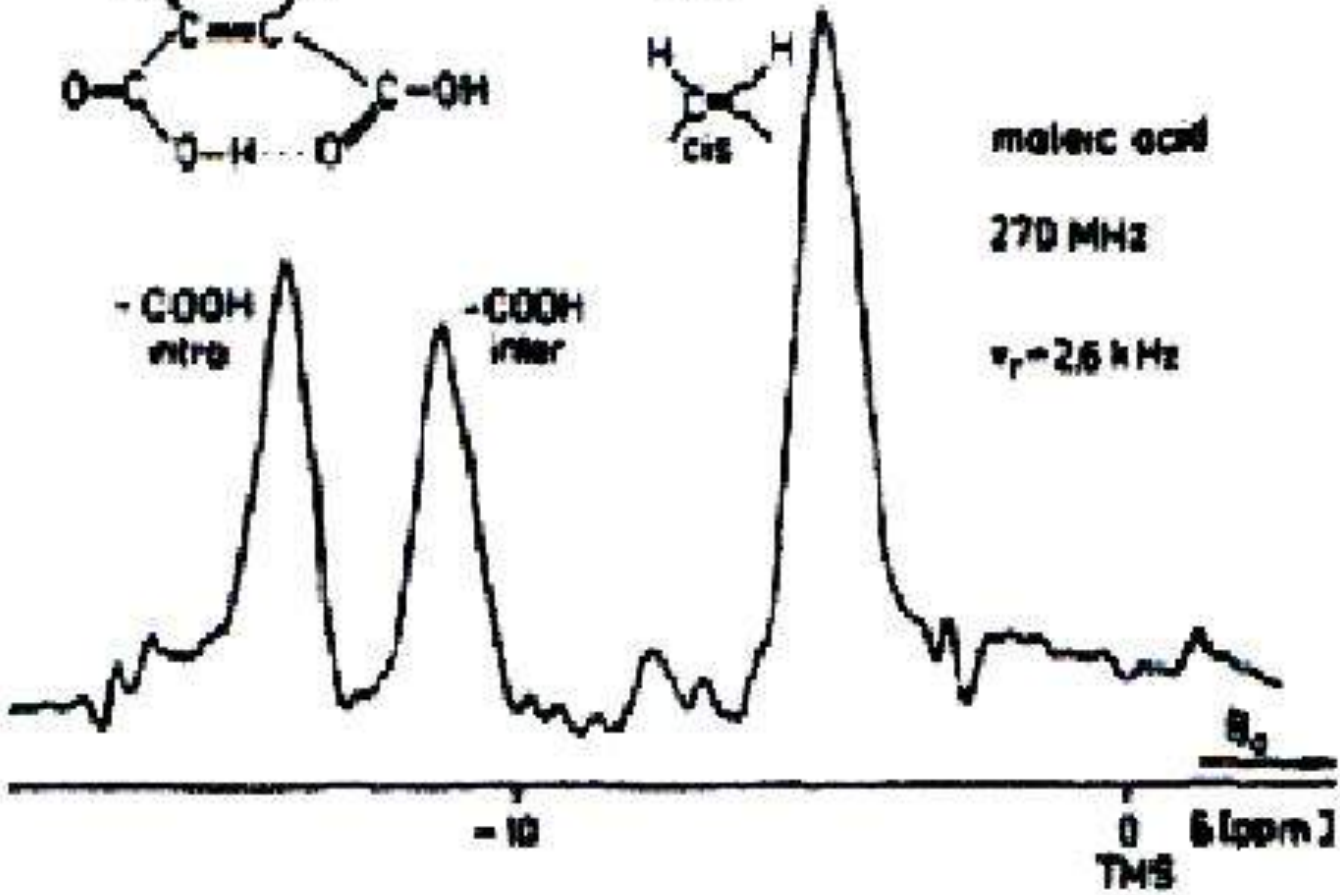
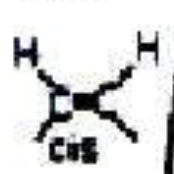
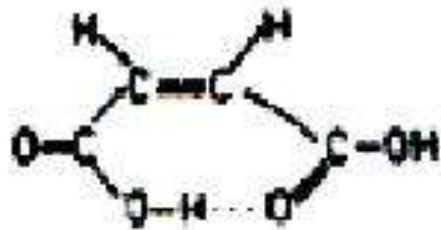
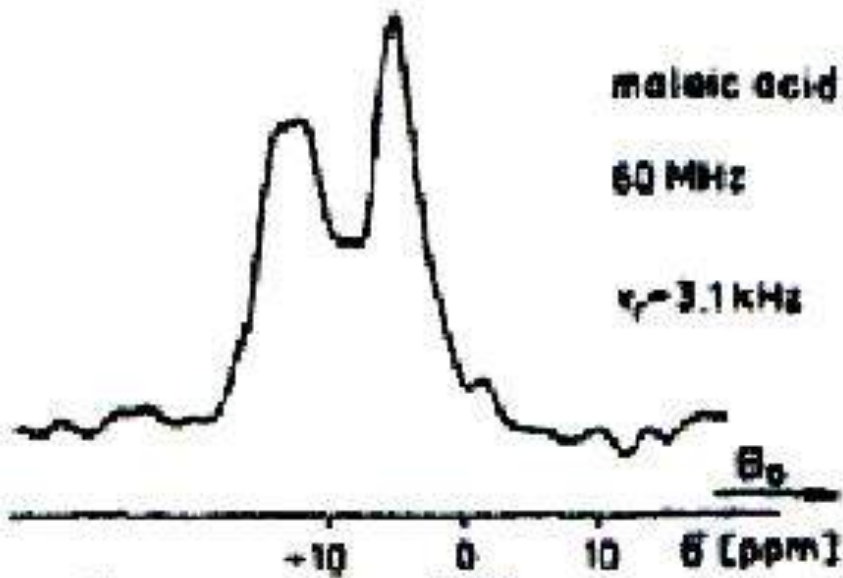


Intervals for the experimentally determined values of the ^1H NMR chemical shift δ_{H} of isolated (black) and interacting (red area) OH groups in zeolites.

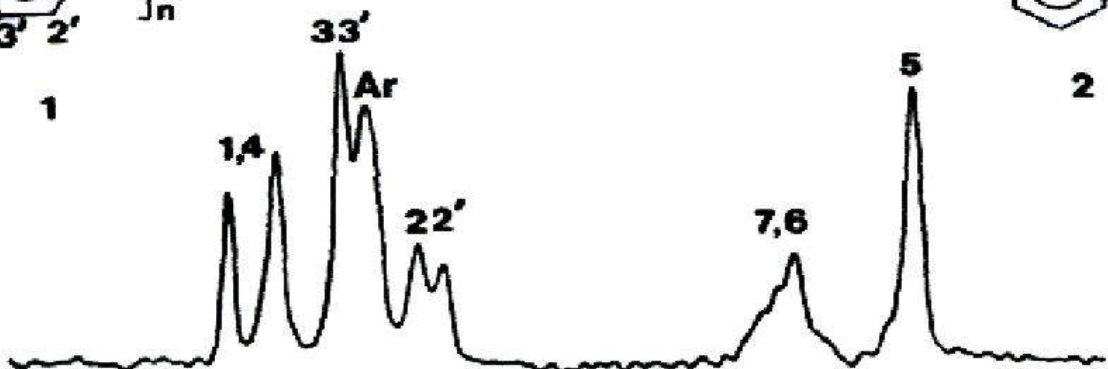
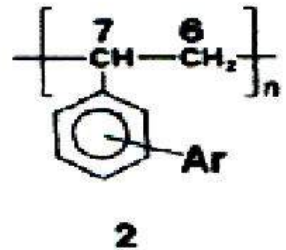
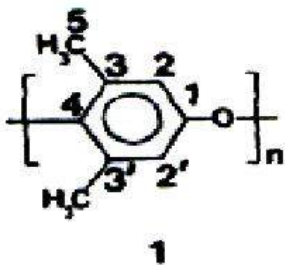
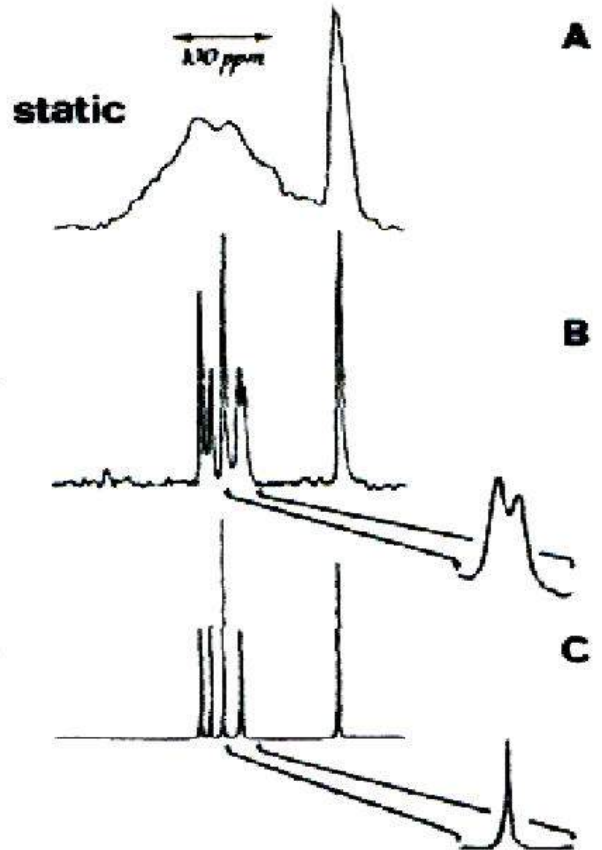
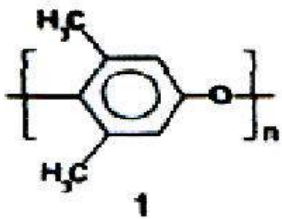
Anhydrous H-mordenite



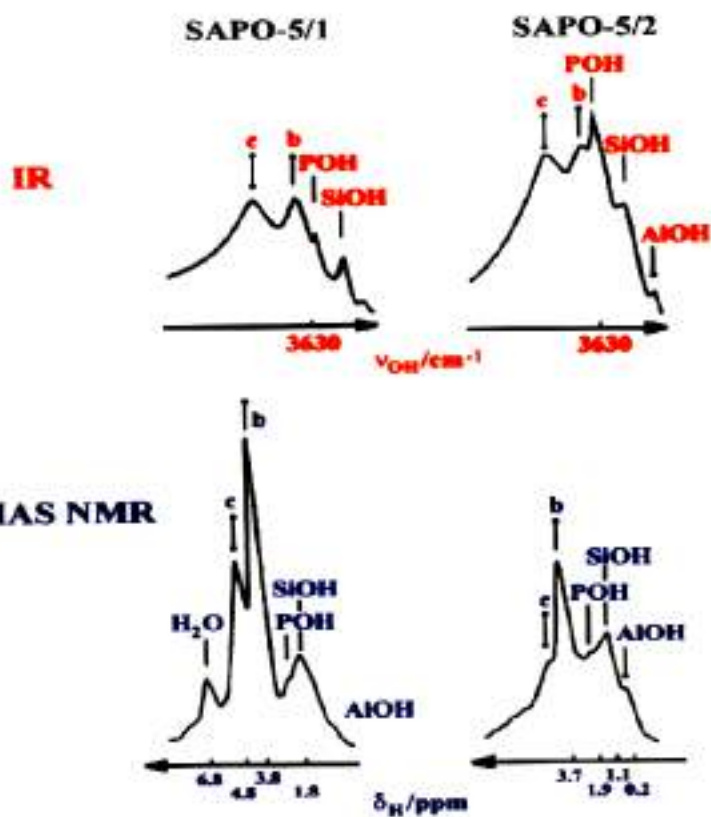
Maleic acid at 60 and 270 MHz
 Influence of hydrogen bond
HO2CHC=CHCO2H



Poly phenylene oxide and blend with polystyrene



Hydrogen bonds: δ (OH) and ν (OH) comparison of intensities



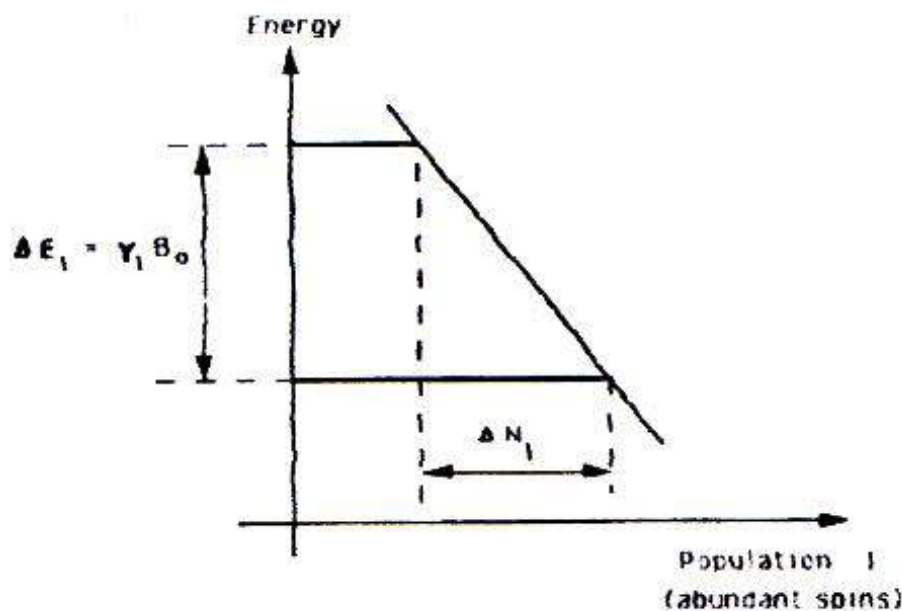
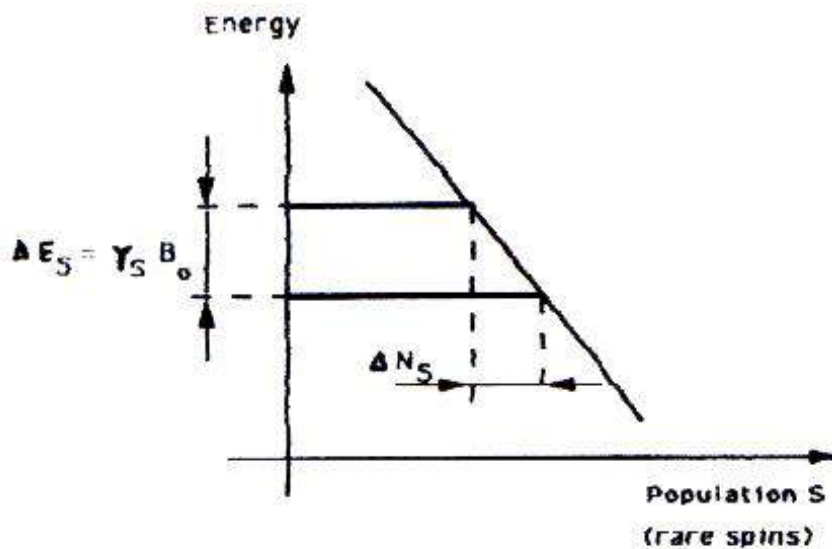
Polarization transfer from abundant spins I (high γ_I) to the low concentration spins S (low γ_S)

-:-:-:-:-:-:-:-

For spins $1/2$,

magnetization : $M = (N/4k_B T) \gamma \hbar B_0$

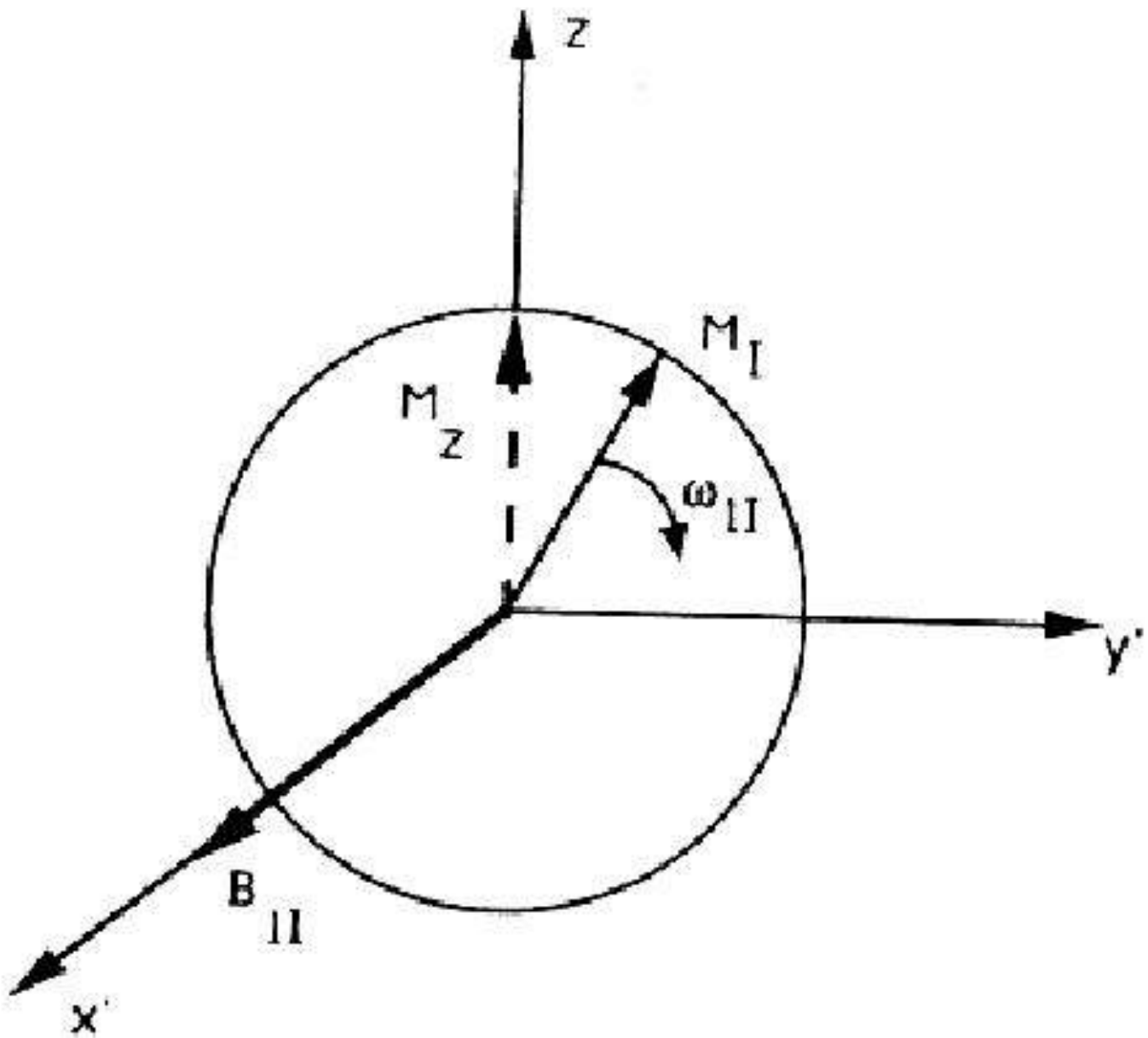
Signal/ noise ratio: $\propto (I+1) N \gamma^{5/2}$

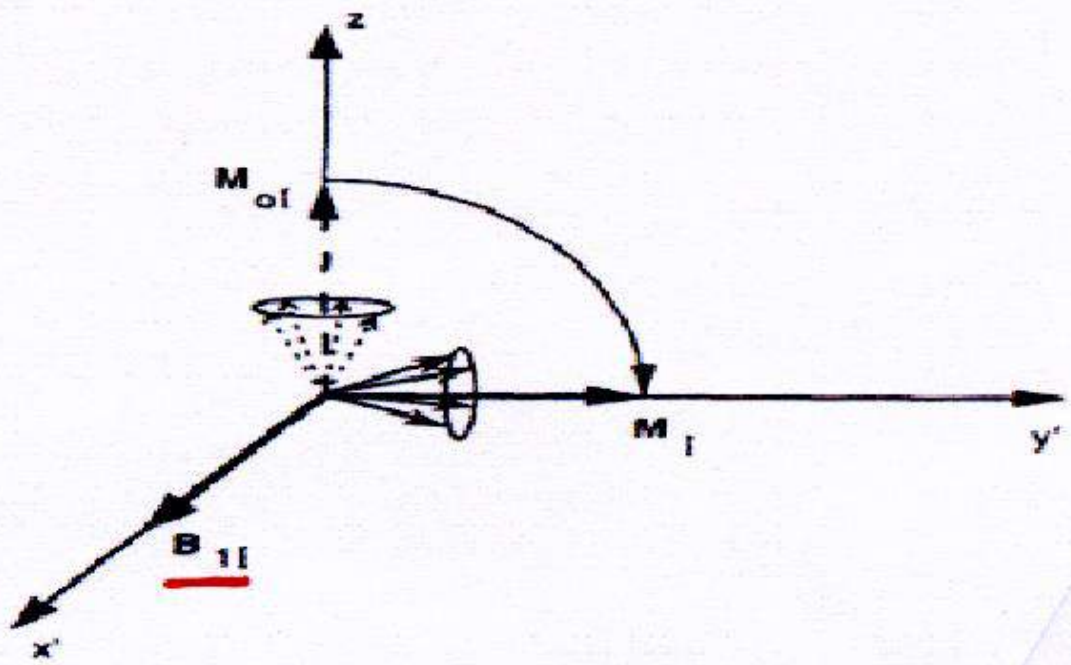


For the same B_0 , ΔN_I and ΔN_S are proportional to γ_I and γ_S .

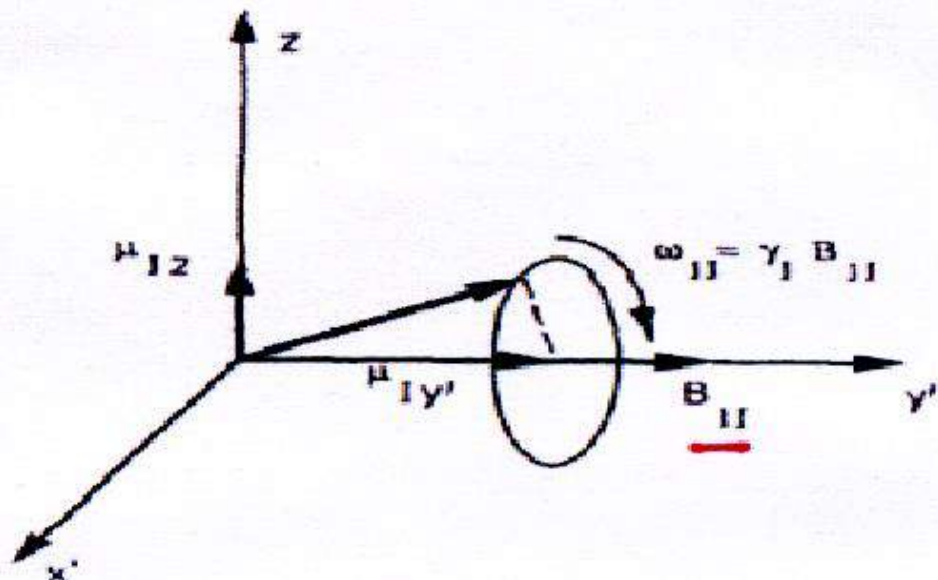
$\Delta N_I / \Delta N_S = \gamma_I / \gamma_S$

In the rotating framework
 B_{11} along x' \rightarrow rotation of M_1 in the
plane zoy'



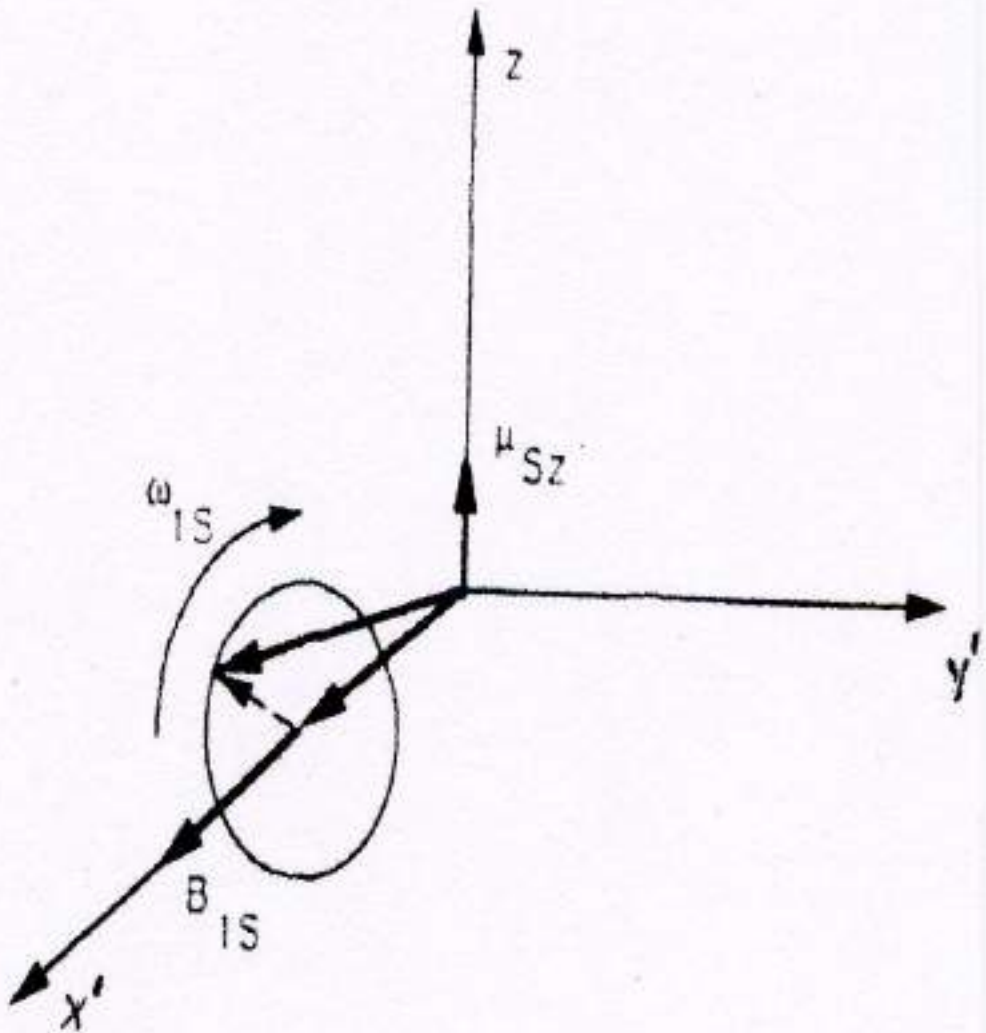


After a $\pi/2$ pulse along x' at frequency ω_{0I} the abundant spin magnetization M_I lies along y' .



Immediately after a second $\pi/2$ pulse along y' the I spins rotate around y' . The resultant magnetization M_I is “spin-locked” on the axis.

Due to another rf field $B_{1,s}$ along X' , individual magnetic moment μ_s turns around X' with a frequency $\omega_{1,s} = \gamma_s B_{1,s}$



Hartmann-Hahn condition

I and S have the oscillating components which may have the same time dependence if

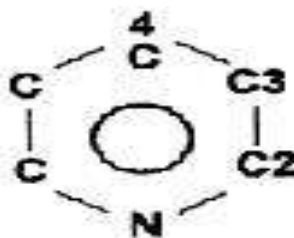
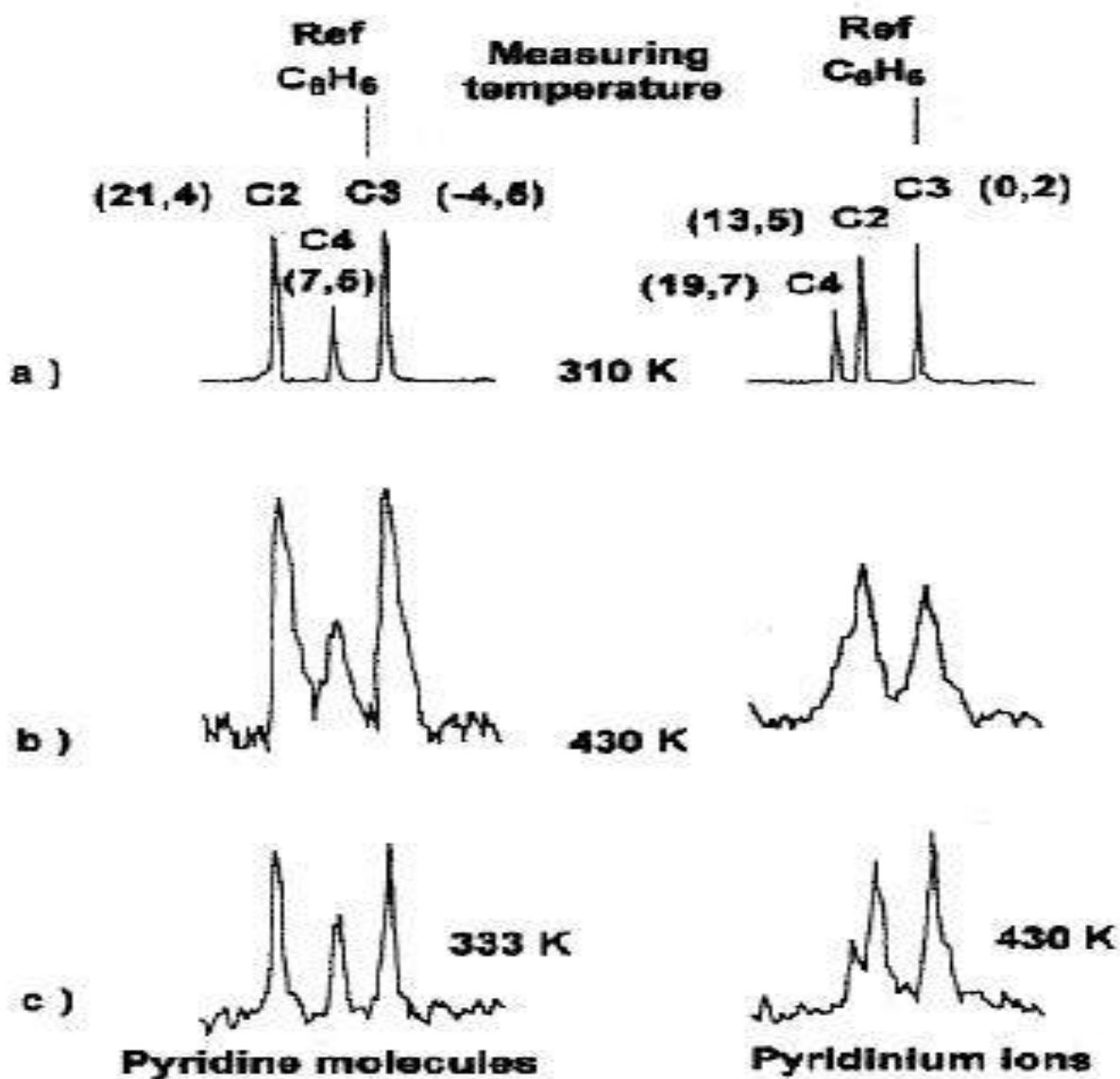
$$\omega_{1I} = \omega_{1S}$$

$$\gamma_S B_{1S} = \gamma_I B_{1I}$$

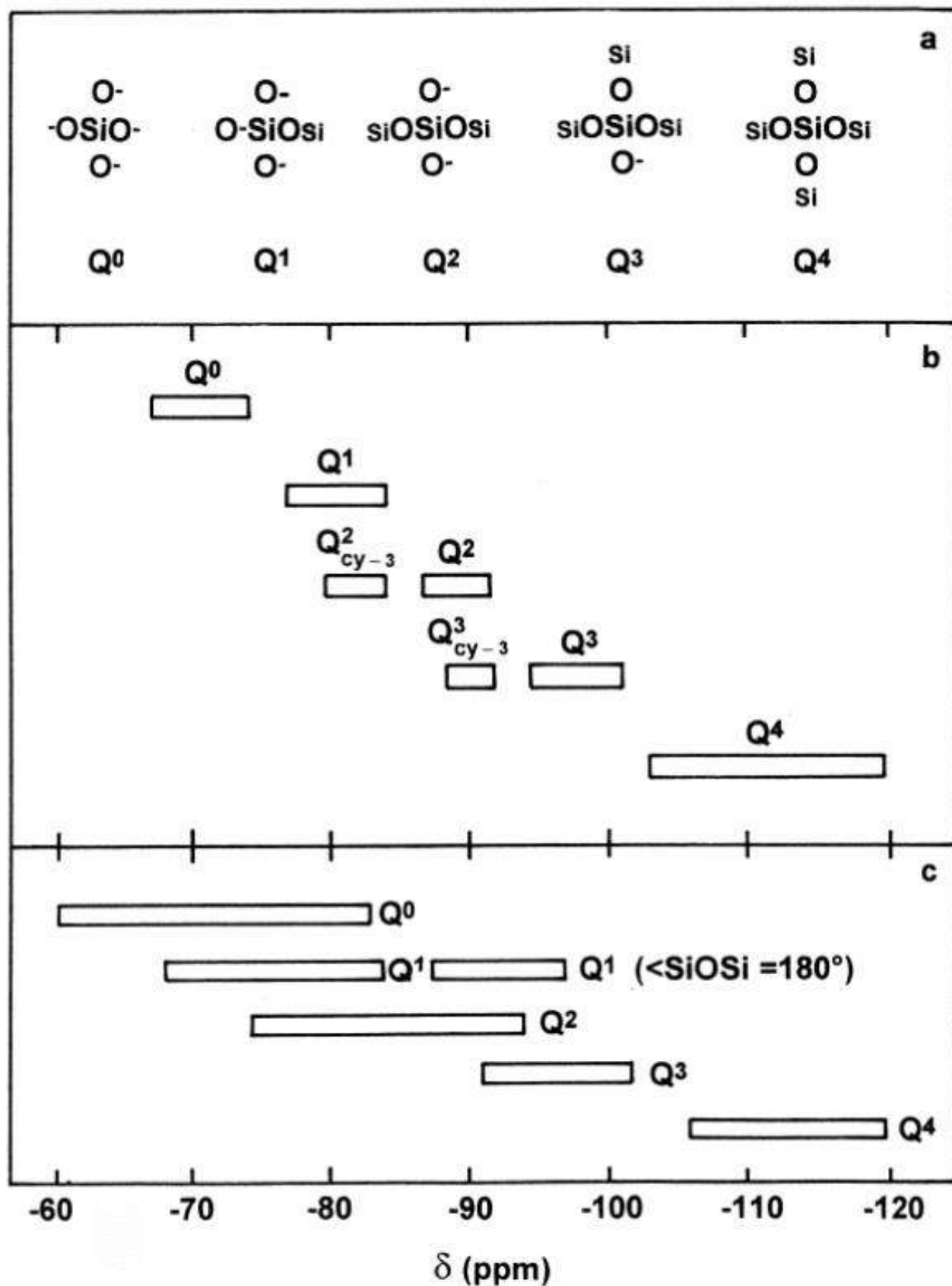
^{13}C NMR of Pyridine

a: liquid (left) and in H_2SO_4 (right)

b and c: adsorbed on NaY (left) and HY (right)

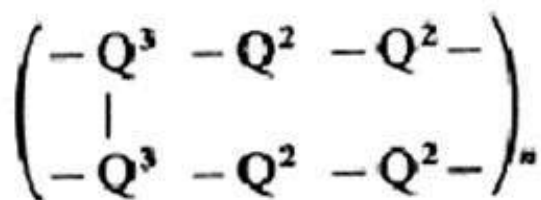
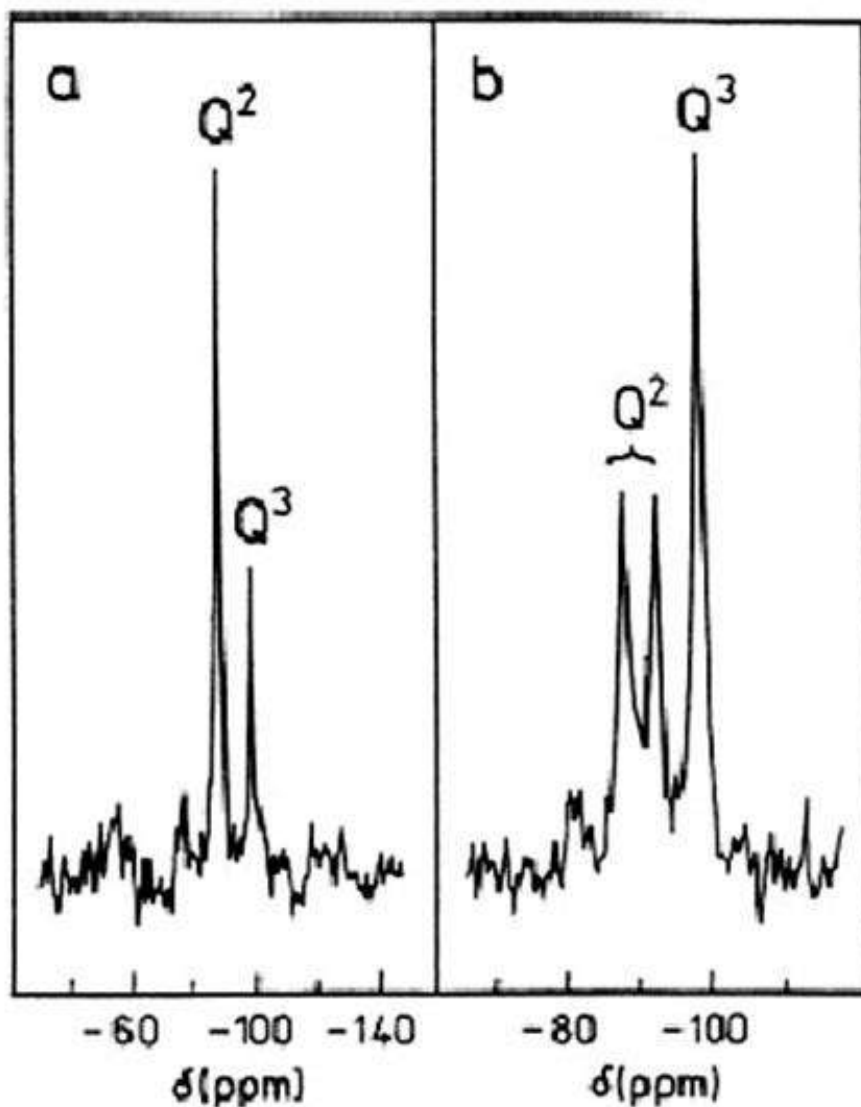


$\delta(^{29}\text{Si})$ for silicates Q_n

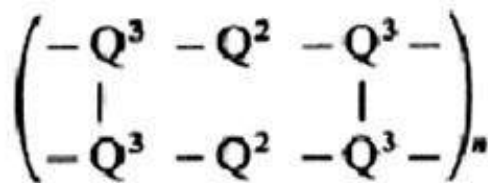


δ (Si)

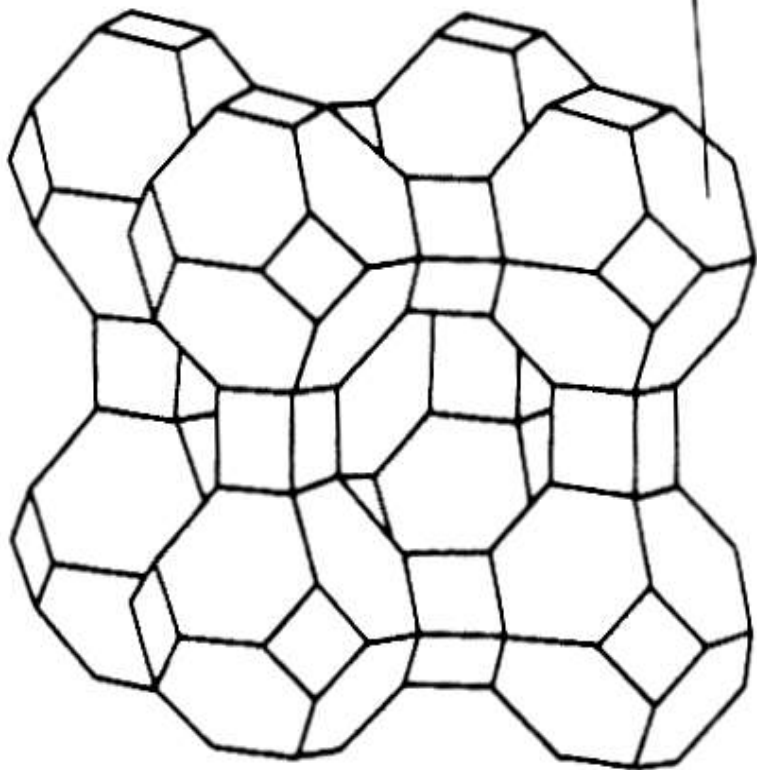
Xonolite Tremolite



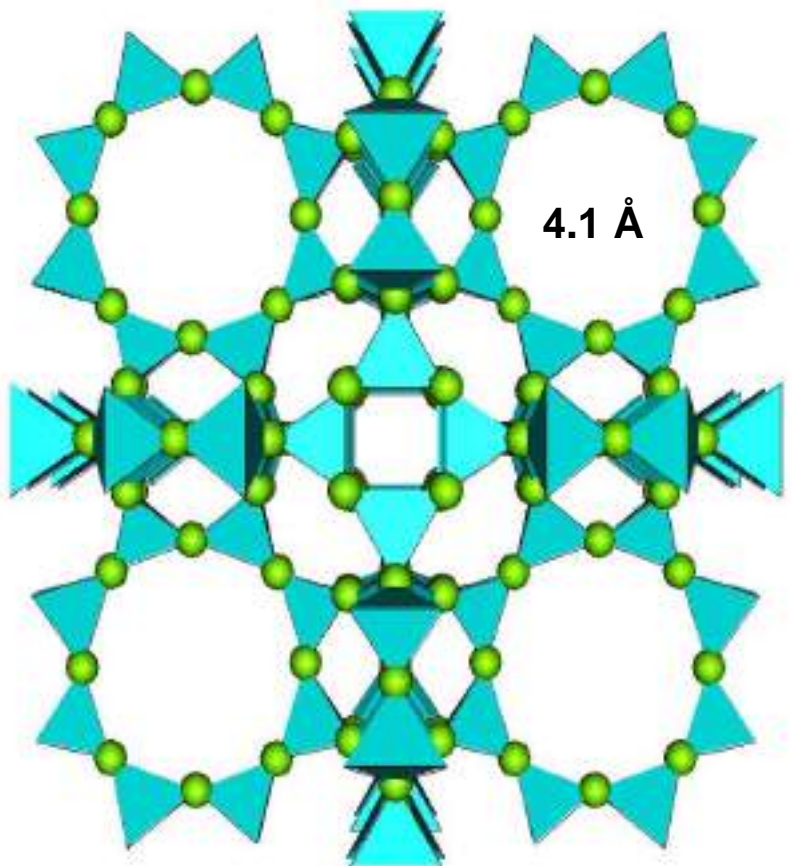
Xonolite $Ca_6Si_6O_{17}(OH)_2$

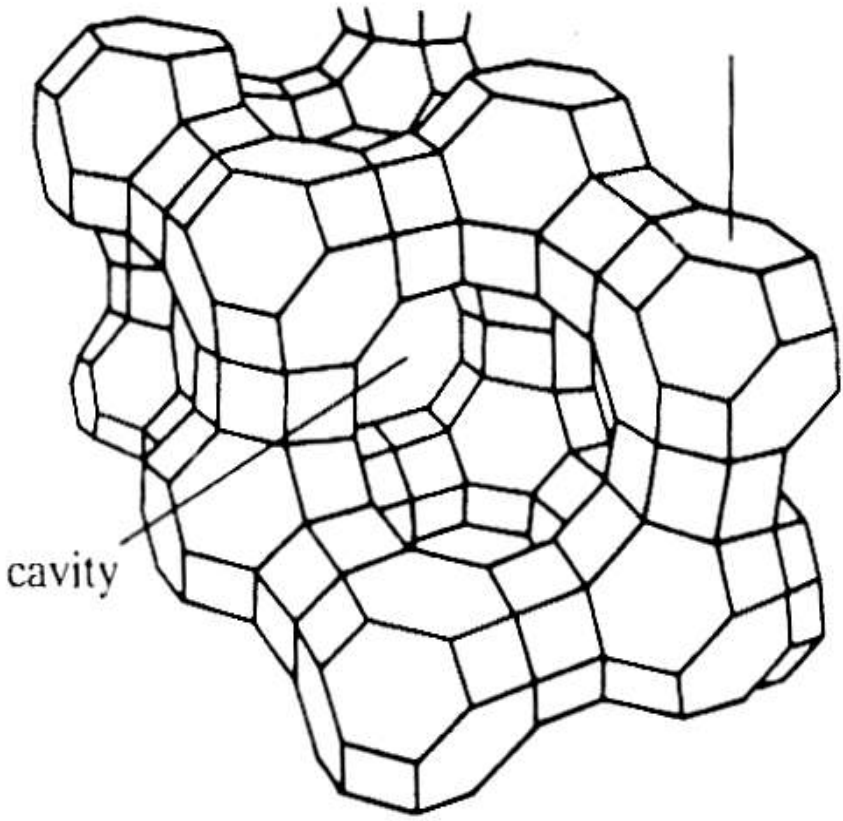


tremolite $Ca_2Mg_5(Si_4O_{11})_2(OH)_2$

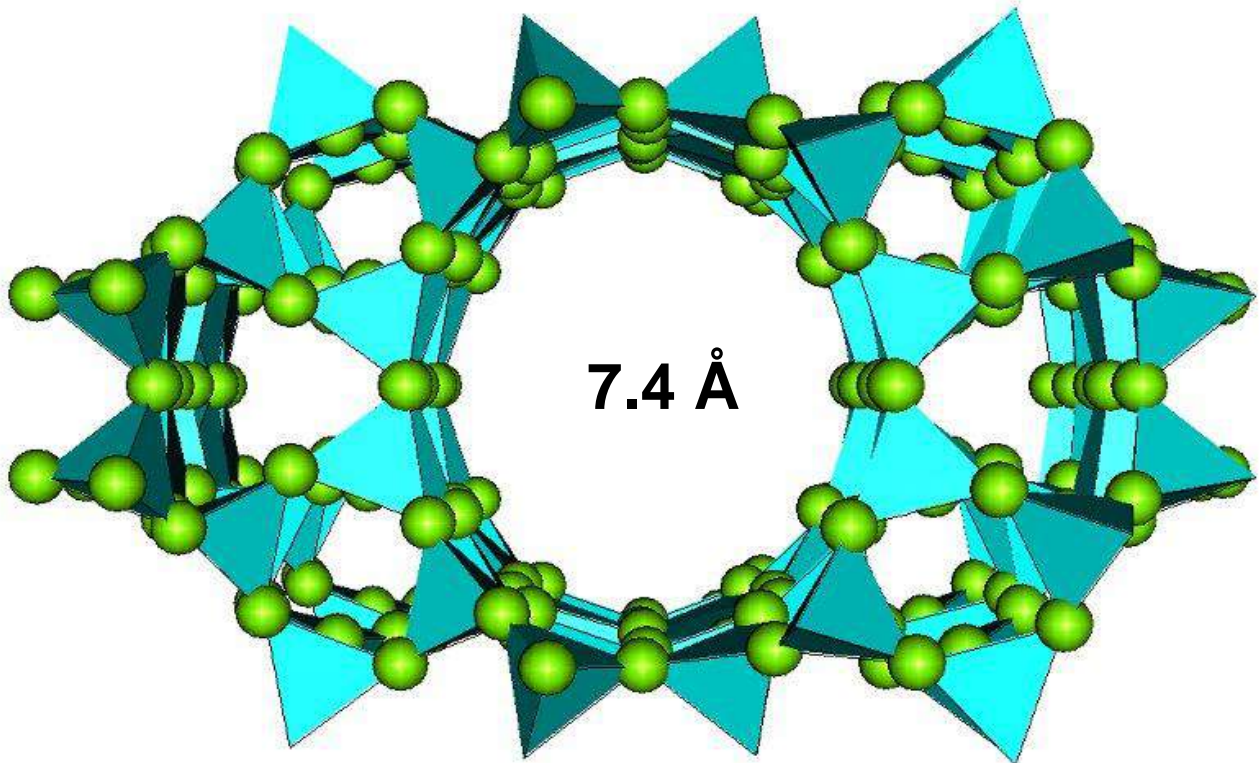


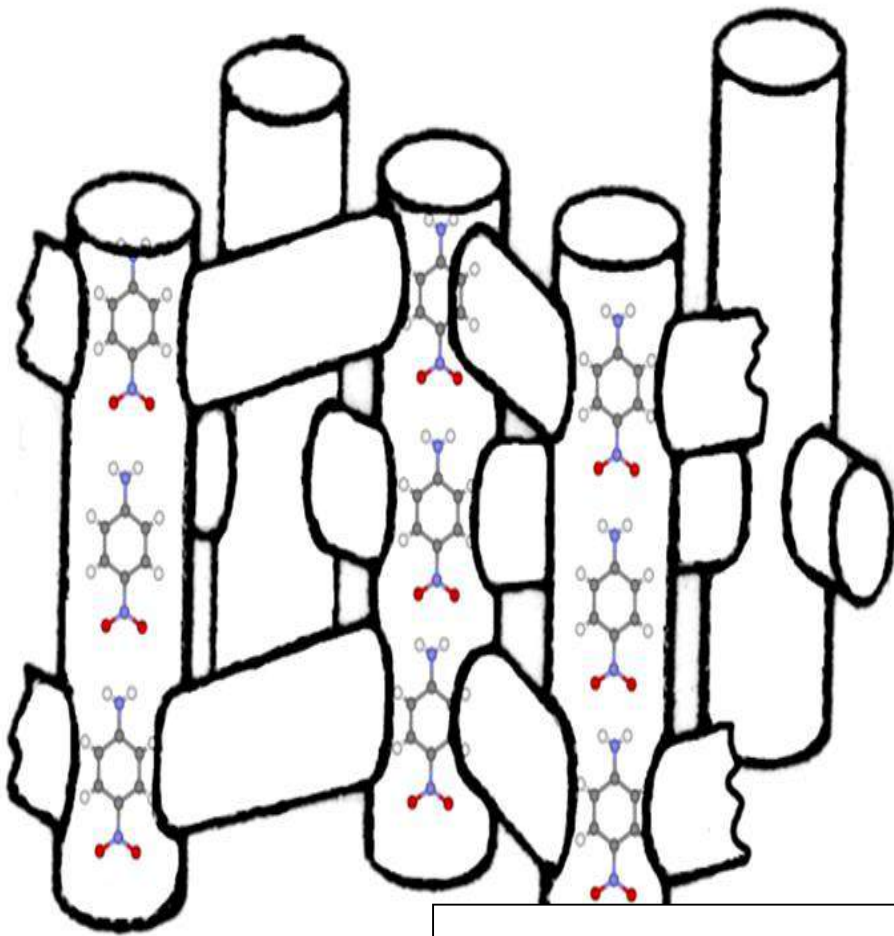
Zeolite A



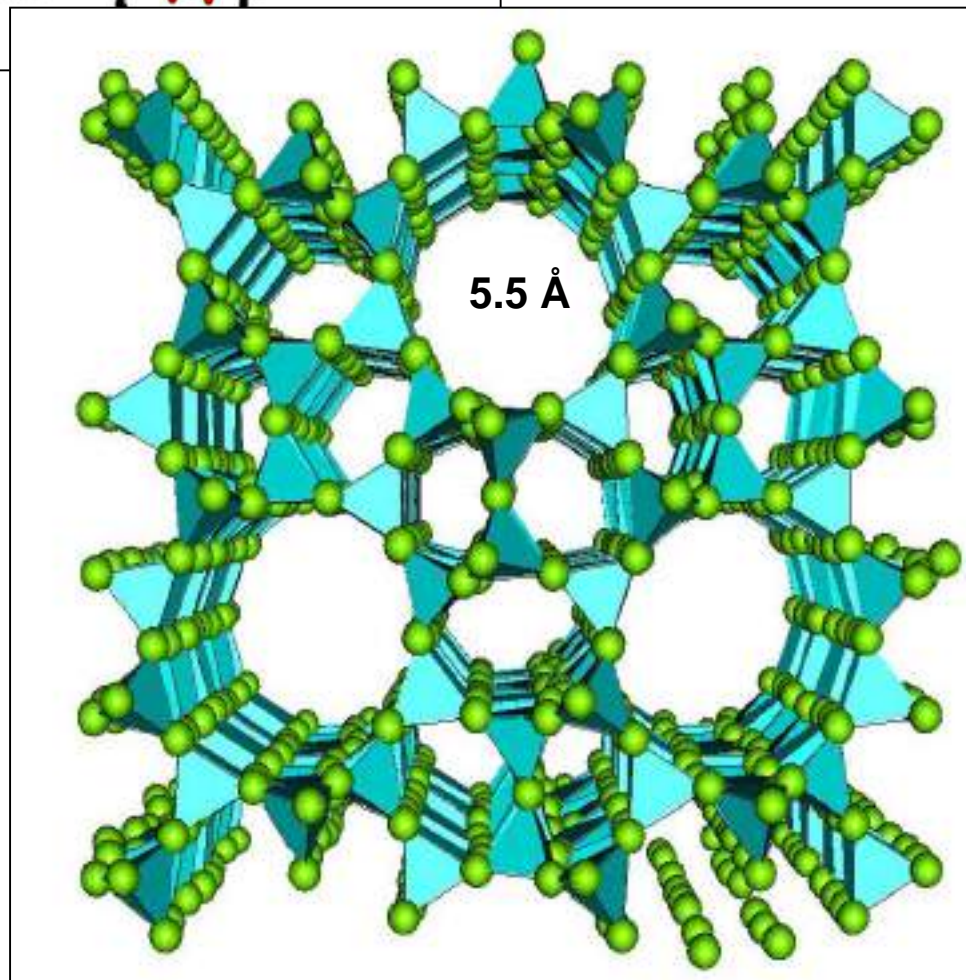


Zeolite Y
(Faujasite)

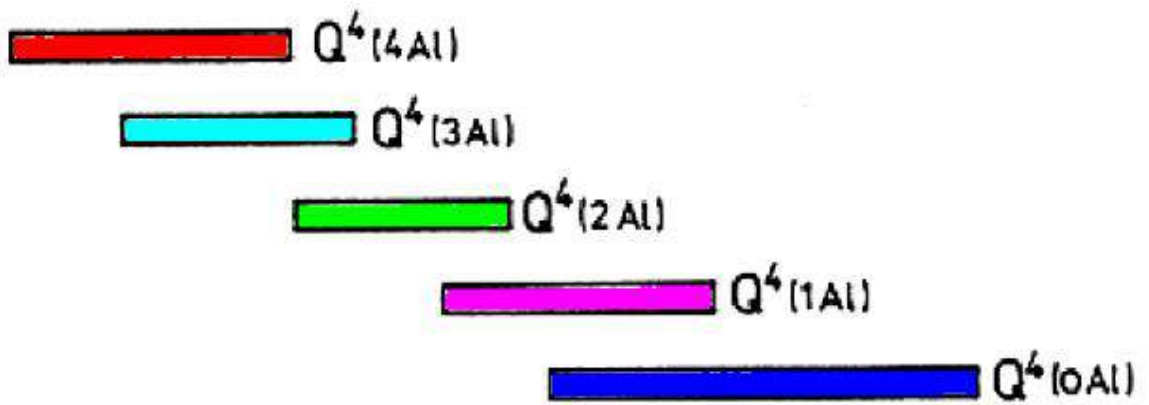




Zeolite ZSM-5



$\delta(^{29}\text{Si})$ in units $Q_4(n \text{ Al})$

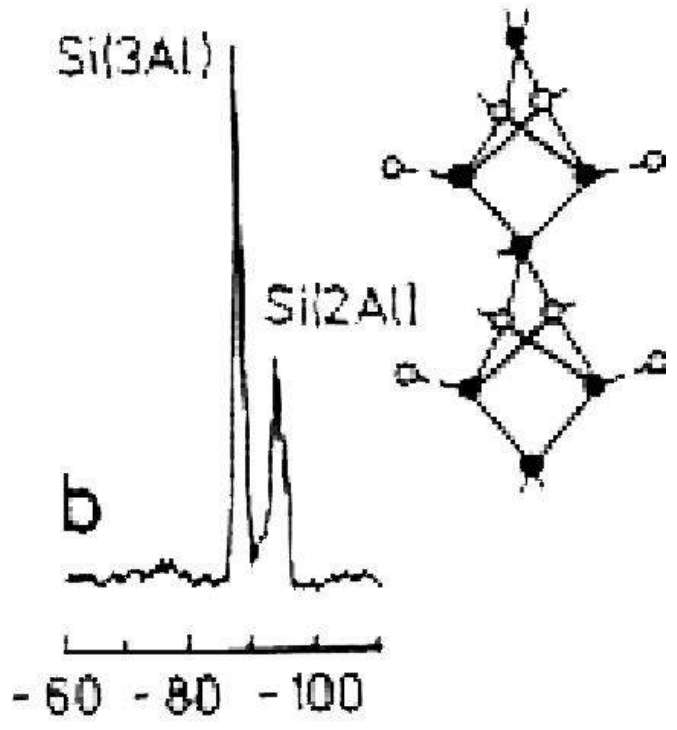
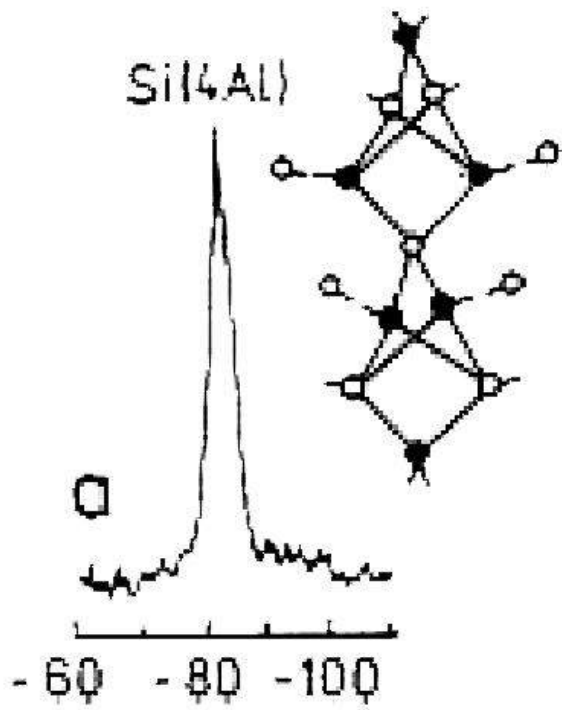


-80 -90 -100 -110 -120
 $\delta(\text{ppm})$

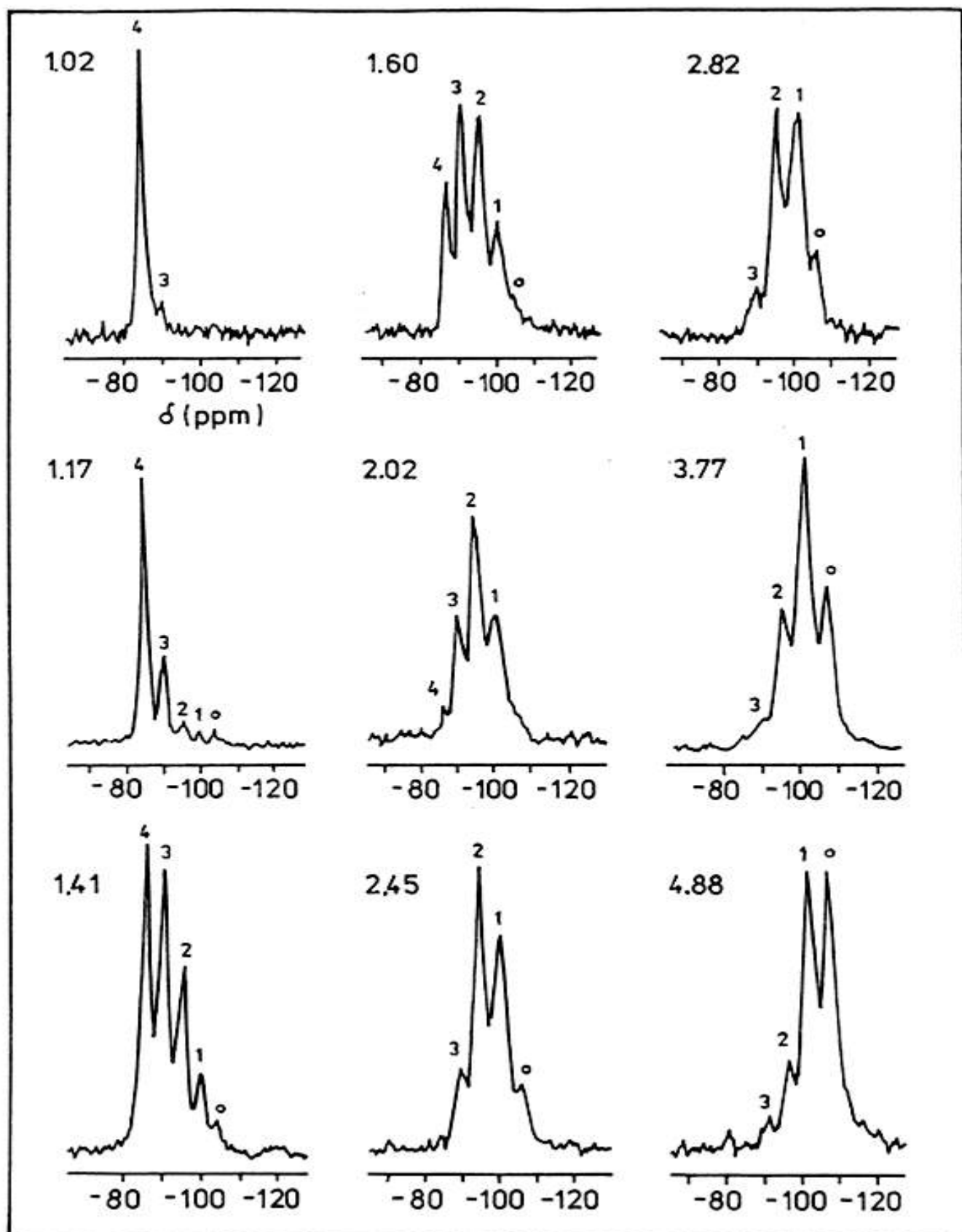
Thomsonite

Natrolite

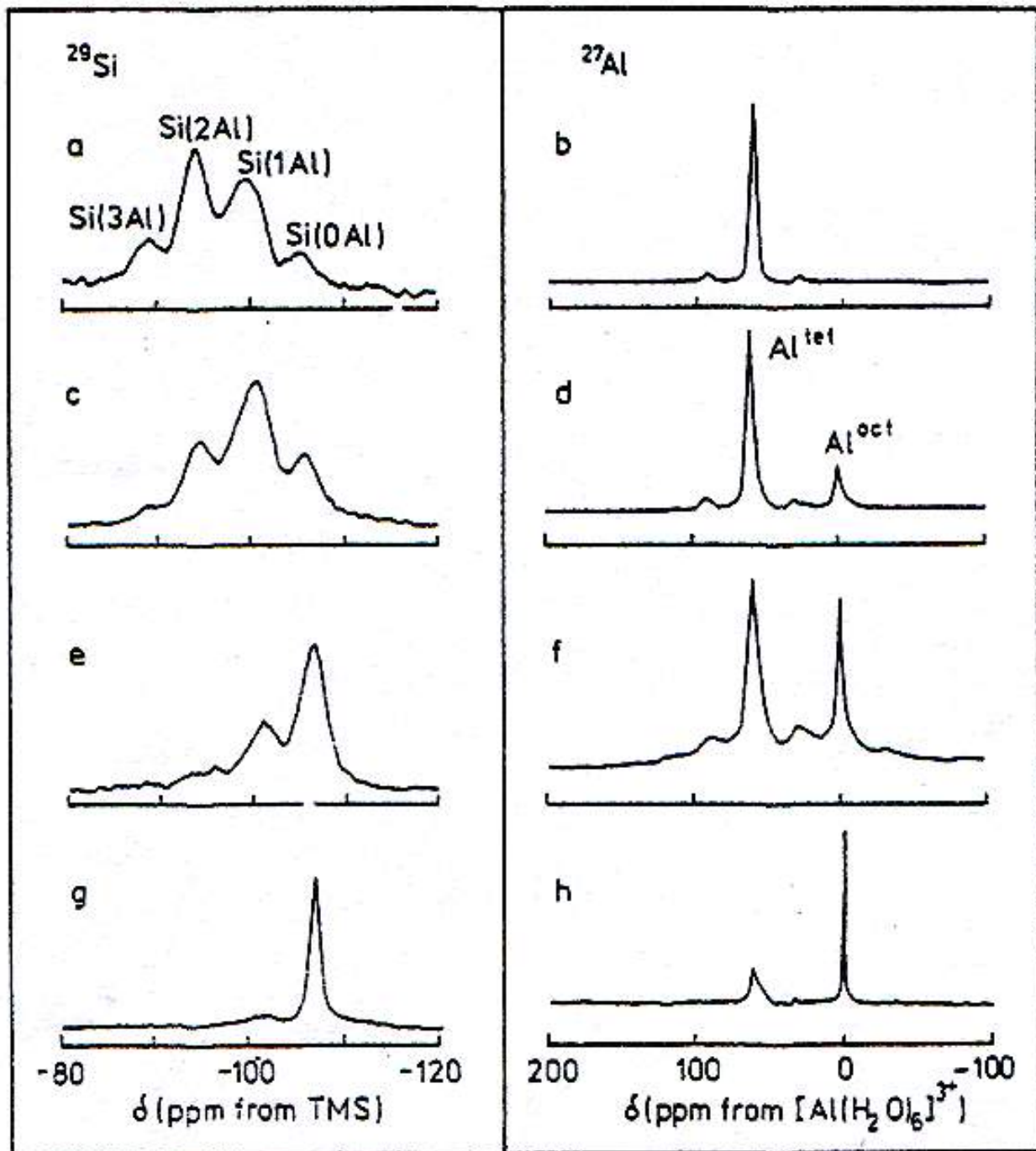
● Si ○ Al



Variation of ^{29}Si -NMR with Si/Al ratio of faujasite



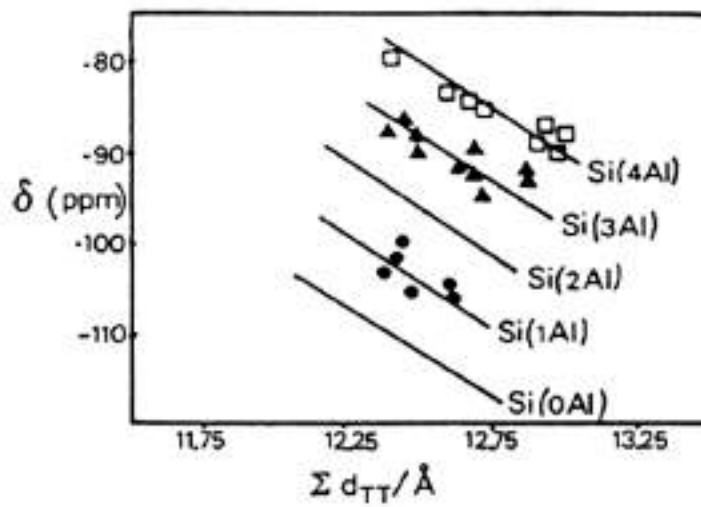
Dealumination of Y zeolite



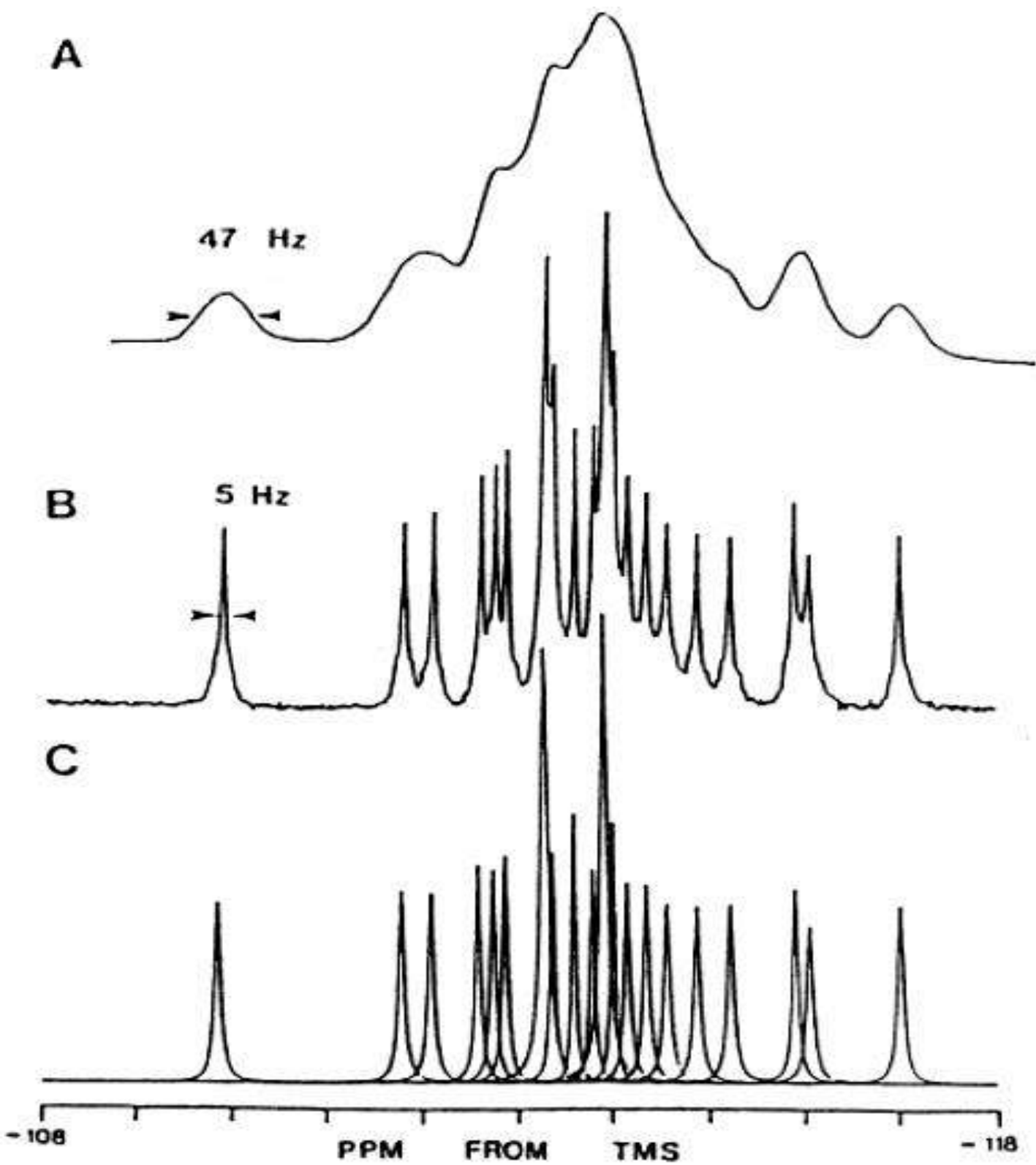
Determination of the ratio Si/Al

$$\text{Si/Al} = \frac{\sum_{n=0}^4 I_{\text{Si}}(n\text{Al})}{\sum_{h=0}^4 \frac{M}{4} I_{\text{Si}}(h\text{Al})}$$

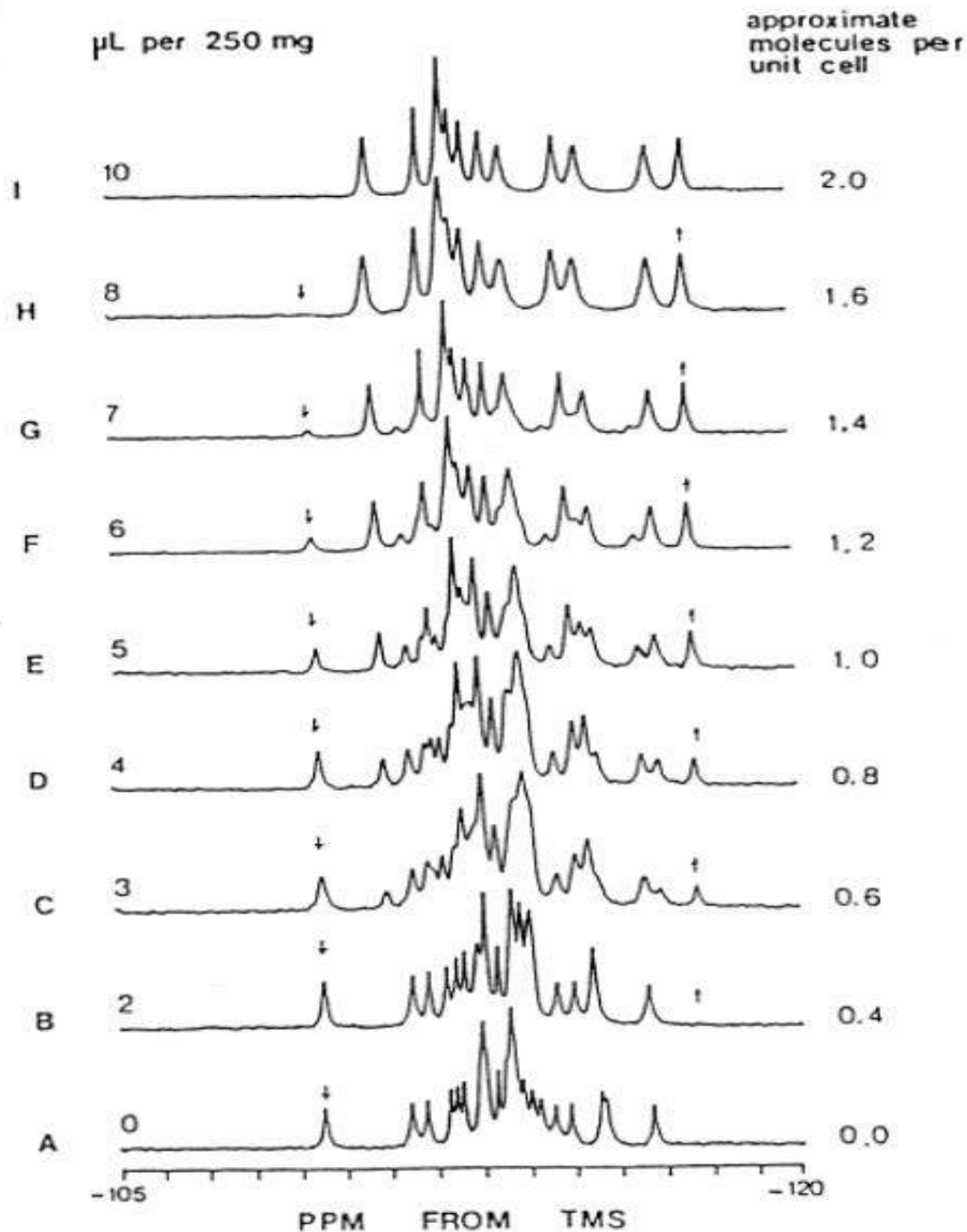
Variation of $\delta(^{29}\text{Si})$ against distance TT



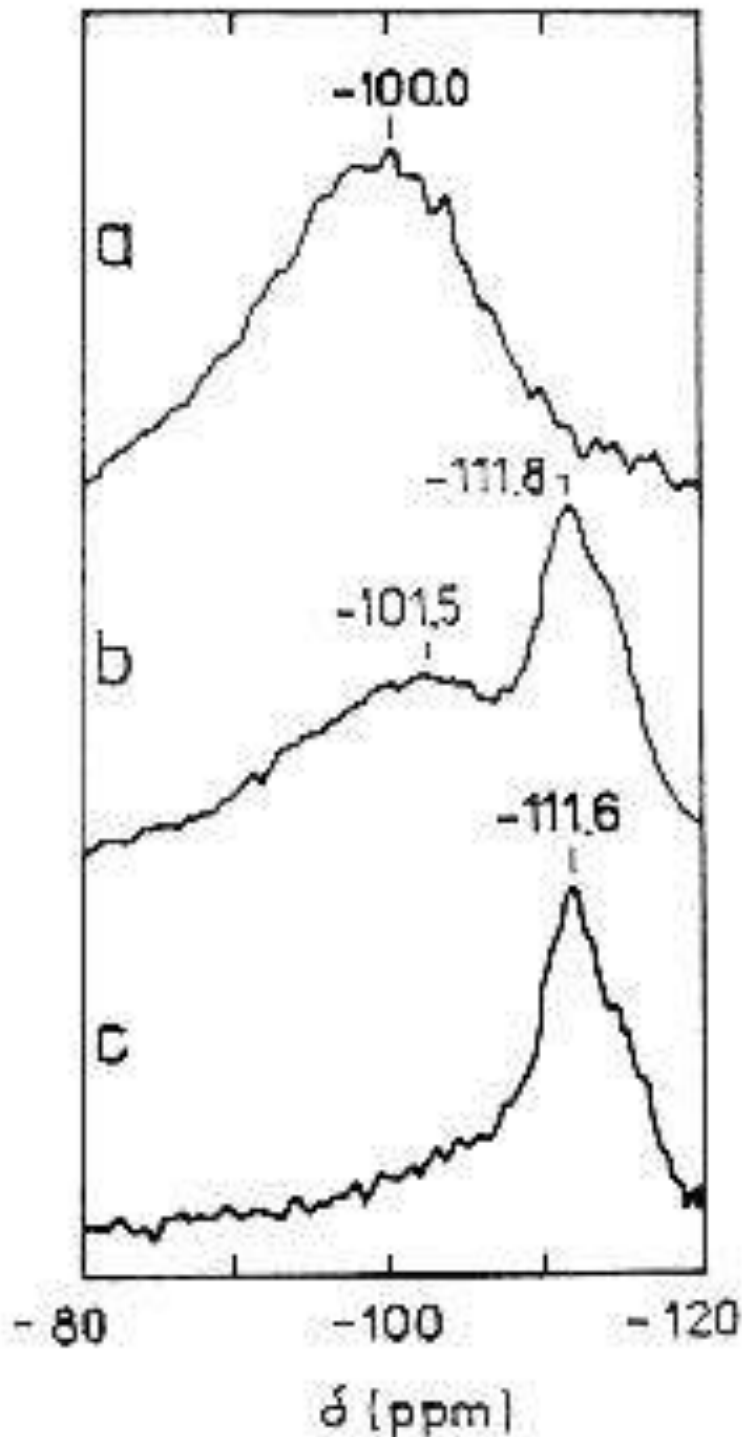
ZSM5. A: static; B: MAS; C: simulation



^{29}Si -MAS-NMR of silicalite. Influence of p-xylene concentration. Transformation of monoclinic into orthorhombic symmetry

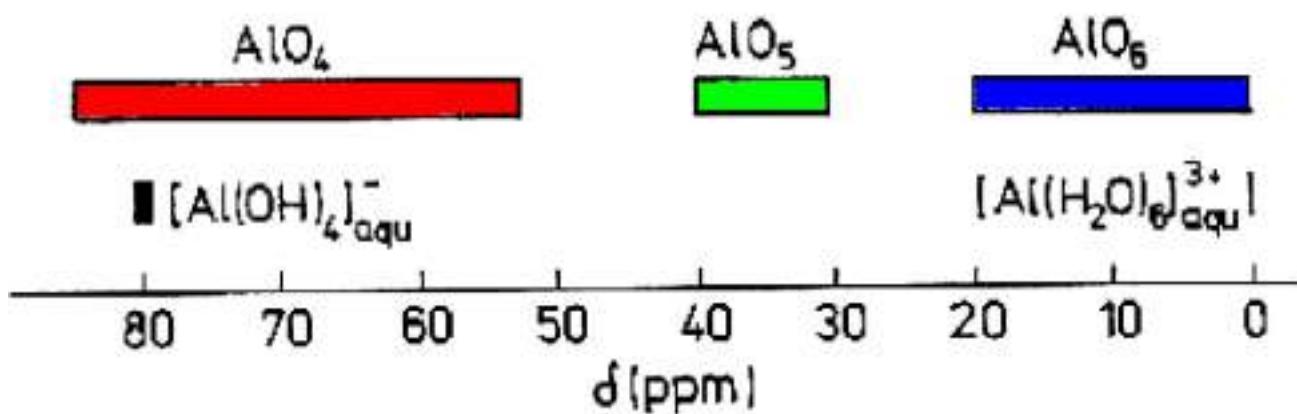


$\delta(^{29}\text{Si})$ during the synthesis of ZSM5
crystallinity: a) 0% Si/Al=1.8
b) 45% Si/Al=5; c) 100%



$\delta(^{27}\text{Al})$ of AlO_n

reference $[\text{Al}(\text{H}_2\text{O})_6]^{3+}$



Variation of $\delta^{27}\text{Al}$ versus Al-O-Si angle

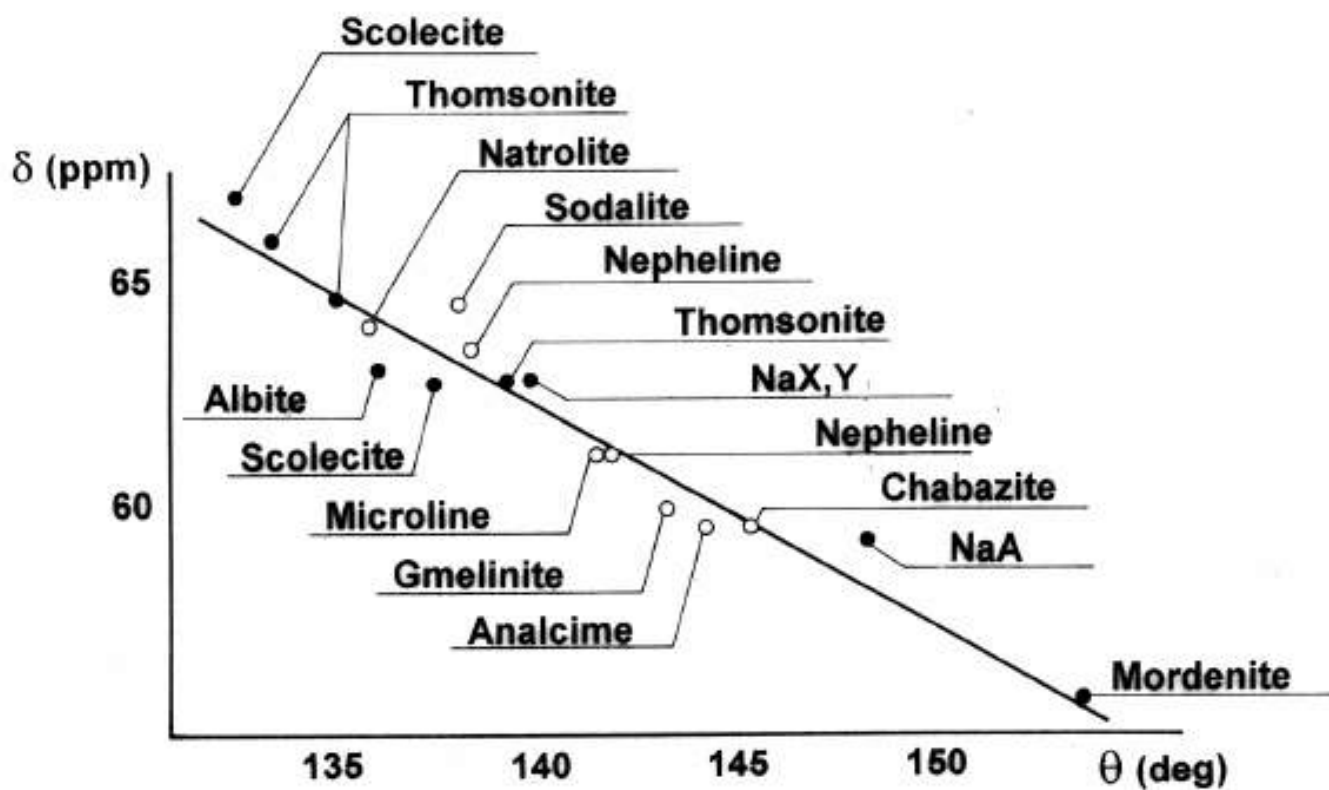
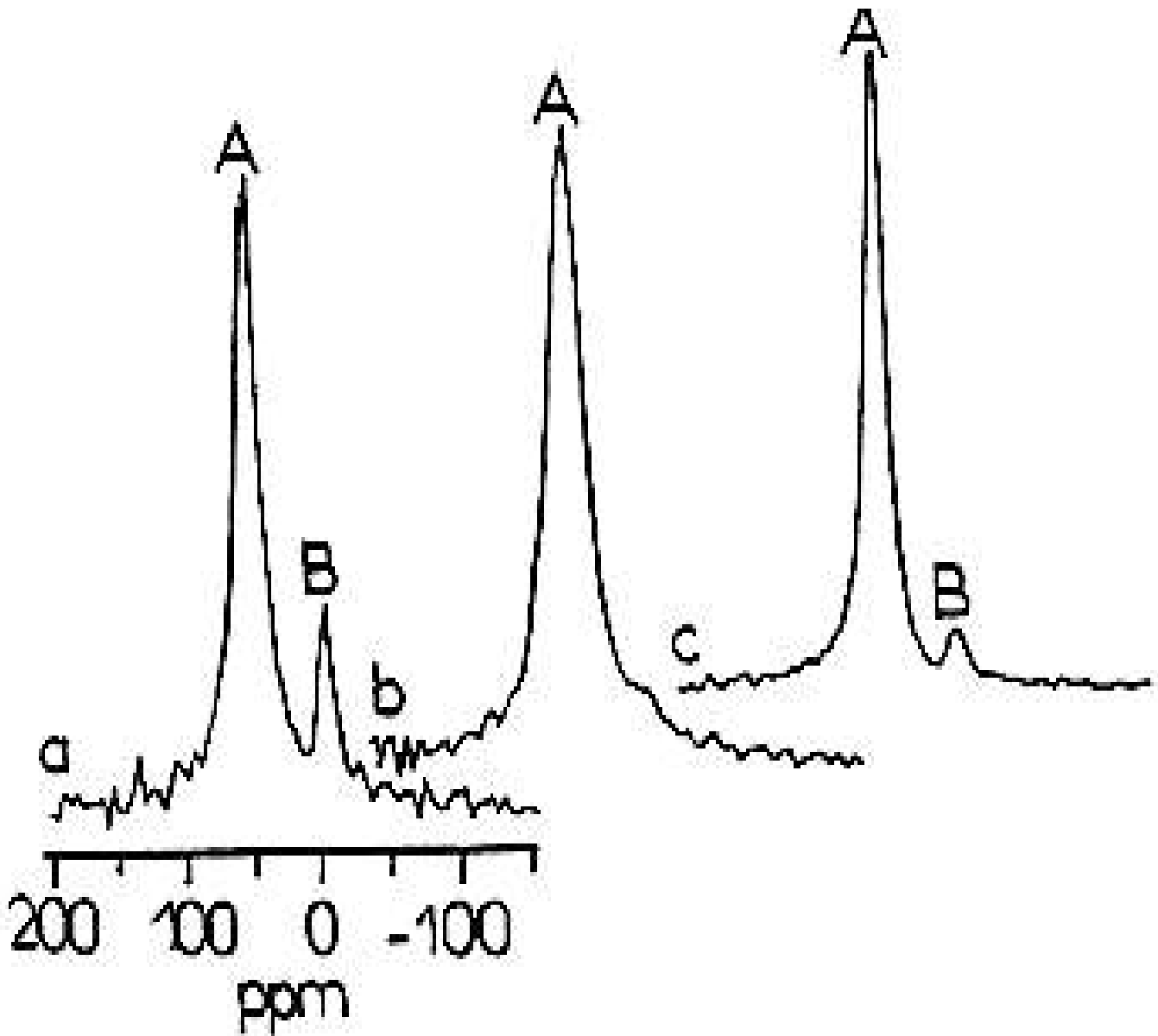


FIG. 3.36 – Variation de $\delta(^{27}\text{Al})$ avec l'angle Al-O-Si.

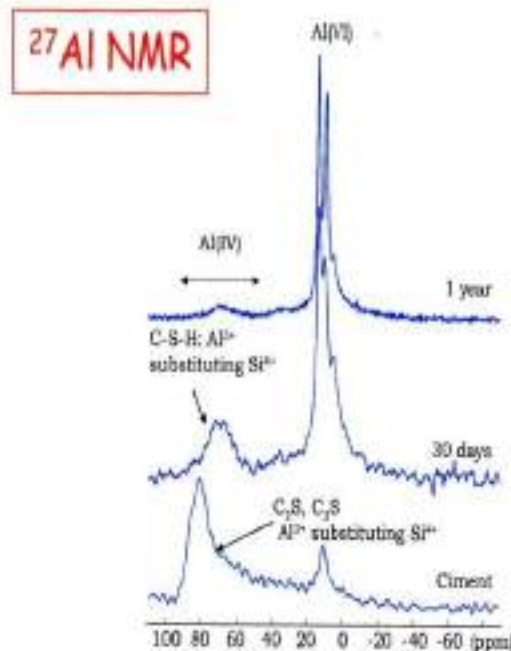
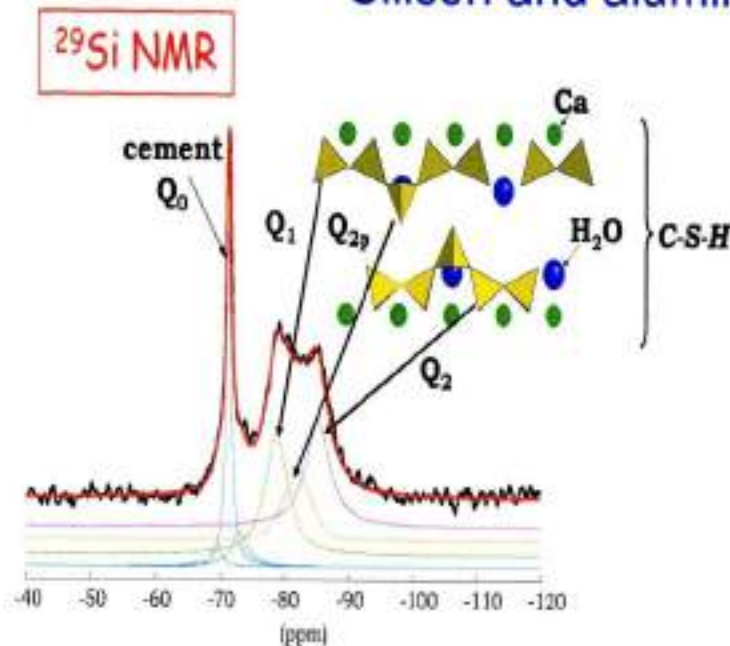
Spectre de ^{27}Al

a: sans coke; *b*: avec 10 % coke;
c: after regeneration under oxygen



NMR spectroscopy in cement science

Silicon and aluminum coordination



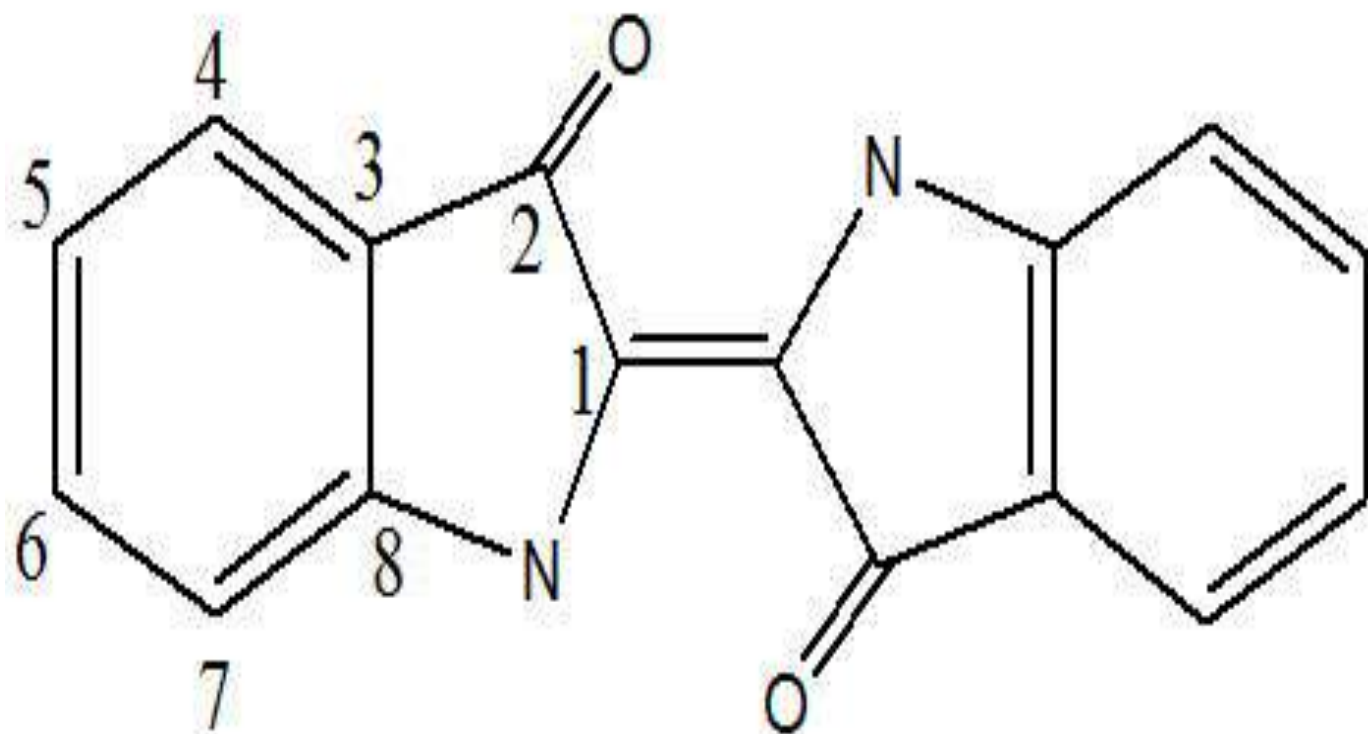
□ Solid-state NMR spectroscopy is extensively utilized (^{29}Si , ^{27}Al , ^1H):

« Application of NMR spectroscopy to cement science » Gordon and Breach, 1994

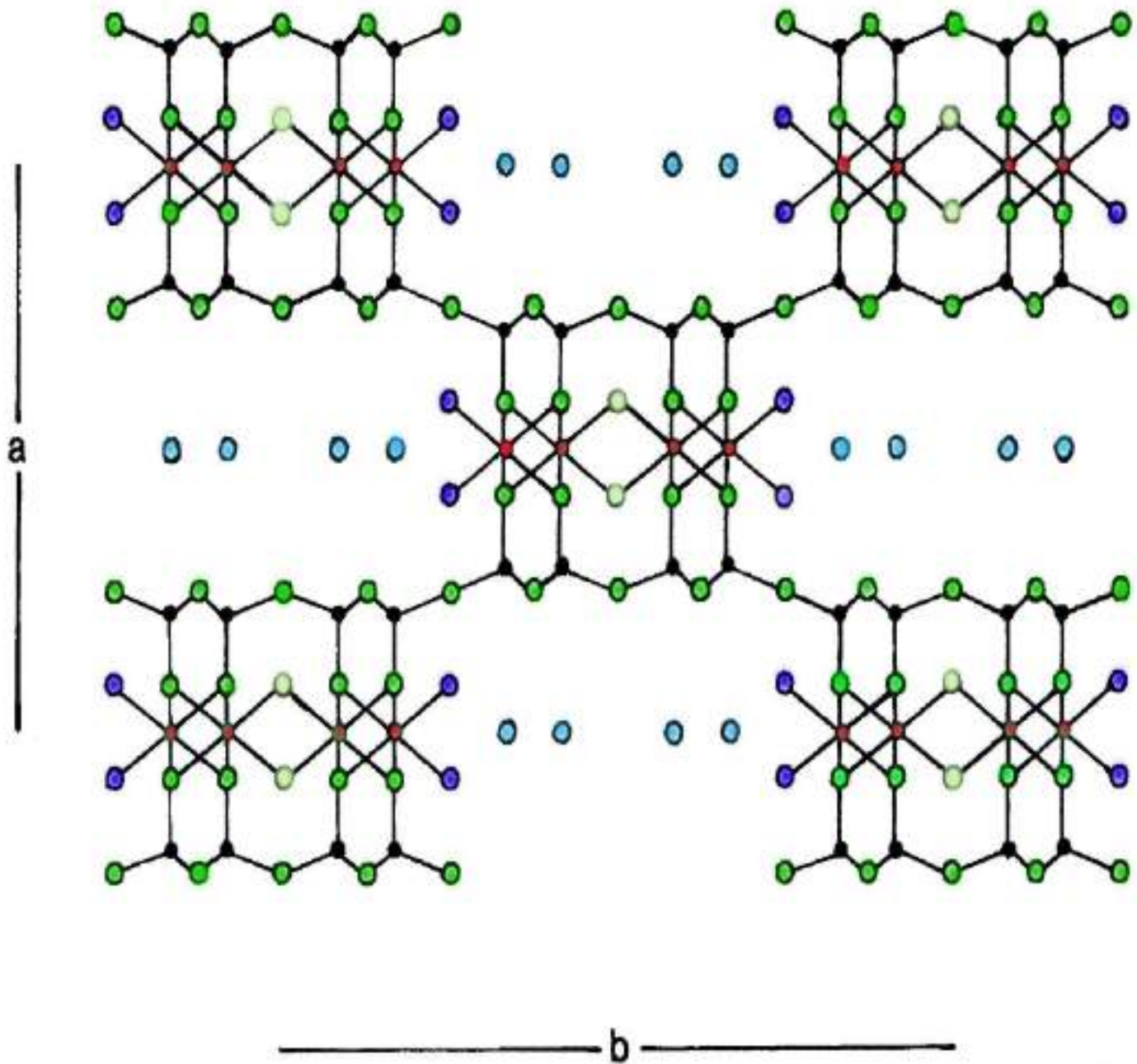
« NMR spectroscopy of cement based materials » Springer 1998

- $\text{CaO} \cdot \text{SiO}_2 \cdot \text{Al}_2\text{O}_3 \cdot \text{Fe}_2\text{O}_3 \cdot \text{SO}_3 \cdot \text{Na}_2\text{O} \cdot \text{MgO} \cdot \text{CO}_2 \cdot \text{H}_2\text{O}$
- ^{43}Ca , ^{25}Mg , ^{33}S

Indigo

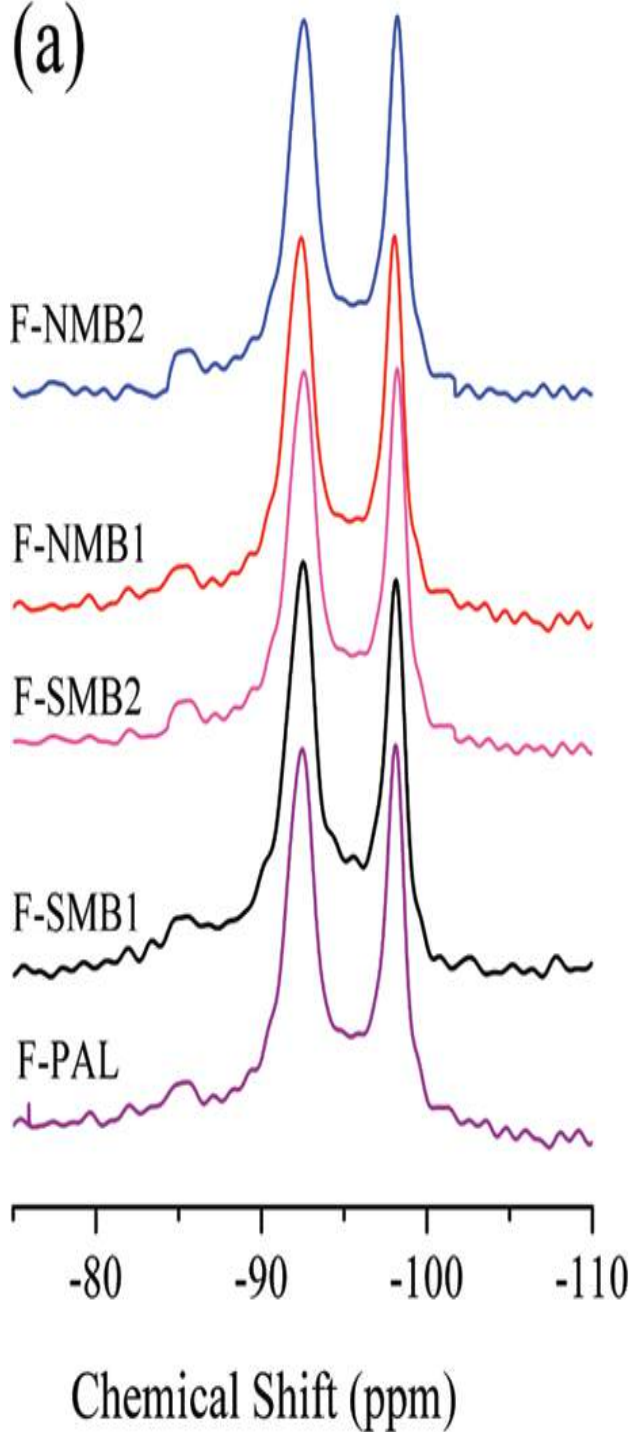


Palygorskite

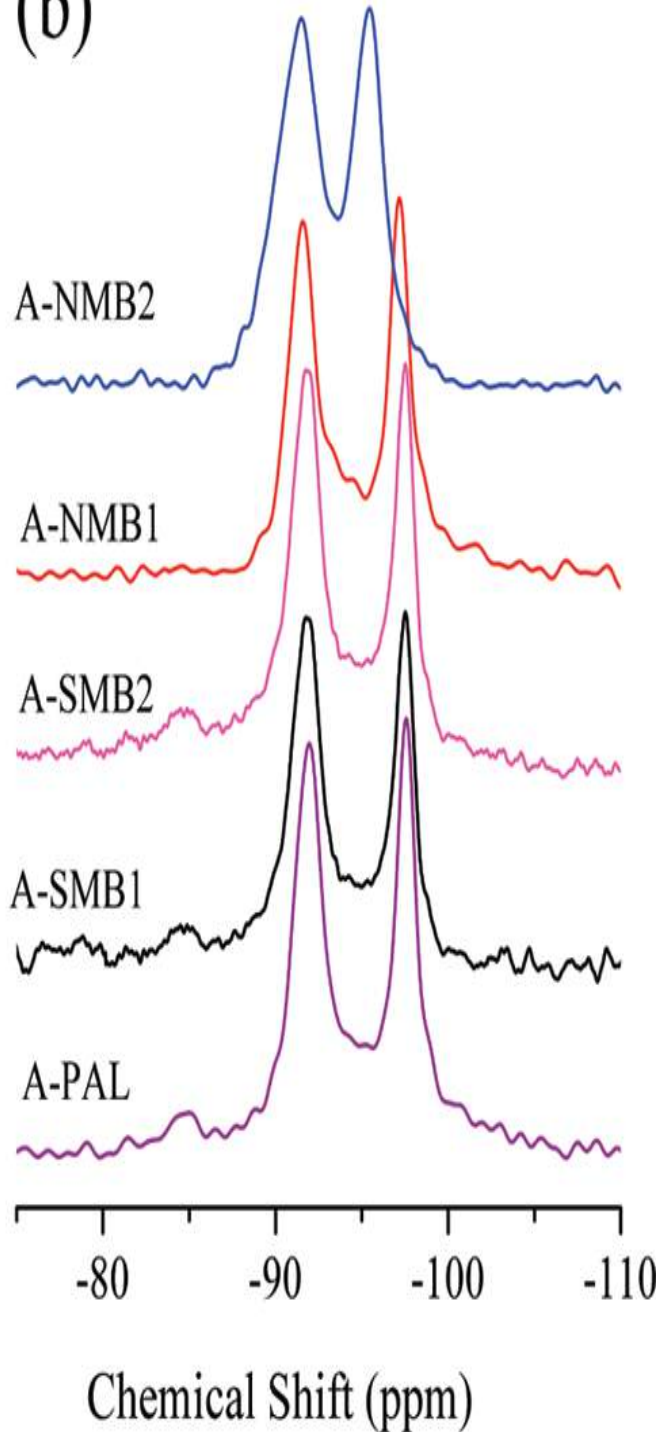


29Si MAS NMR spectra of fresh (a) and aged (b)
Maya Bluelike pigments.

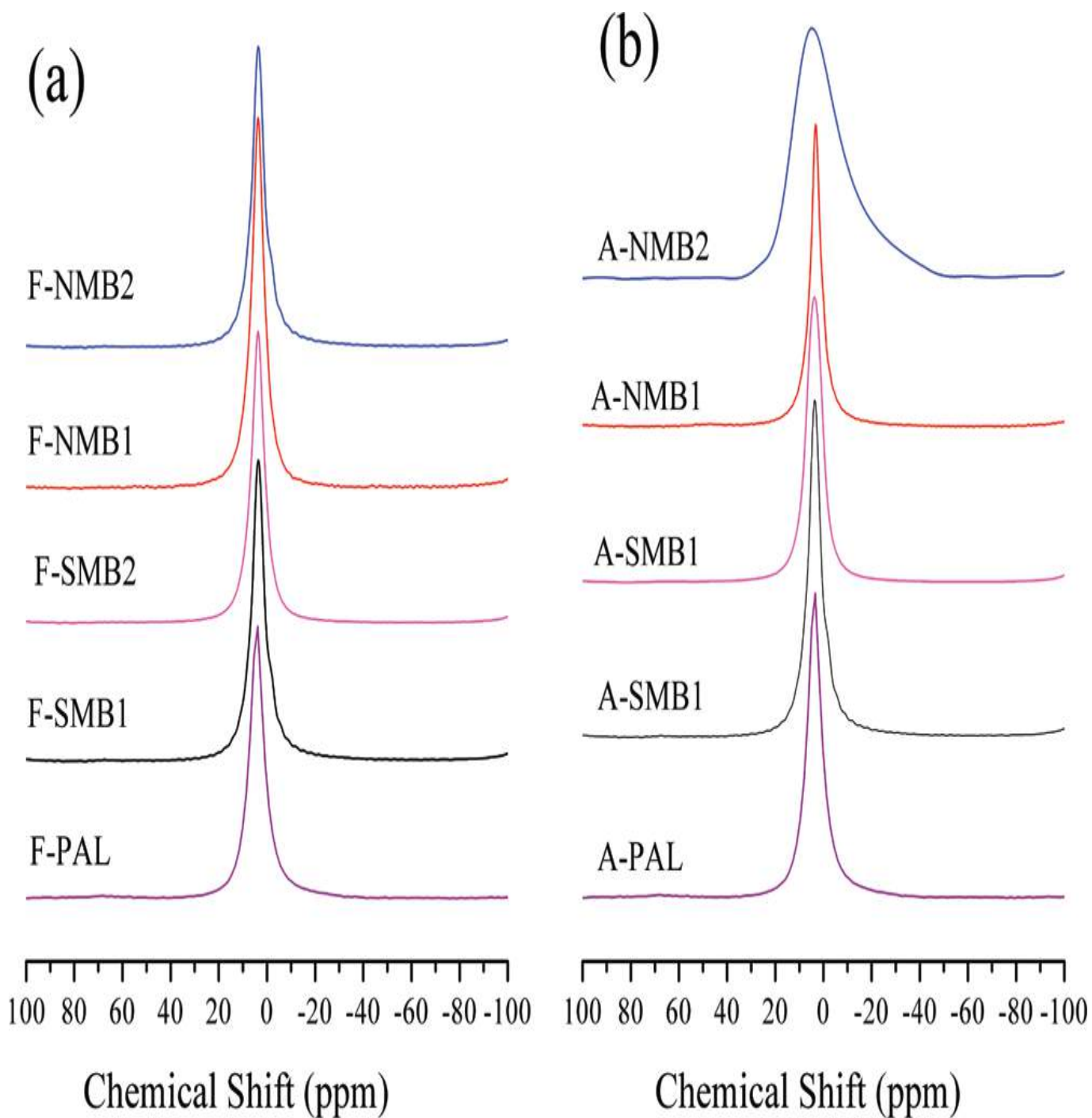
(a)



(b)



27Al MAS NMR spectra of fresh (a) and aged (b)
Maya
Blue-like pigments.



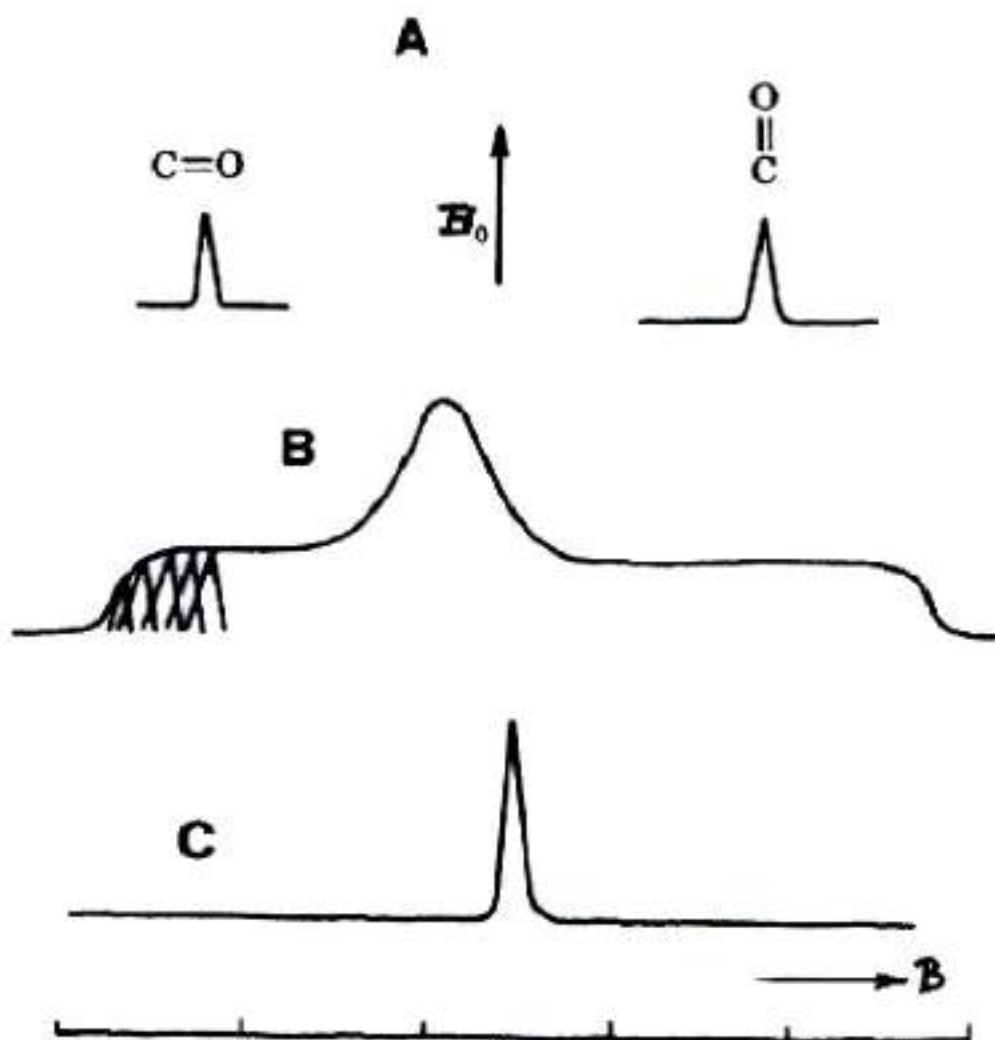
Chemical shift anisotropy

Schematic representation of the ^{13}C NMR absorption of a carbonyl functionality

A- single crystal in two different orientations/ B_0

B- In a polycrystalline sample where there are contributions from the random distribution of orientations.

C- In solution



Chemical shift anisotropy

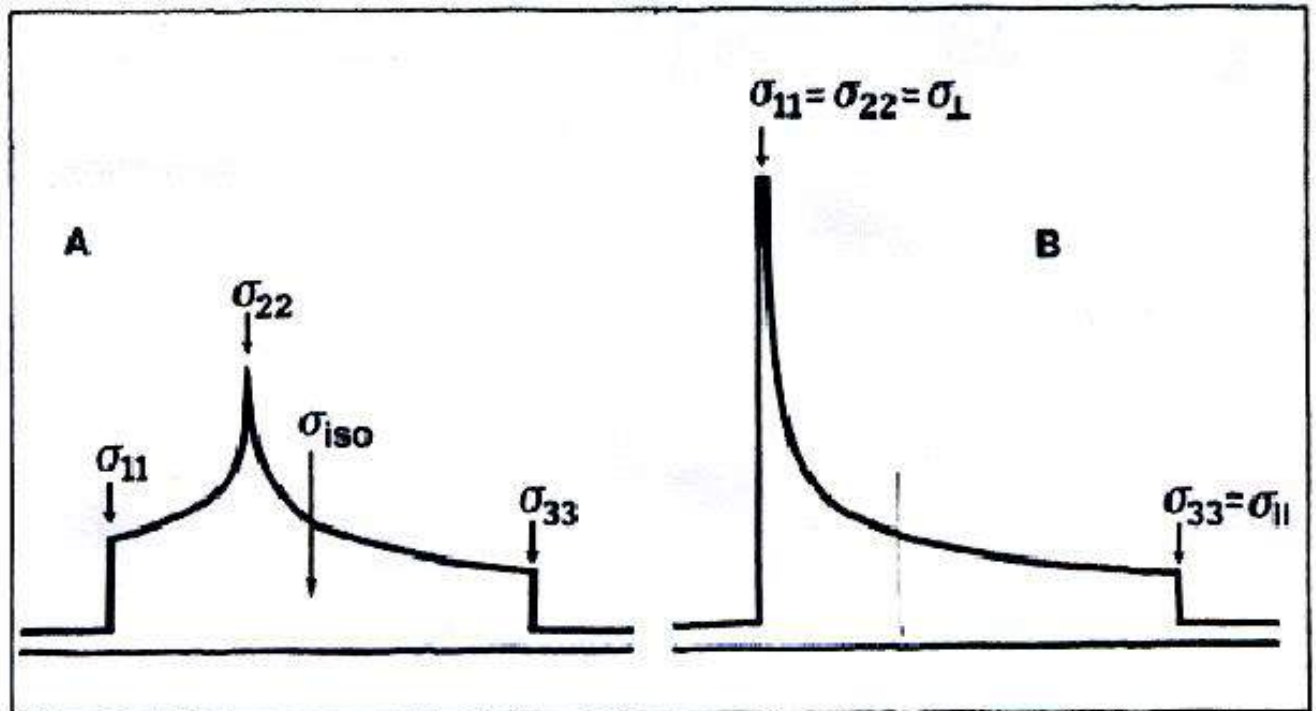
MAS removes all solid-state interactions.
Multi-pulse sequence does not remove the
chemical shift anisotropy.

Asymmetric shift anisotropy

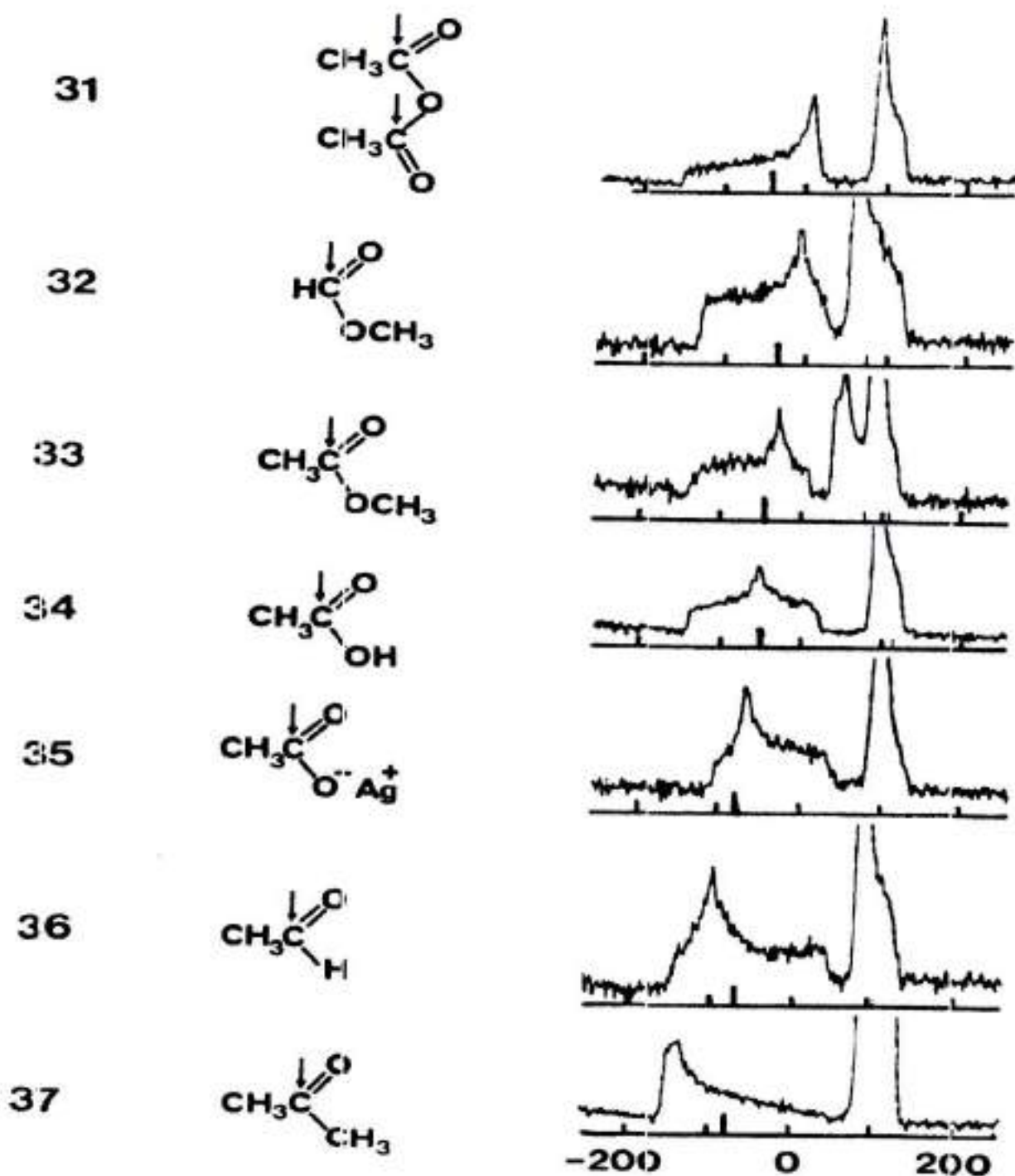
$$\sigma_{iso} = \sigma_{11} + \sigma_{22} + \sigma_{33}$$

Axially shift anisotropy

$$\sigma_{11} = \sigma_{22} = \sigma_{\perp} \quad \sigma_{33} = \sigma_{\parallel}$$

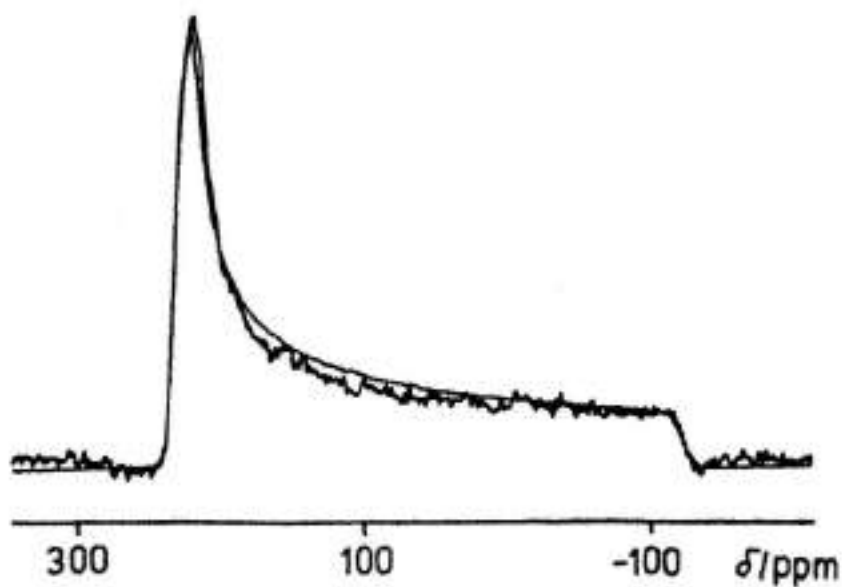


^{13}C spectra of polycrystalline compounds containing carbonyl groups.
Low-field: CO; high field: CH₃

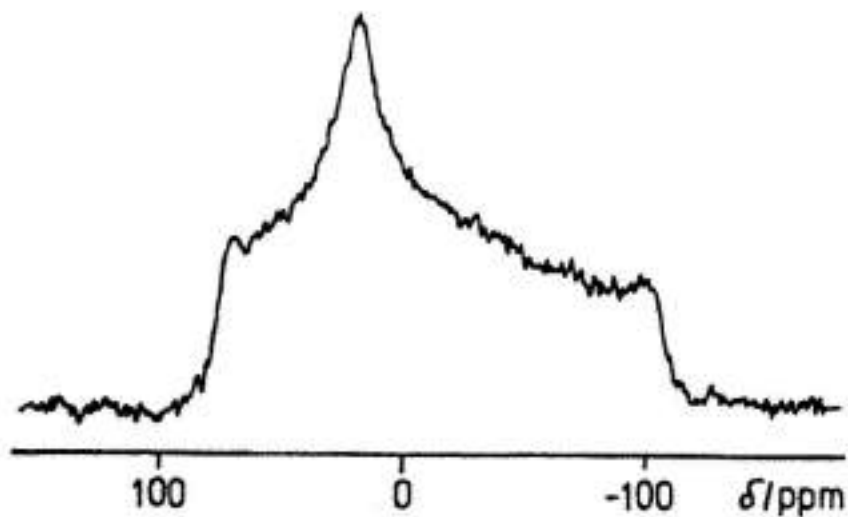


^{31}P NMR

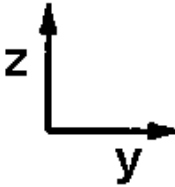
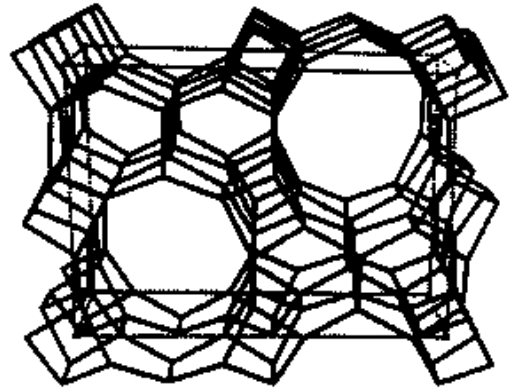
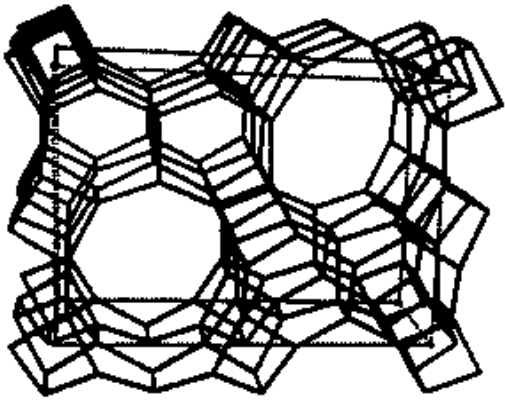
P_4O_6



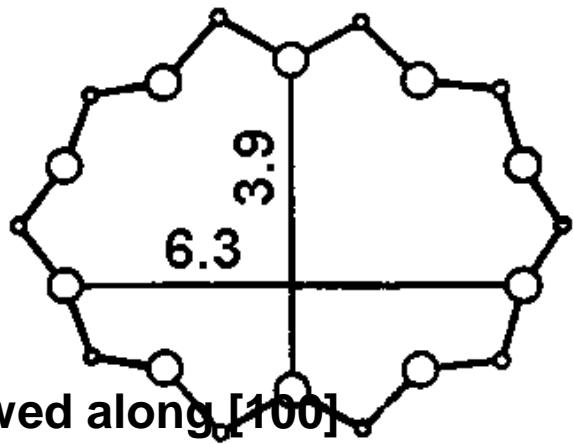
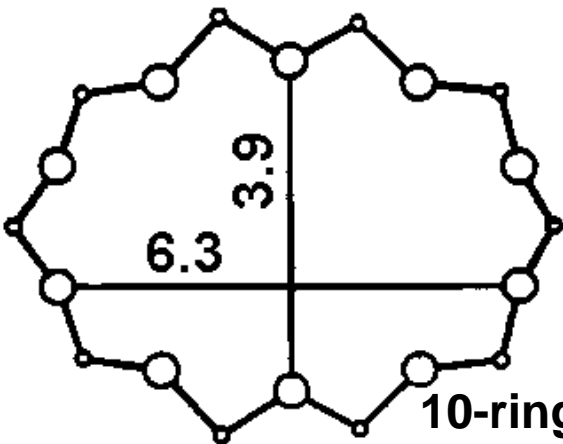
$\text{Ba}(\text{Et})_2\text{PO}_4$



SAPO 11; AIPO11

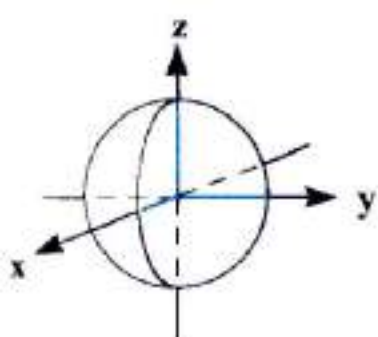
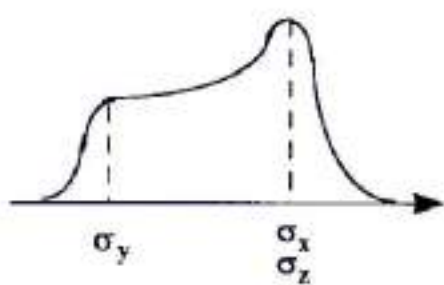
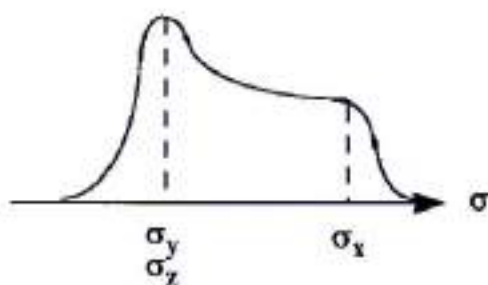
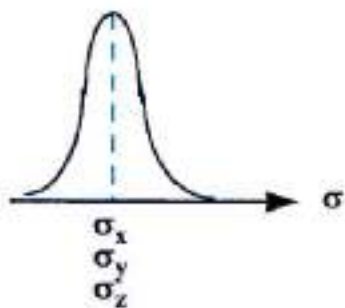
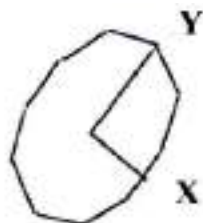


Framework viewed along [100]

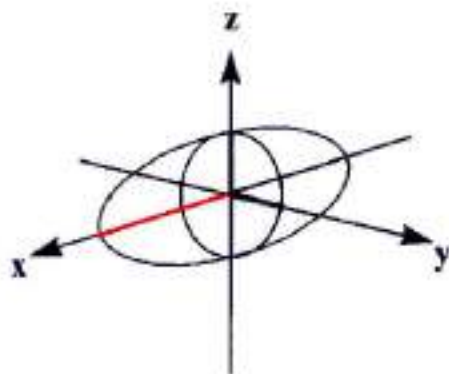


10-ring viewed along [100]

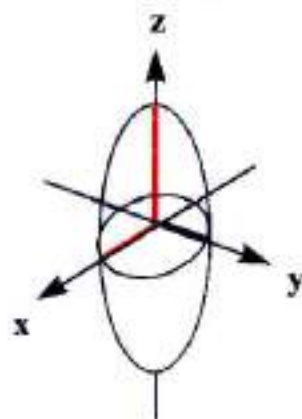
Anisotropy of chemical shift



$$\sigma_x > \sigma_y = \sigma_z$$

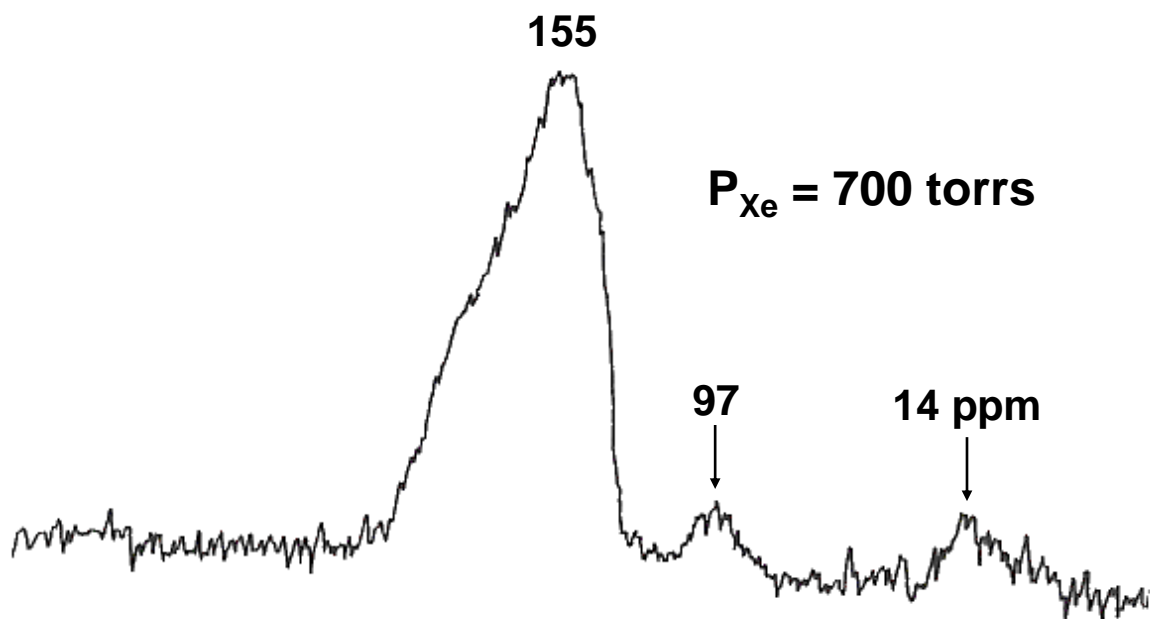
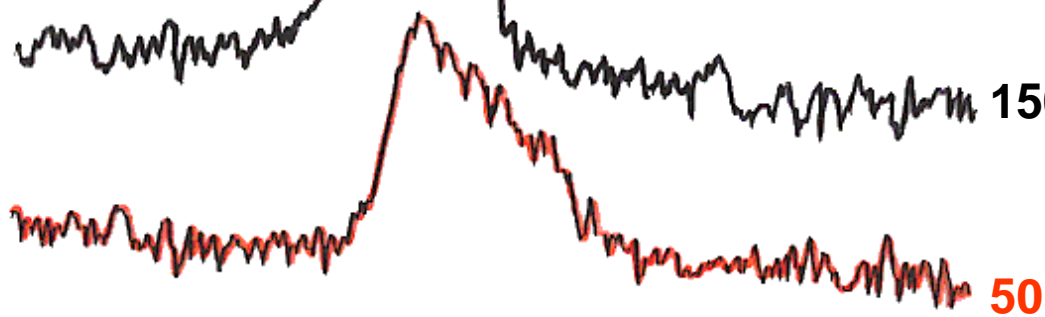
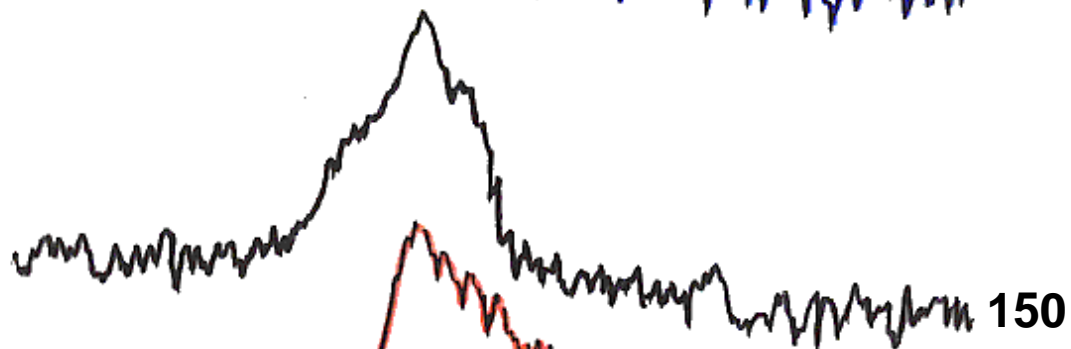
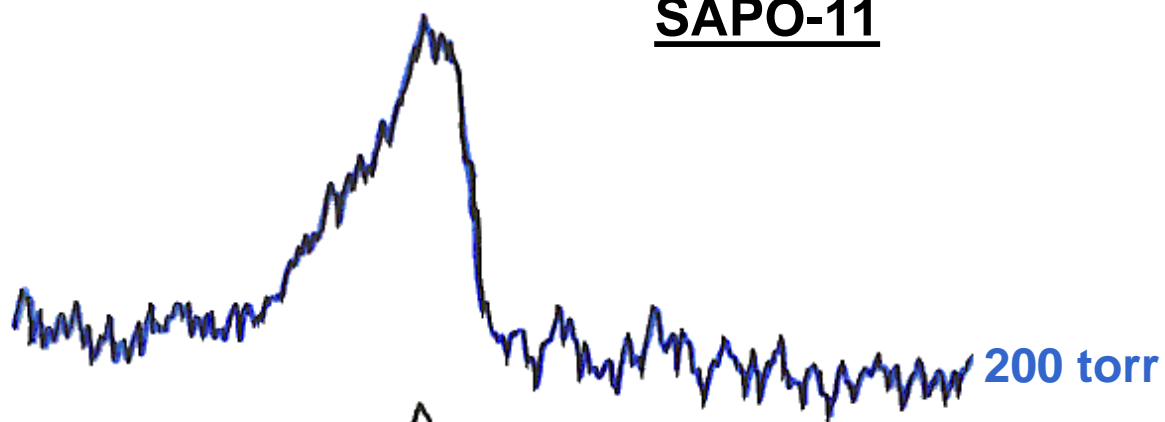


$$\sigma_x > \sigma_y = \sigma_z$$



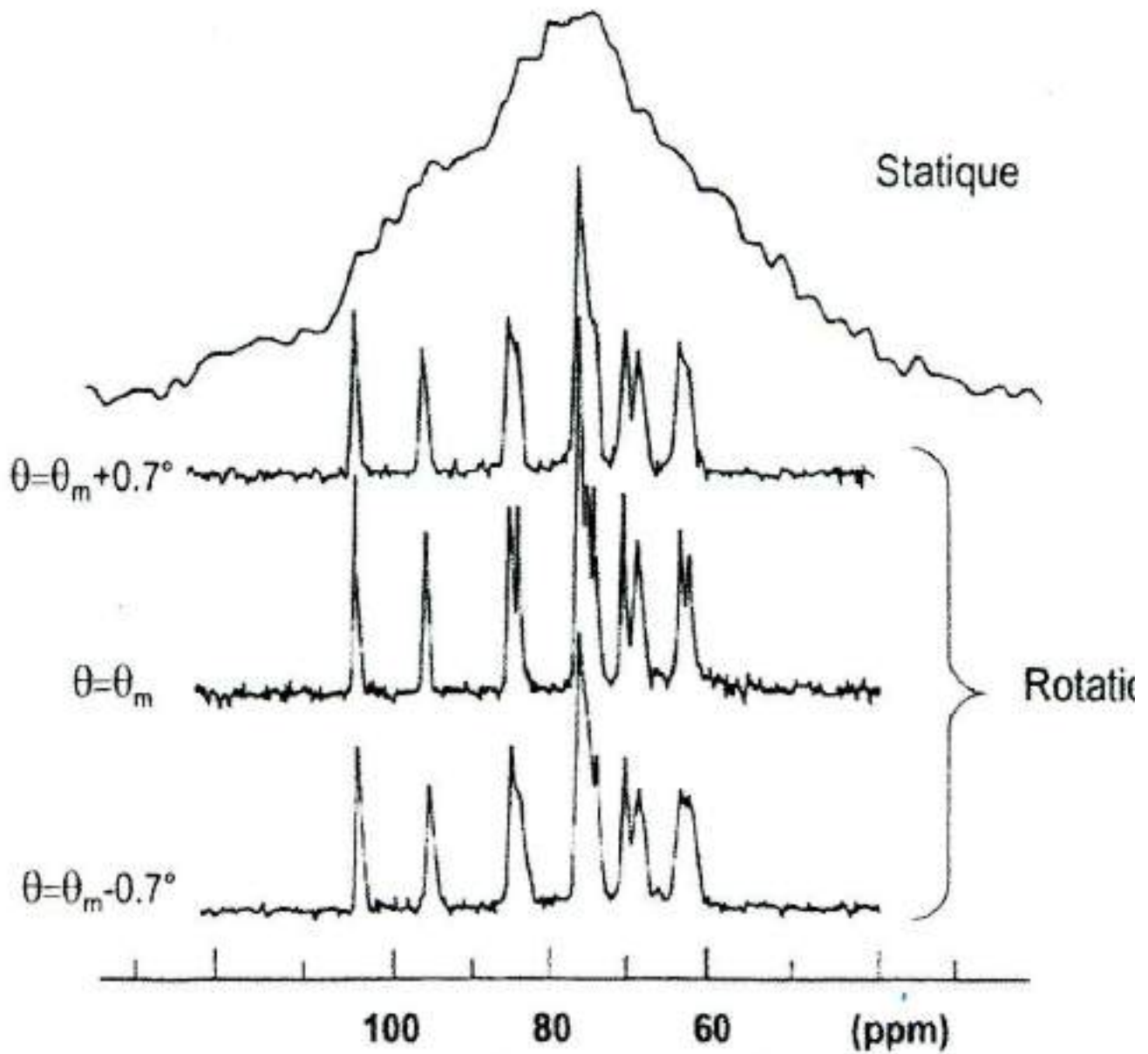
$$\sigma_y < \sigma_x = \sigma_z$$

SAPO-11

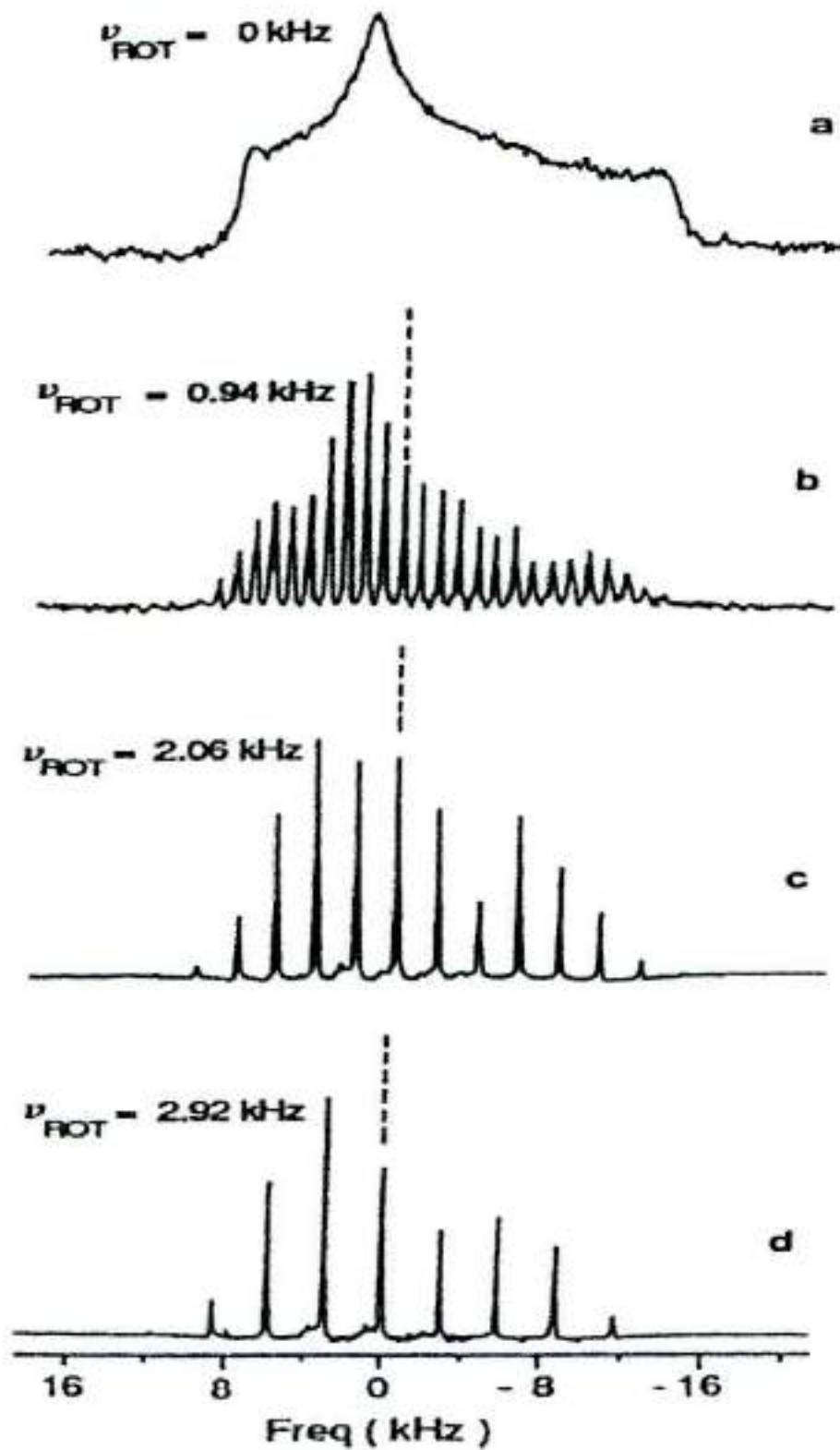


SAPO 11-3

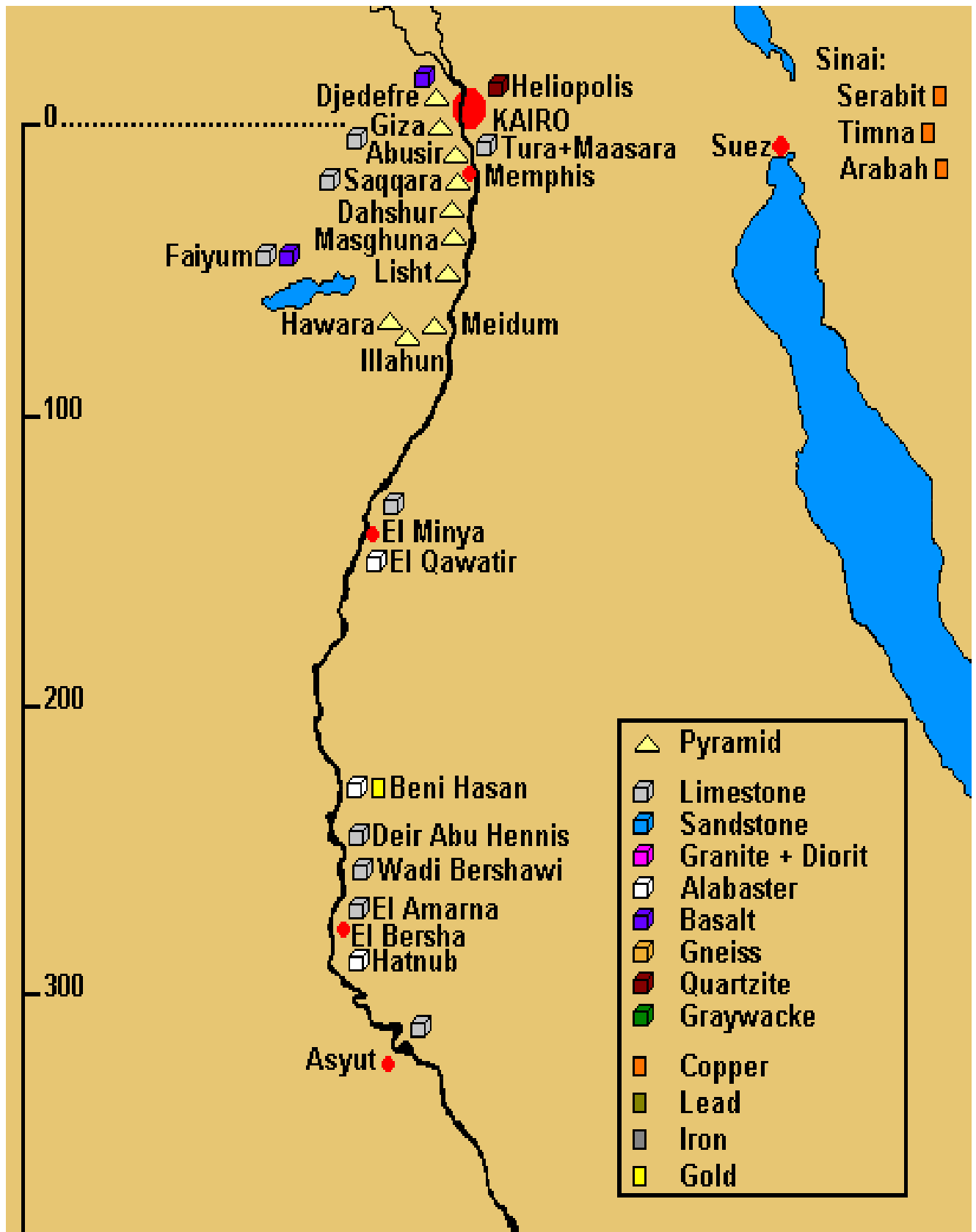
Accuracy of the angle



Influence of the rotation on the sidebands



Pyramids and Limestones



First pyramid (step pyramid) built for Pharaoh DJOSER by his architect IMHOTEP in Saqqara (Memphis) 2630-2605 b.c.

height: 62 m; base: 120/110 m



Rhomboid Pyramid of Sneferu (Dahshour)
(height: 105; base: 188/60)



Pyramids of Gizeh (Giza)



Pyramid of the Pharaoh Kheops (Khufu)
(initial height: 146 m; square base: 230 m)
(2584 bc.....20-25 years.?)
2.5 million blocks, 2.5...60 tons



Senefru's bent Pyramid in Dahshour

Kenneth J.D. MacKenzie *et al*, *Materials Letters*, 65 (2011) 350

A: pyramid stone; B: Tura quarry limestone
C: Khufu quarry limestone; D: Diamaceous earth

